

GxE and GxG interactions

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Background I

Various kinds of E and G

- Latent/Observed

GxG interaction

- Observed x Observed

- Latent x Latent

- Latent x Observed

Background II

Latent Genotype x Measured Environment Interaction

- Kendler, KS & Eaves, LJ (1986) Models for the joint influence of genotype and environment on liability to psychiatric illness. *Psychiat* **143**:279-89
- Heath, AC, Cates, R, Martin, NG, Meyer, JM, Heath, AC, Heath, MC & Eaves, LJ (1993) Genetic contributions to the liability to alcoholism: Comparisons across cohorts and across environments. *Journal of Substance Abuse* **5**: 221-246
- Neale, MC & Cardon, LR (1992) *Methodology for Genetic Association Studies of Twins & Families*. Dordrecht, NL: Kluwer Academic Publishers

Background III

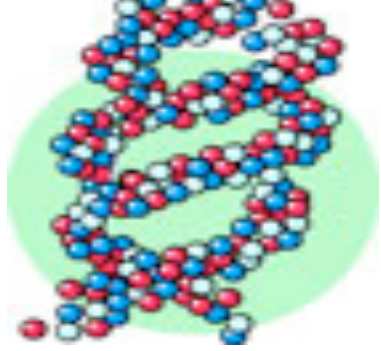
1994: Definition variables in Mx

- Enables ‘continuous’ version of multiple group analysis

Purcell, S (2002). Variance components models for environment interaction in twin analysis. *Twin Res*,

- Useful framework: do A/C/E change as a function of measured ‘environmental’ variable?

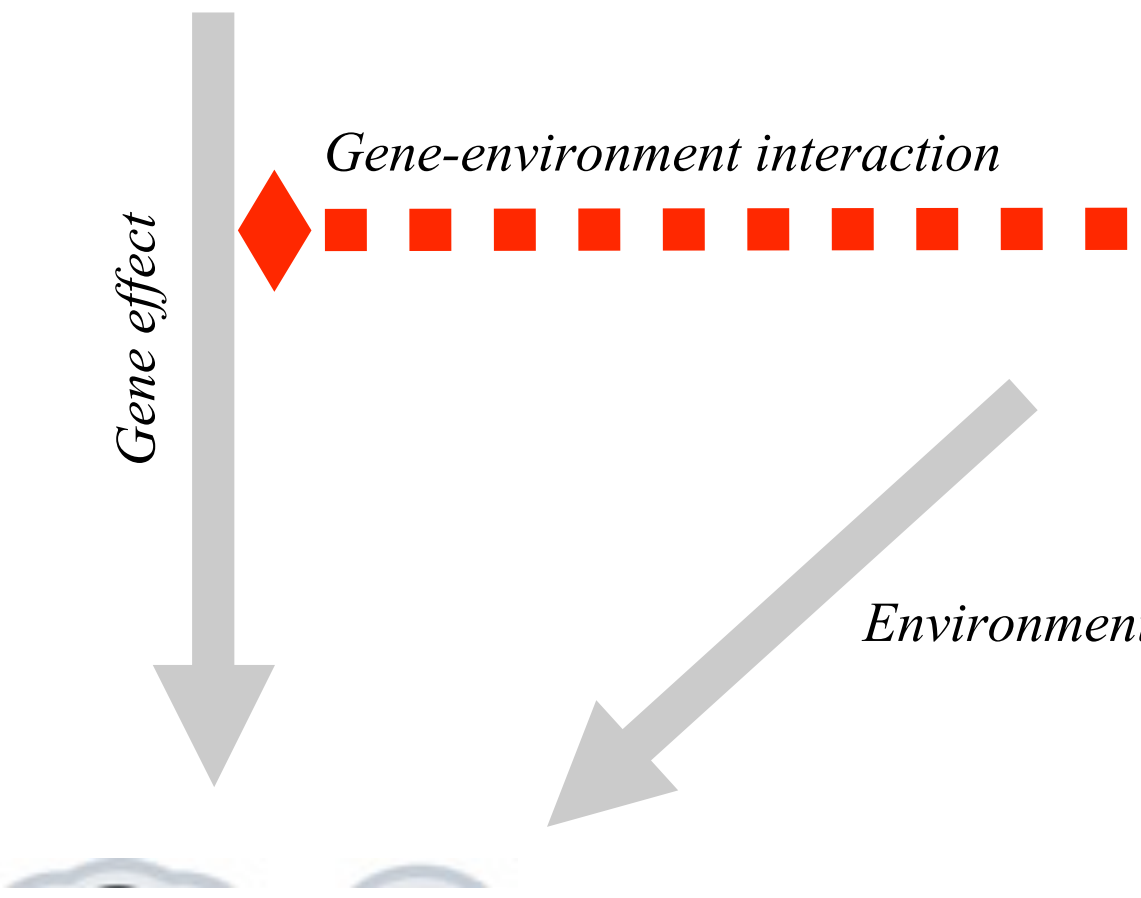
- Often regress out main effects of moderator on t

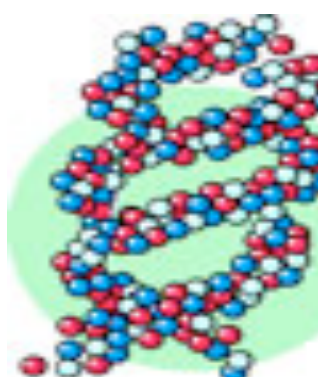
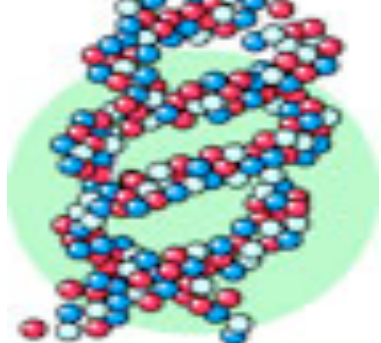


Gene-environment interaction

Gene effect

Environmental effect

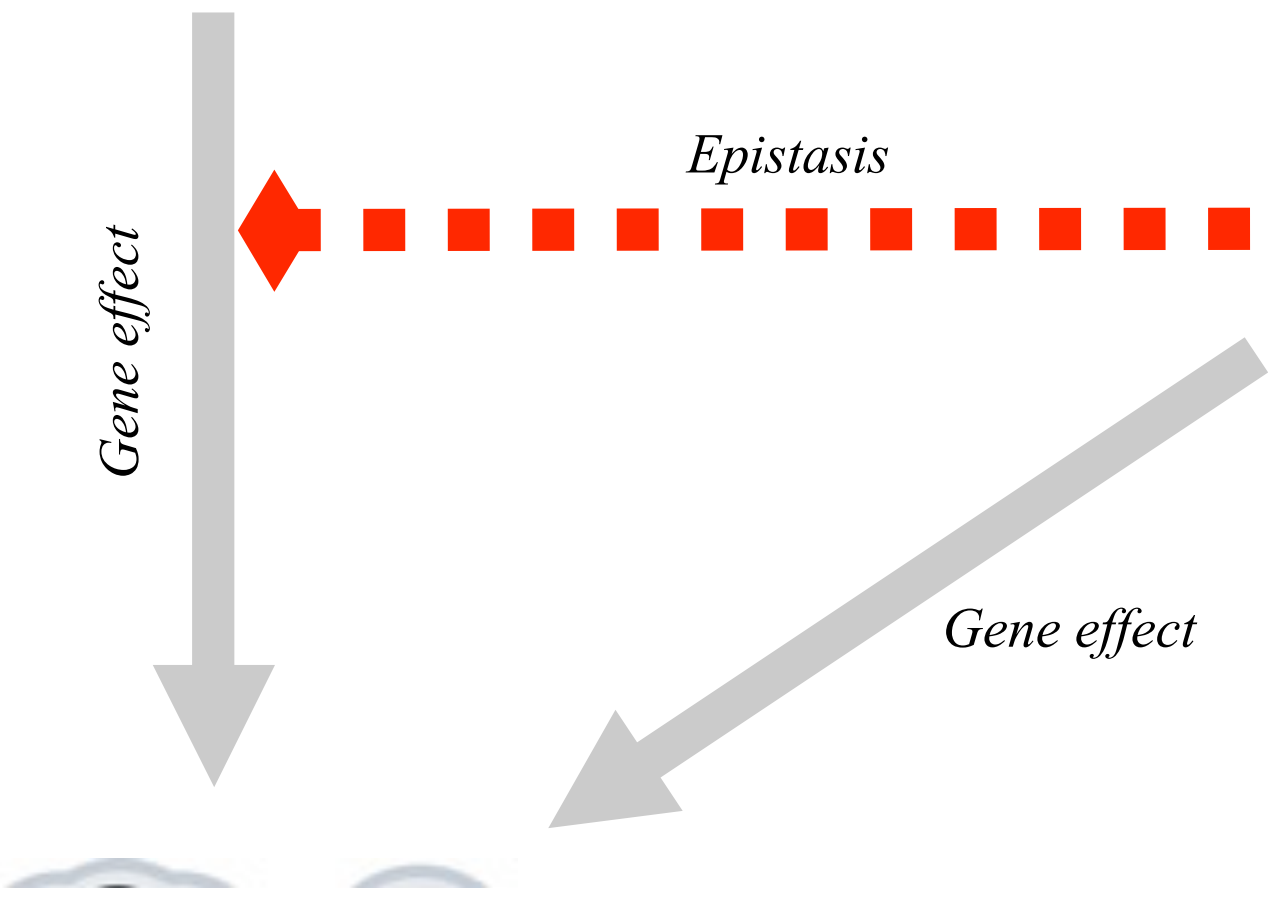




Gene effect

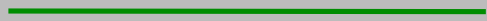
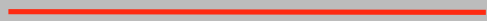
Epistasis

Gene effect



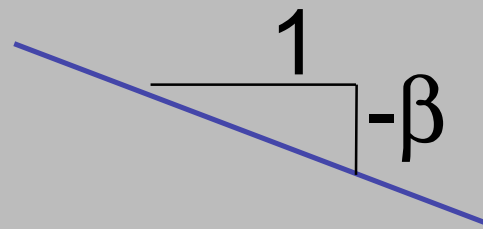
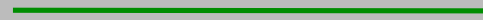
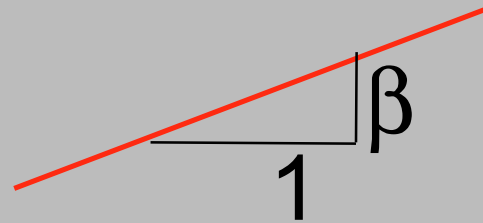
Biometrical G · E model

No interaction



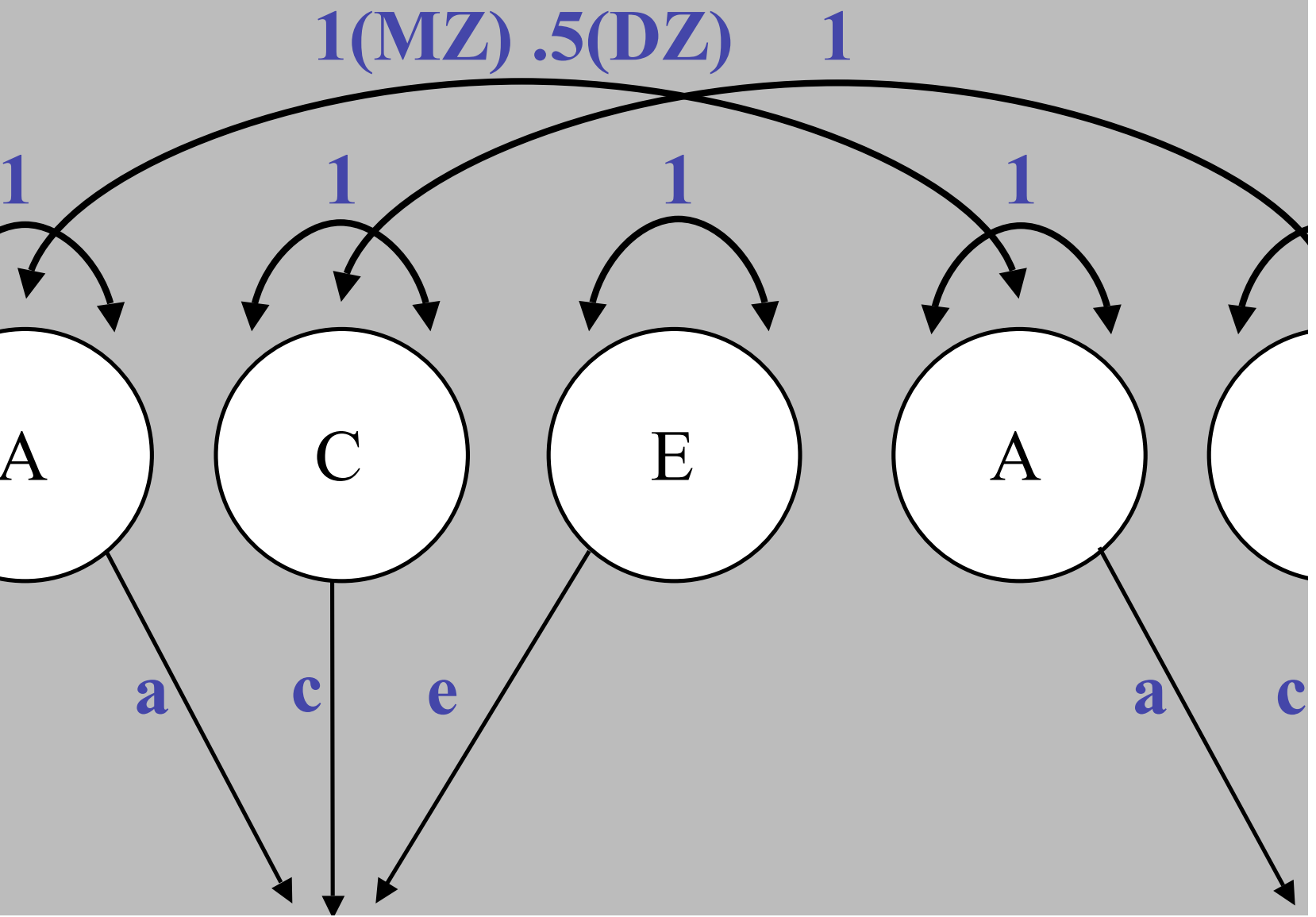
Environment

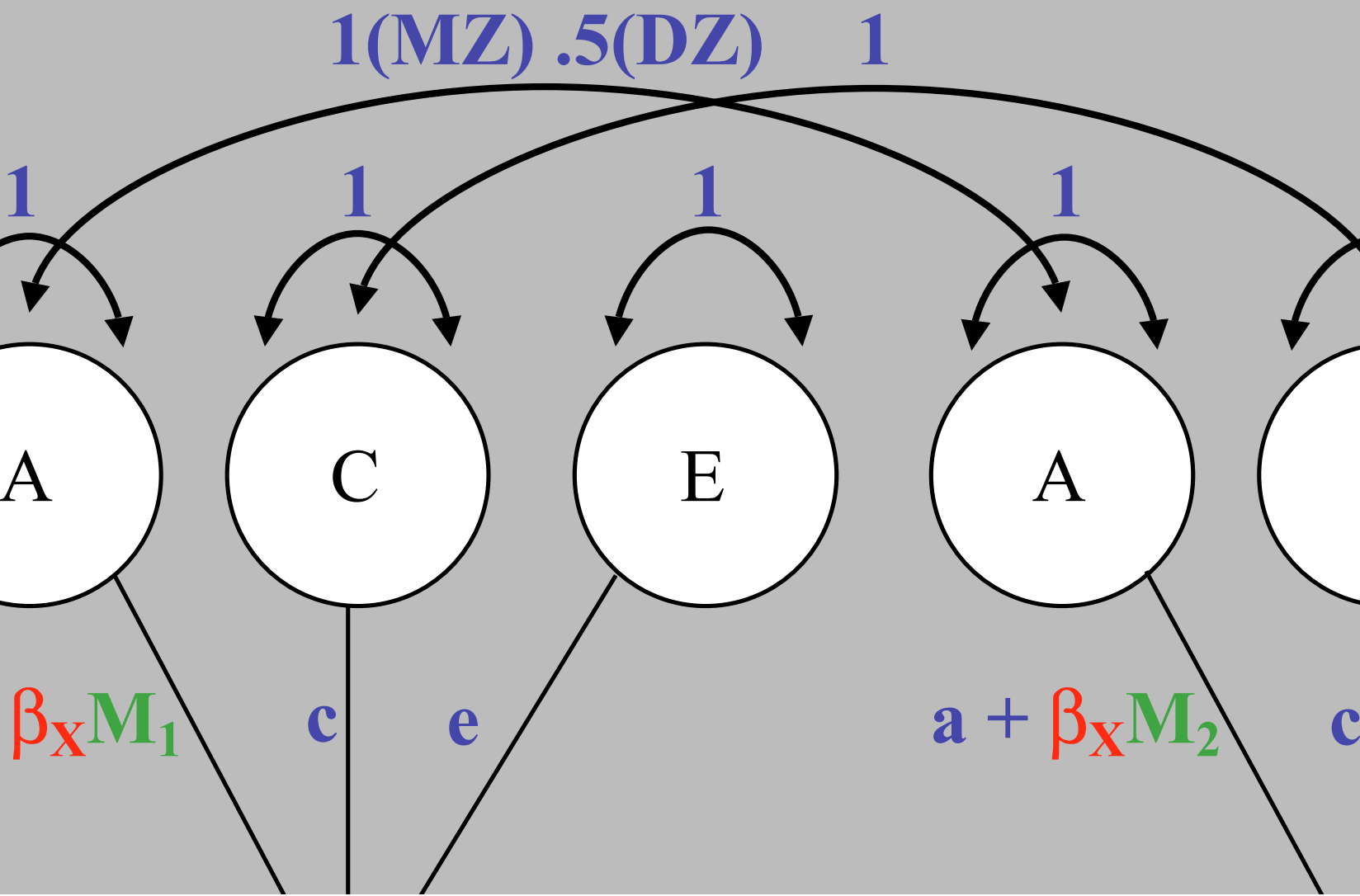
Interaction

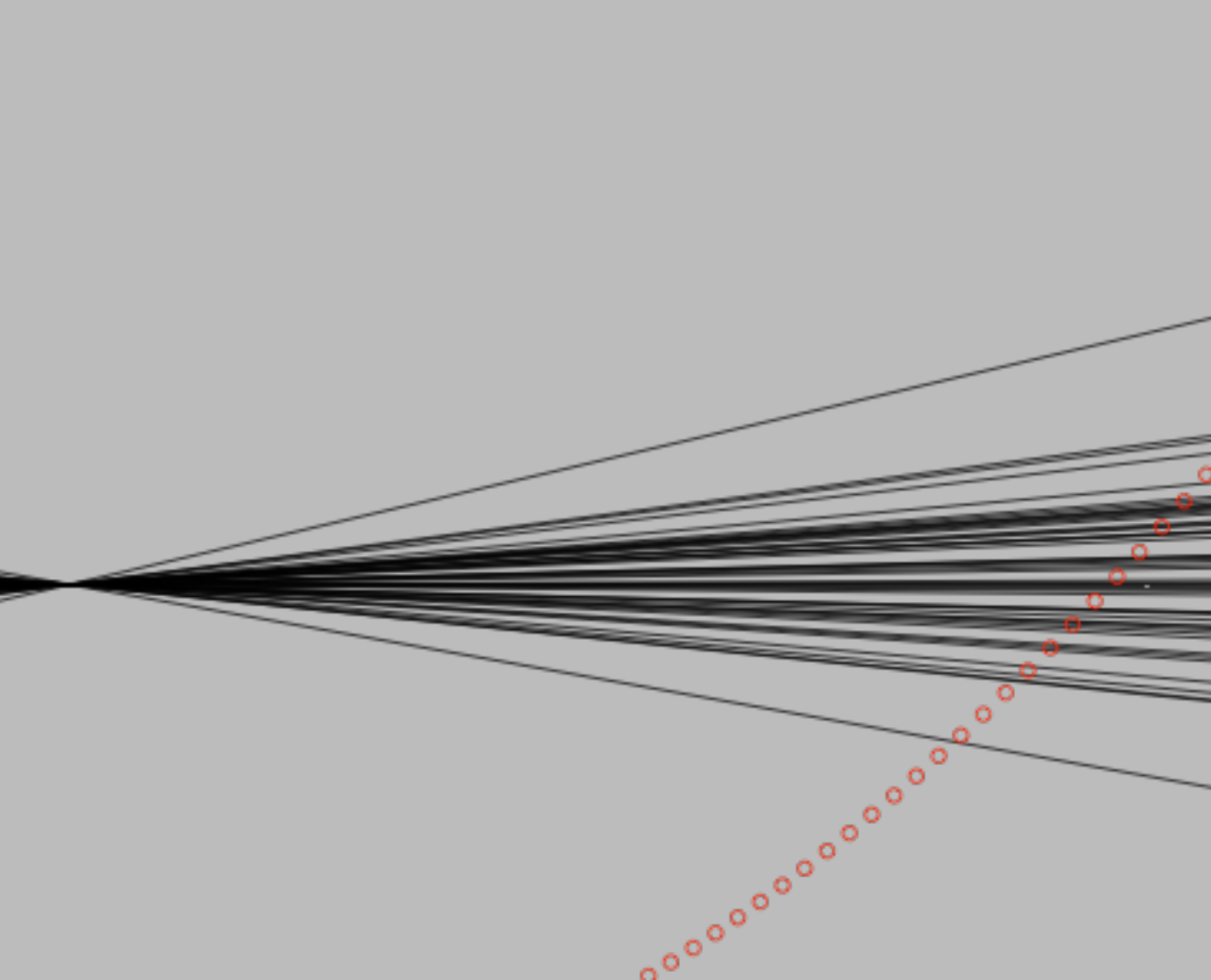


Environment

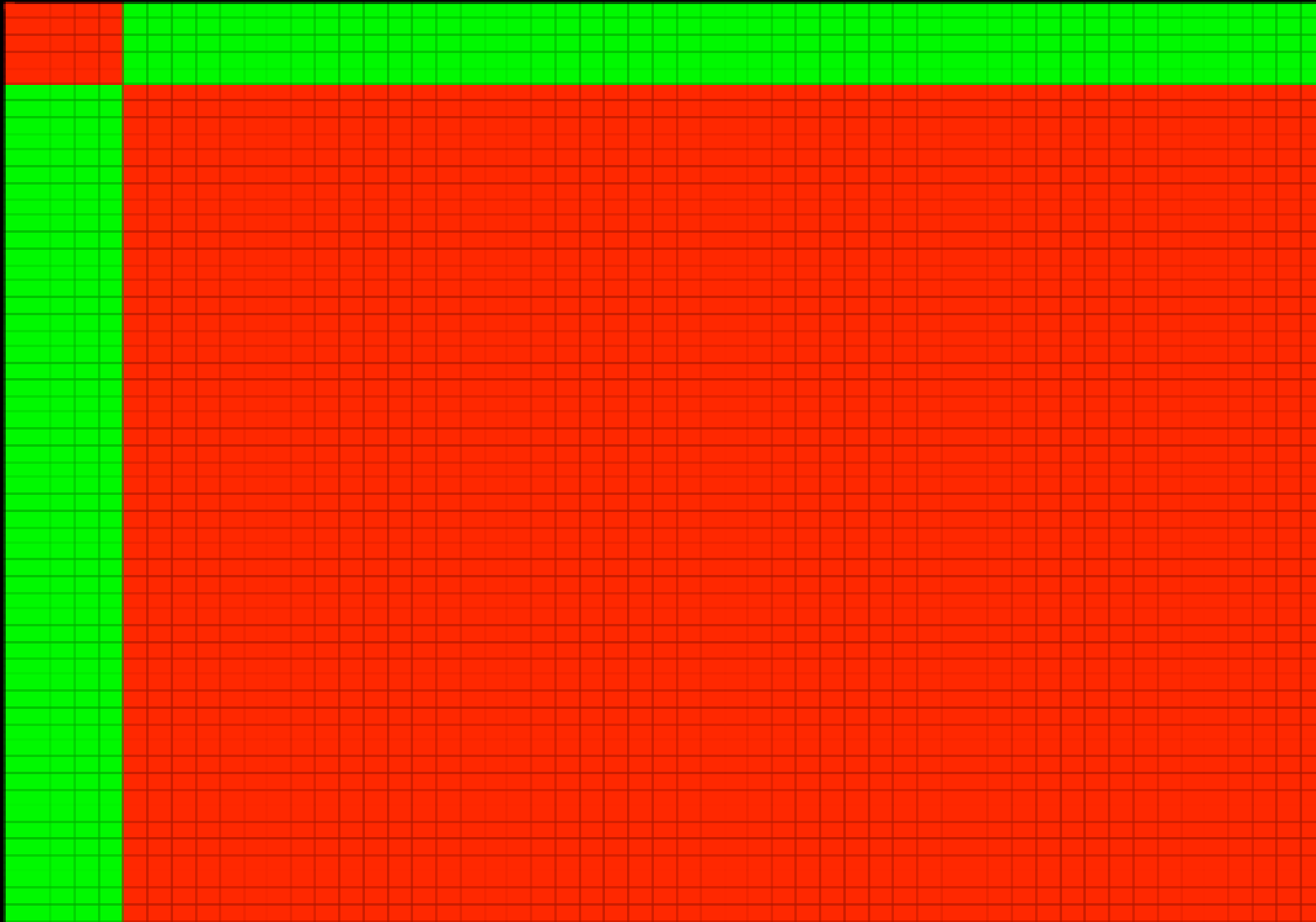
Standard ACE model for twin rese



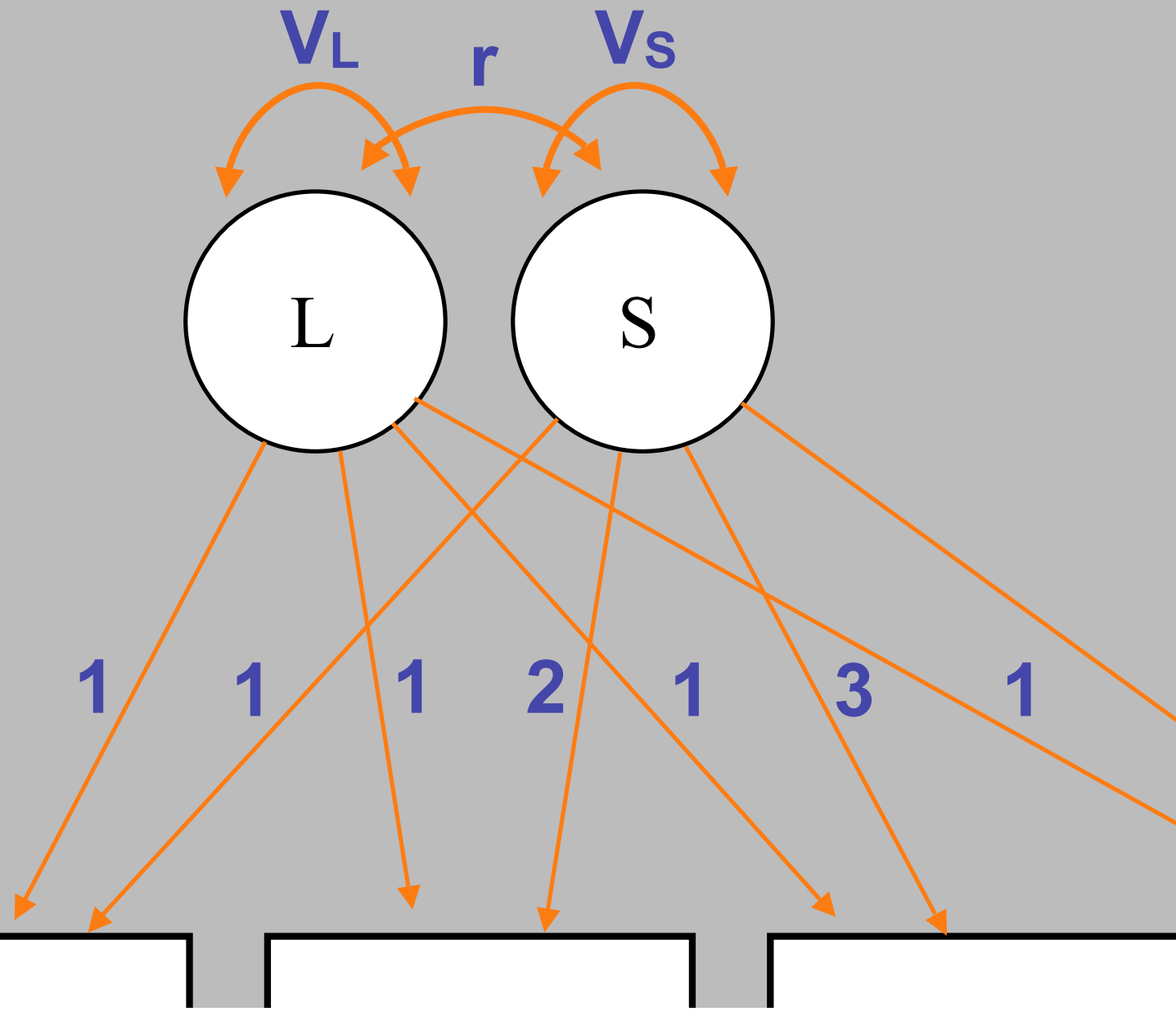




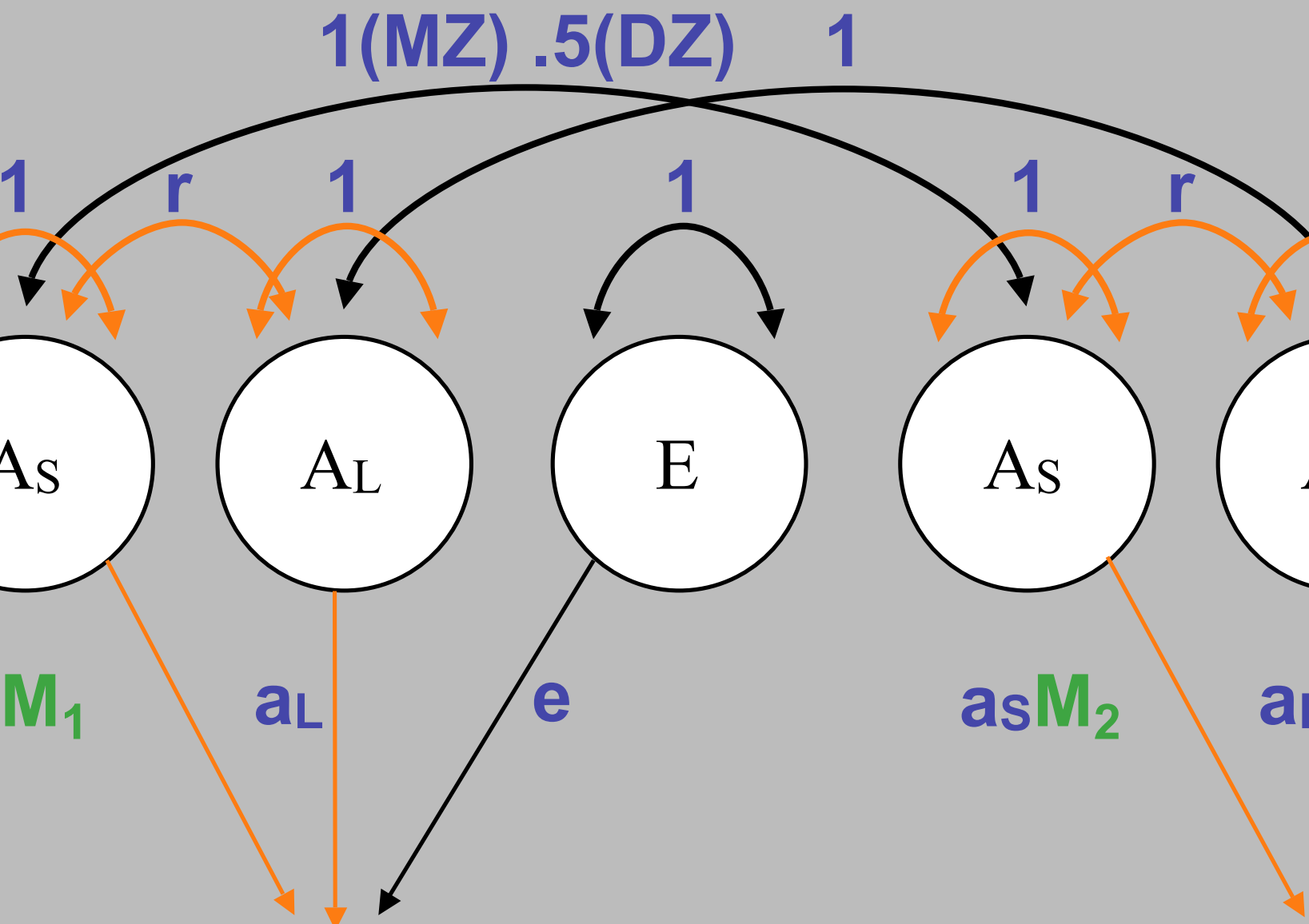
Single-factor model ($r=1$)

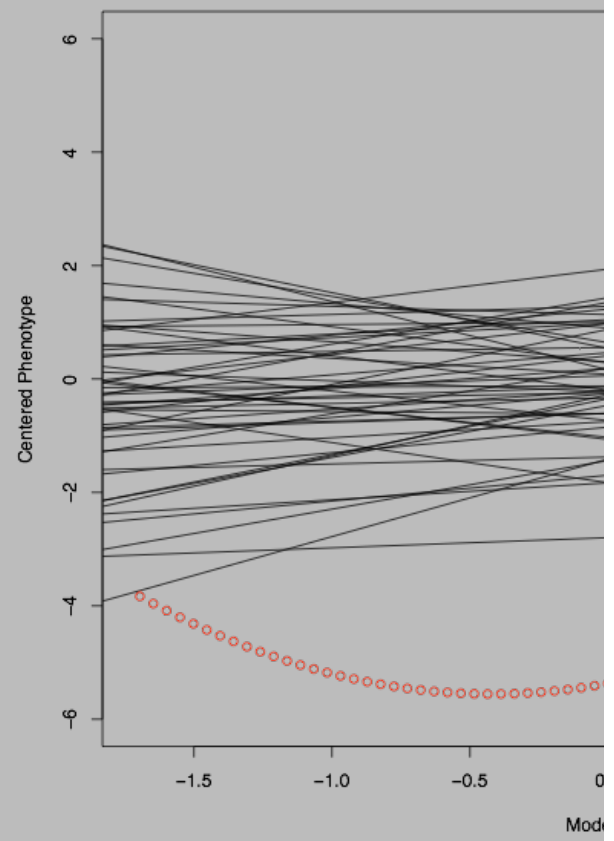
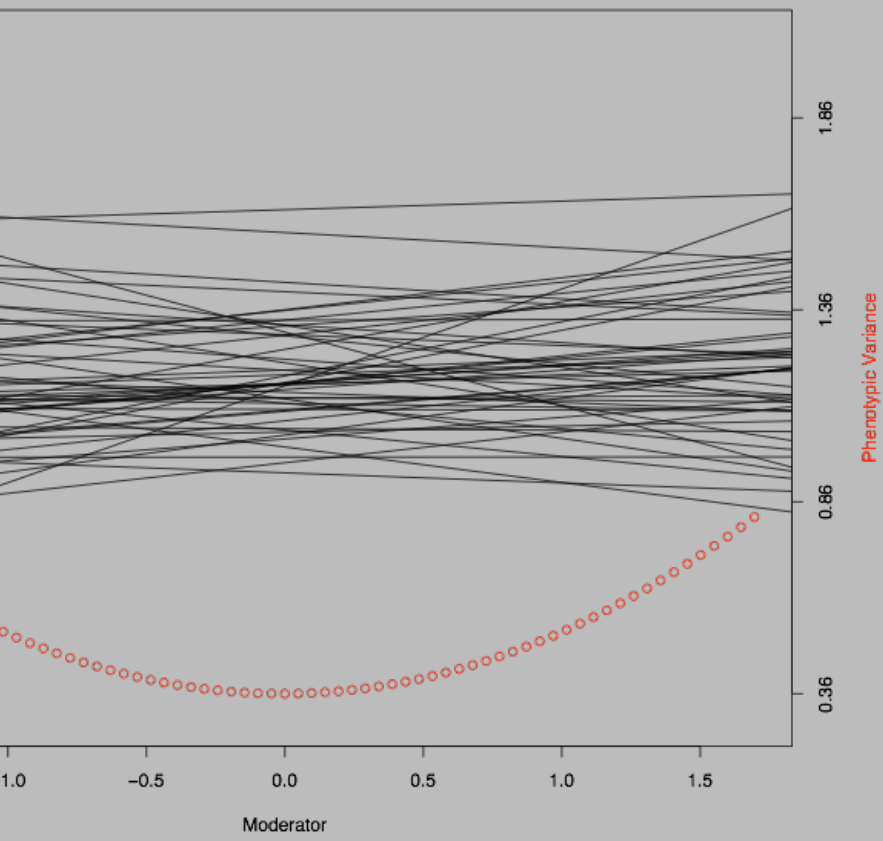


Growth Curve Model



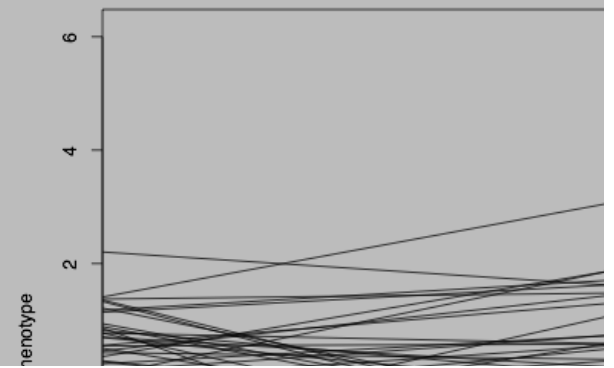
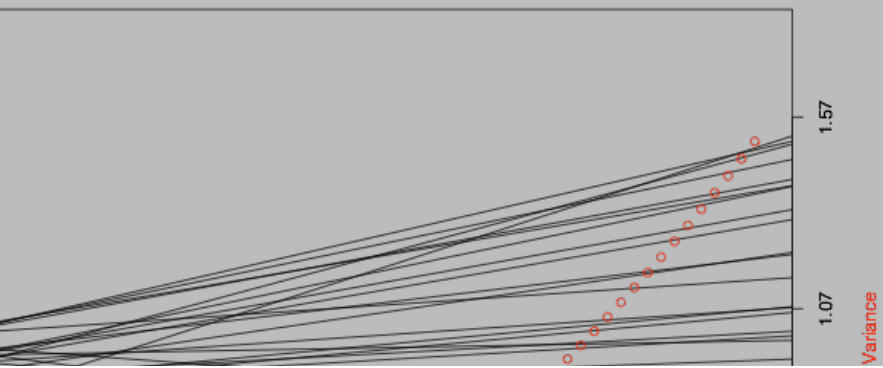
Enhanced Moderated AL



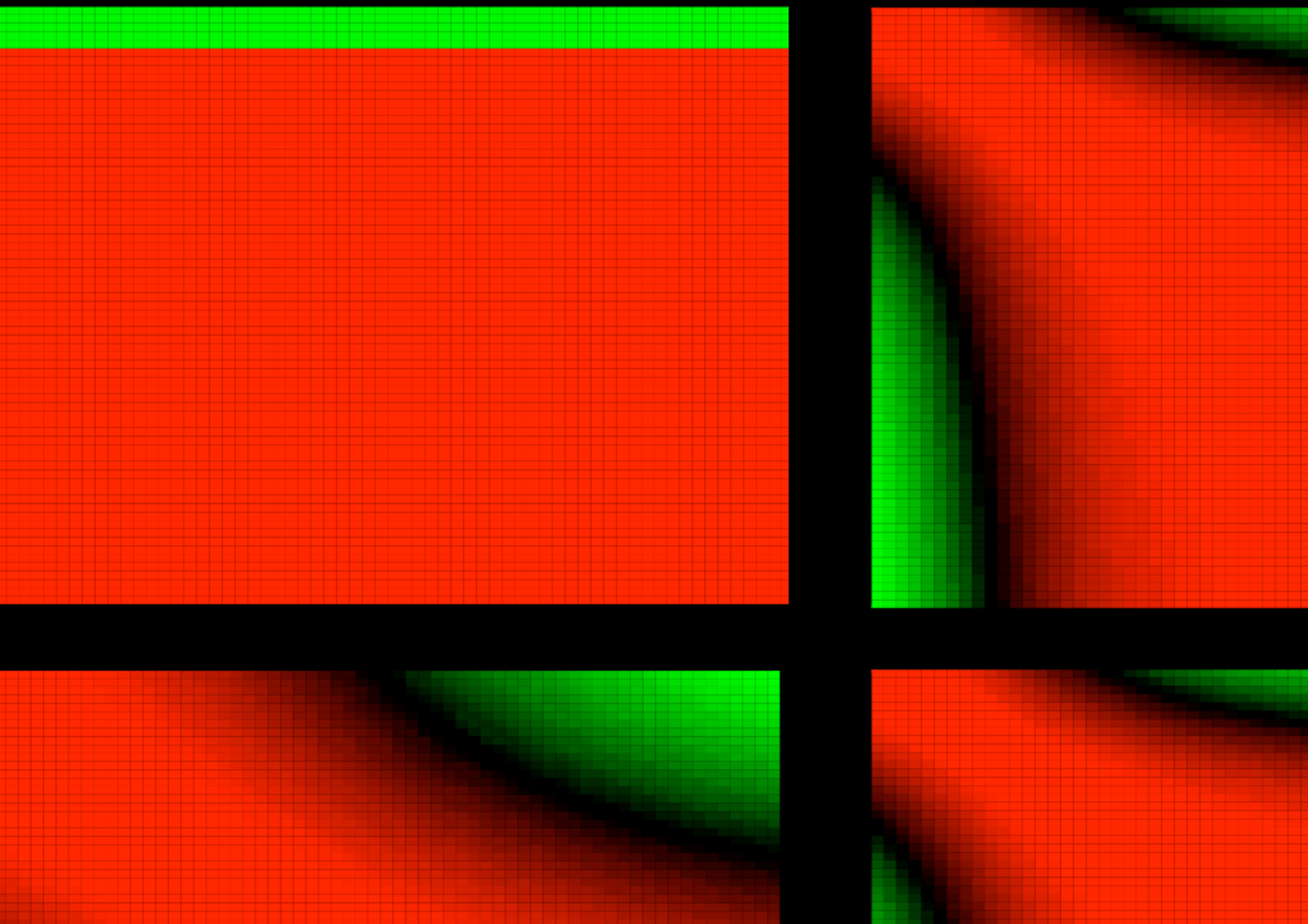


Enhanced Interactions given $r=.9$

Enhanced Interactions



$r=1.0$ $r=.9$ $r=.6$ $r=.3$



model: 1 Twin

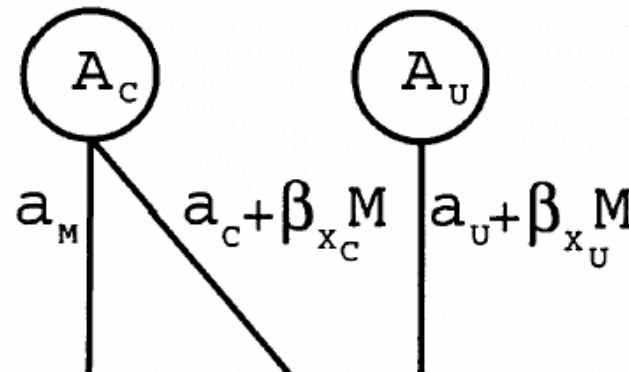
Variance Components Models for Gene–Environment Interaction in Twin Analysis

Shaun Purcell

Social, Genetic and Developmental Psychiatry Research Centre, Institute of Psychiatry, King's College, London, UK

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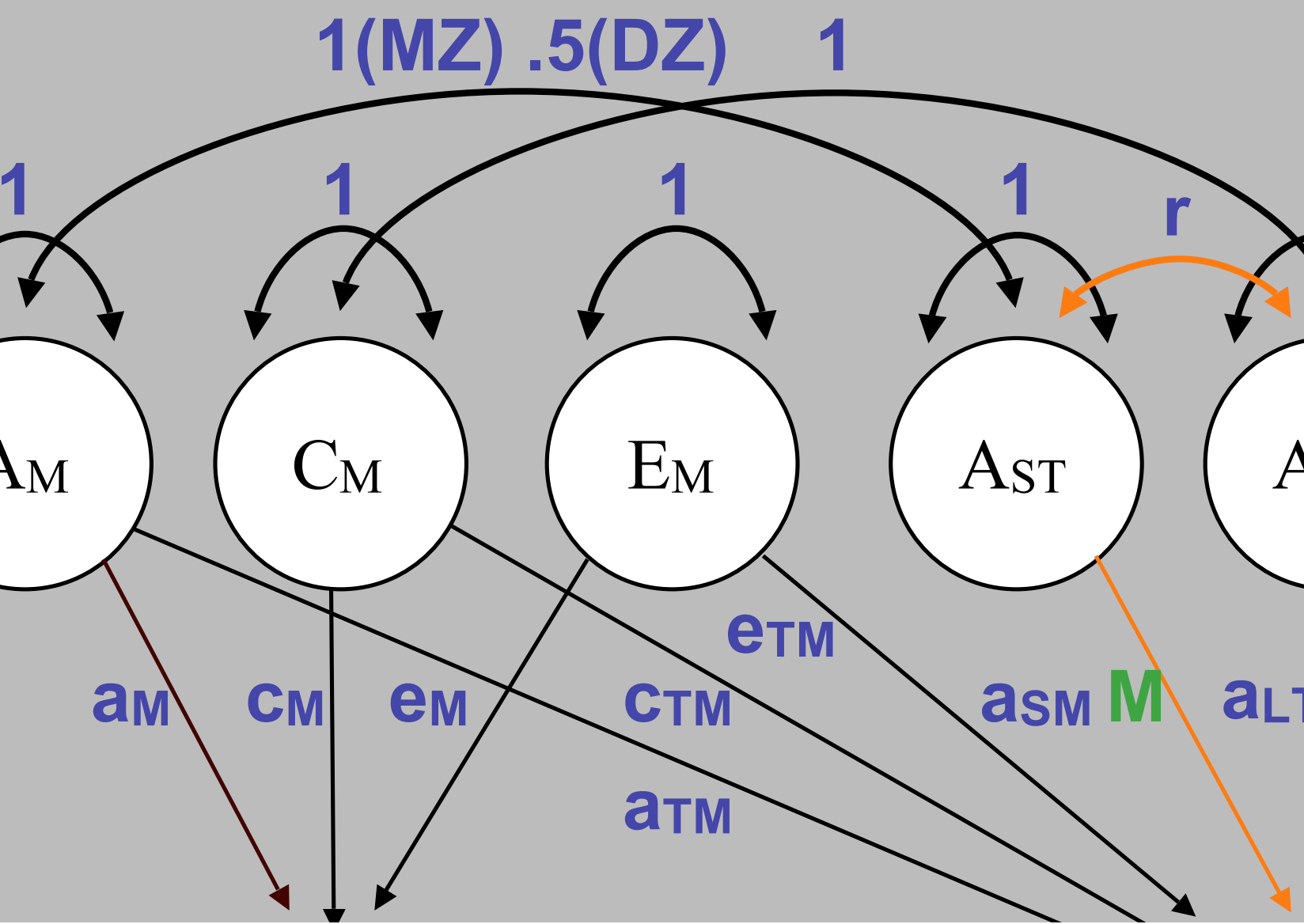
Twin Research Volume 5 Number 6 pp. 554-571



Perhaps
across
compo

Volume

Multivariate Moderated AL Model



Research Design Considerations

No variation in Age(M) at measurement

1. Estimation of parameters via mixture modeling (due to anything)

Variation in age, but twins measured once at same time

1. Know variance, MZ and DZ covariance @ different ages
2. Don't know if same genes/envt at different ages

Variation in age, twins measured once at different times

1. Know 2.1 plus MZ & DZ covariances as f(Age of measurement)
have pairs concordant & discordant wrt Age

Greg Carey Article

- Genotype-Environment Interaction and a Multivariate Solution
 - “Please do not cite until I’m certain the whole thing is right.”
- Definition variables
- Conditional Distributions

Necessary background

- “For example, if the ACE model in a general population assumes that A, C, and E are uncorrelated, then A, C, and E in a poor environmental group will be uncorrelated when home environment is not correlated with ASB”
- Conditional distributions

Distribution of Disruptive Genes

Pearson Aitken Selection

Let \mathbf{z} be a set of random variables, \mathbf{z} , partitioned such that

$$\mathbf{z} = \begin{pmatrix} \mathbf{x} \\ \mathbf{y} \end{pmatrix}.$$

Assume that the relationship among all variables is linear

Let the mean vector of the variables be

$$\boldsymbol{\mu} = \begin{pmatrix} \mu_x \\ \mu_y \end{pmatrix},$$

Pearson Aitken Selection

that selection changes mean vector μ_x to $\tilde{\mu}_x$. Then the
values after selection will equal

$$\tilde{\mu}_y = \mu_y + C_{yx} V_x^{-1} (\tilde{\mu}_x - \mu_x).$$

selection process changes the covariance matrix among the
variables. The covariance matrix will change from V to

$$\tilde{V} = \begin{pmatrix} \tilde{V}_x & \tilde{V}_x V_x^{-1} C_{xy} \\ C_{yx} V_x^{-1} \tilde{V}_x & V_y - C_{yx} (V_x^{-1} - V_x^{-1} \tilde{V}_x V_x^{-1}) C_{xy} \end{pmatrix}$$

Example item response probability curves

Example item response probability curves

