

Complex Trait Genetics in Animal Models

Will Valdar
Oxford University

Mapping Genes for Quantitative Traits in Outbred Mice

Will Valdar
Oxford University

What's so great about mice?

Share ~99% of genes with humans

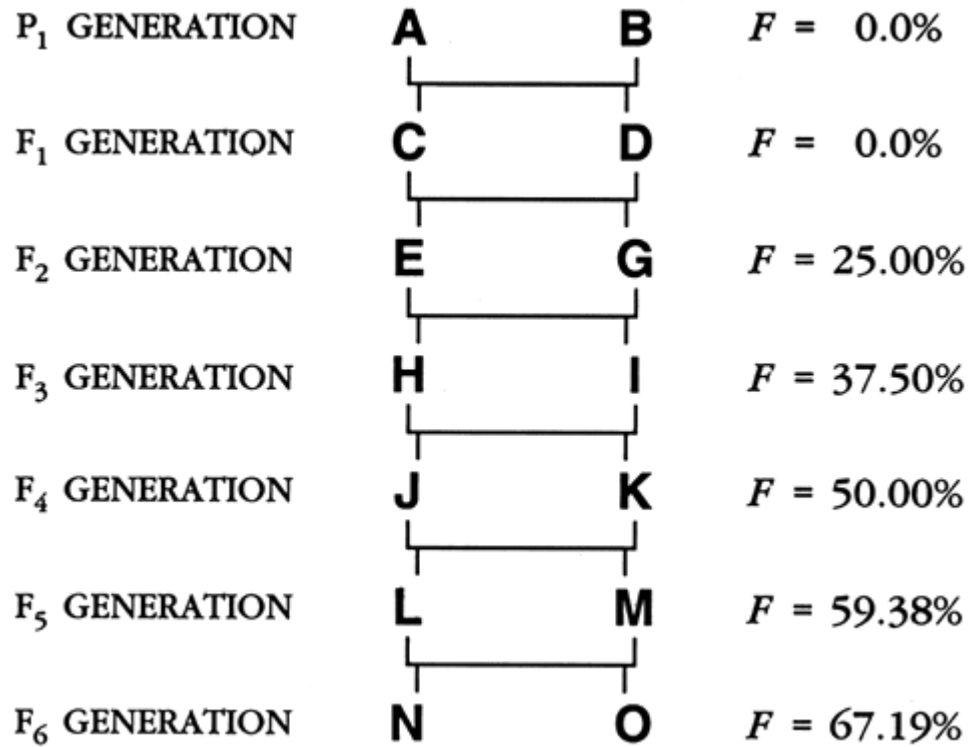
~90% of the two genomes can be portioned into regions of conserved synteny

Shorter lifespans

You can do invasive experiments

You can breed them as you like – control the genetics

What is an inbred strain?



F₂₀ generation

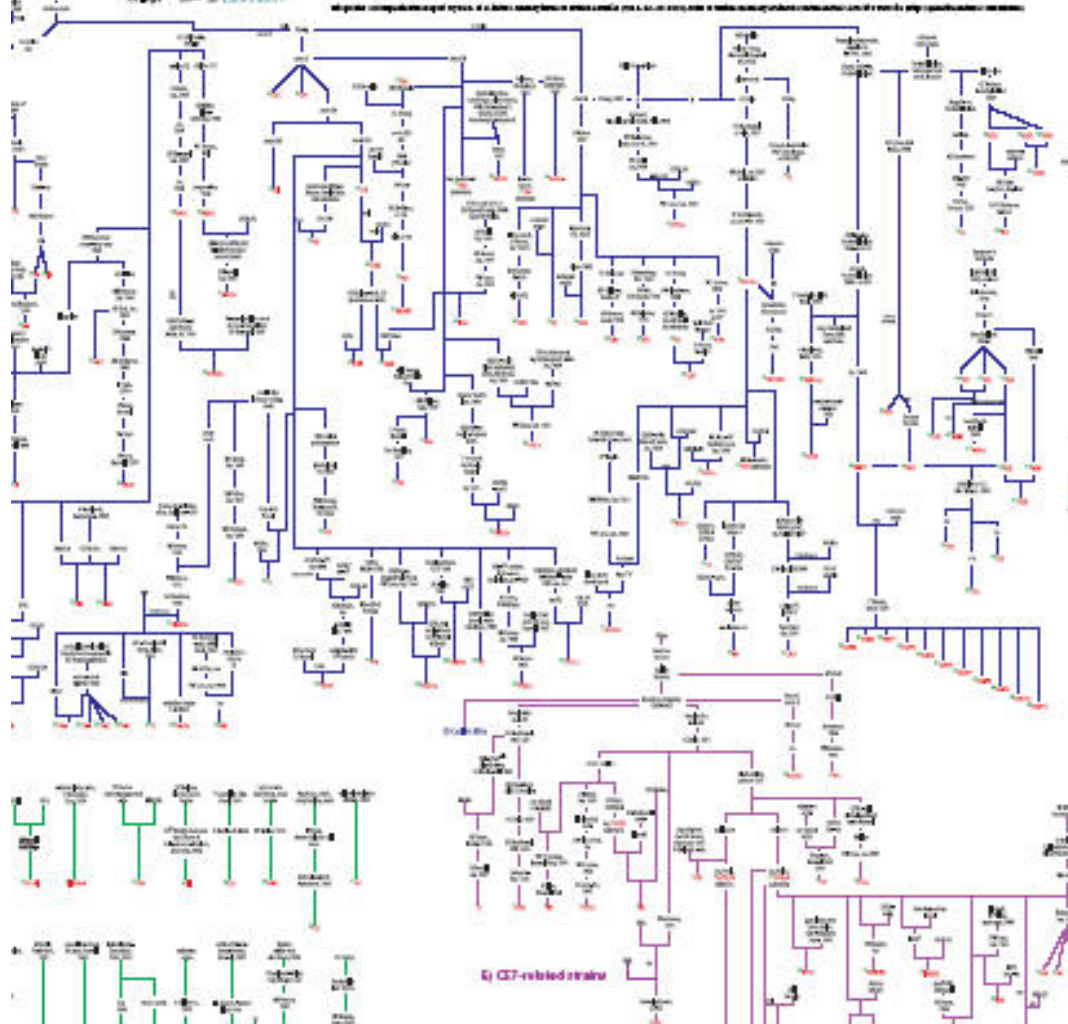
$F = 99\%$



BALB/c

Genealogies of mouse inbred strains

Beck, J.A., Lloyd, S., Halegarath, M., Lennen-Peters, M., Eppig, J.T., Festing, M.F.W. & Fisher, E.M.C.

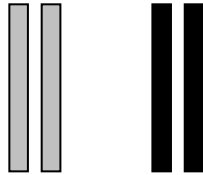


<http://www.informatics.jax.org/mgihome/genealogy/>

one inbred strain



two inbred strains



Mouse model of anxiety

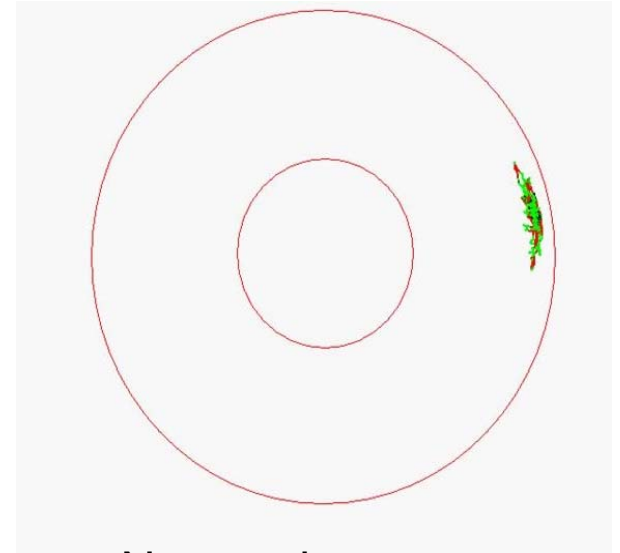
OPEN FIELD ARENA



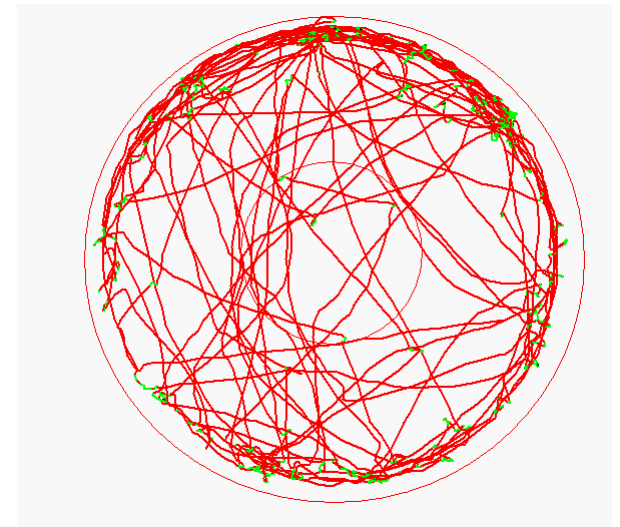
Mouse model of anxiety



Anxious mouse

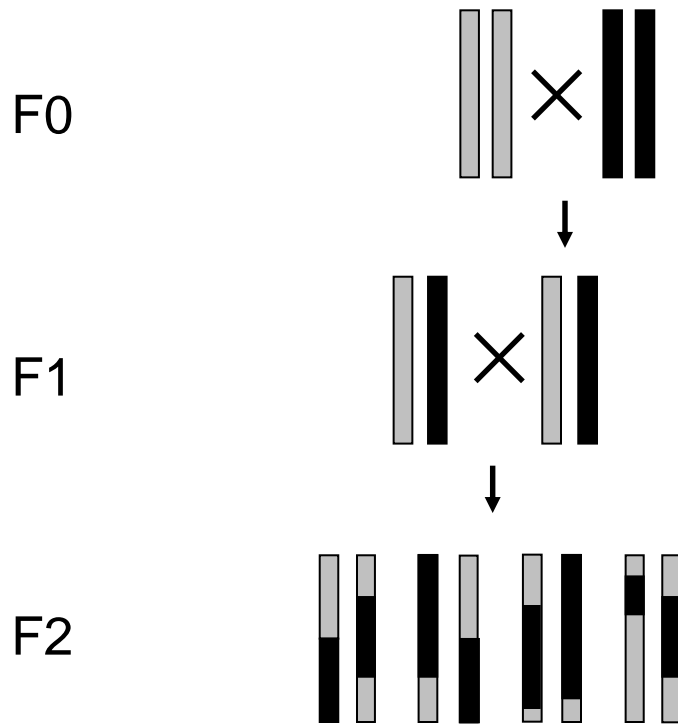


Non anxious mouse

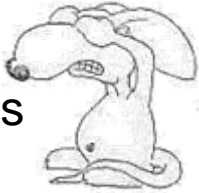


F2 cross

Generation



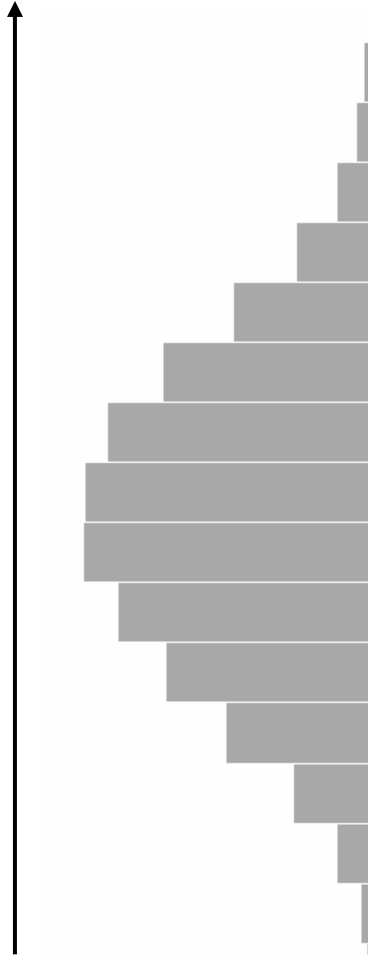
anxious



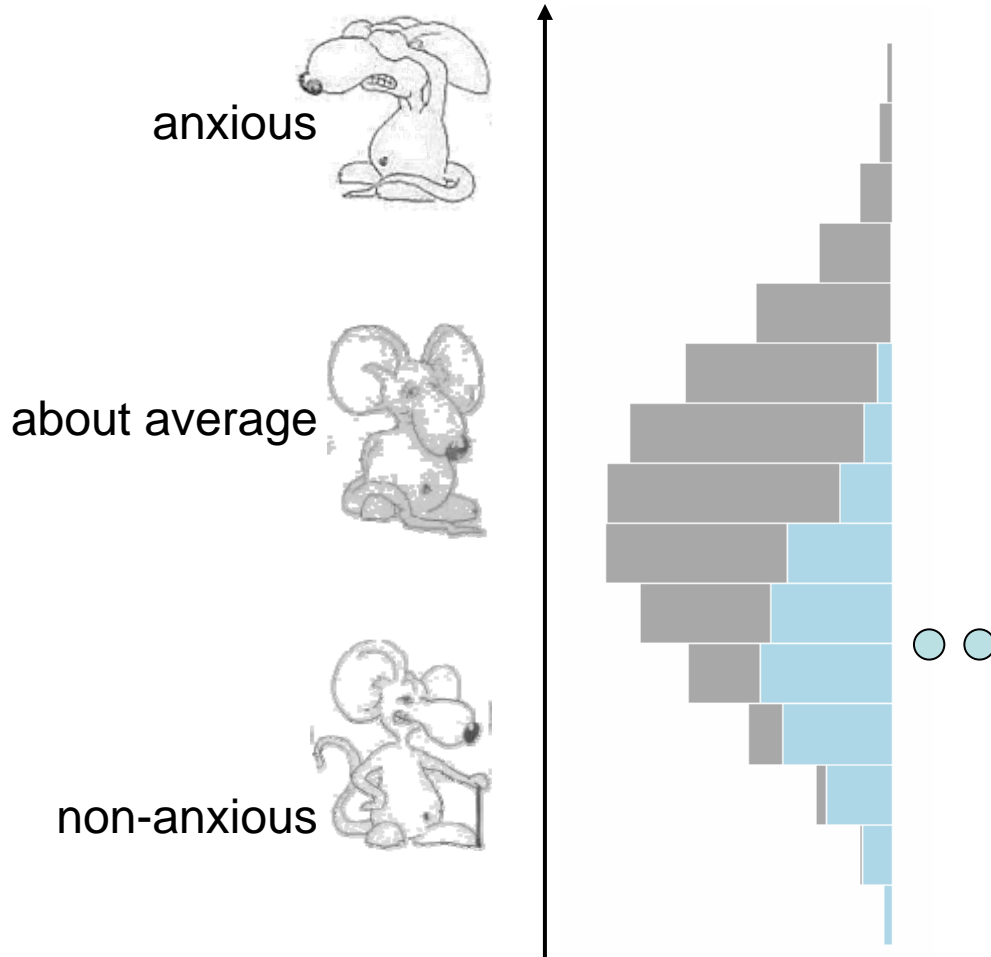
about average



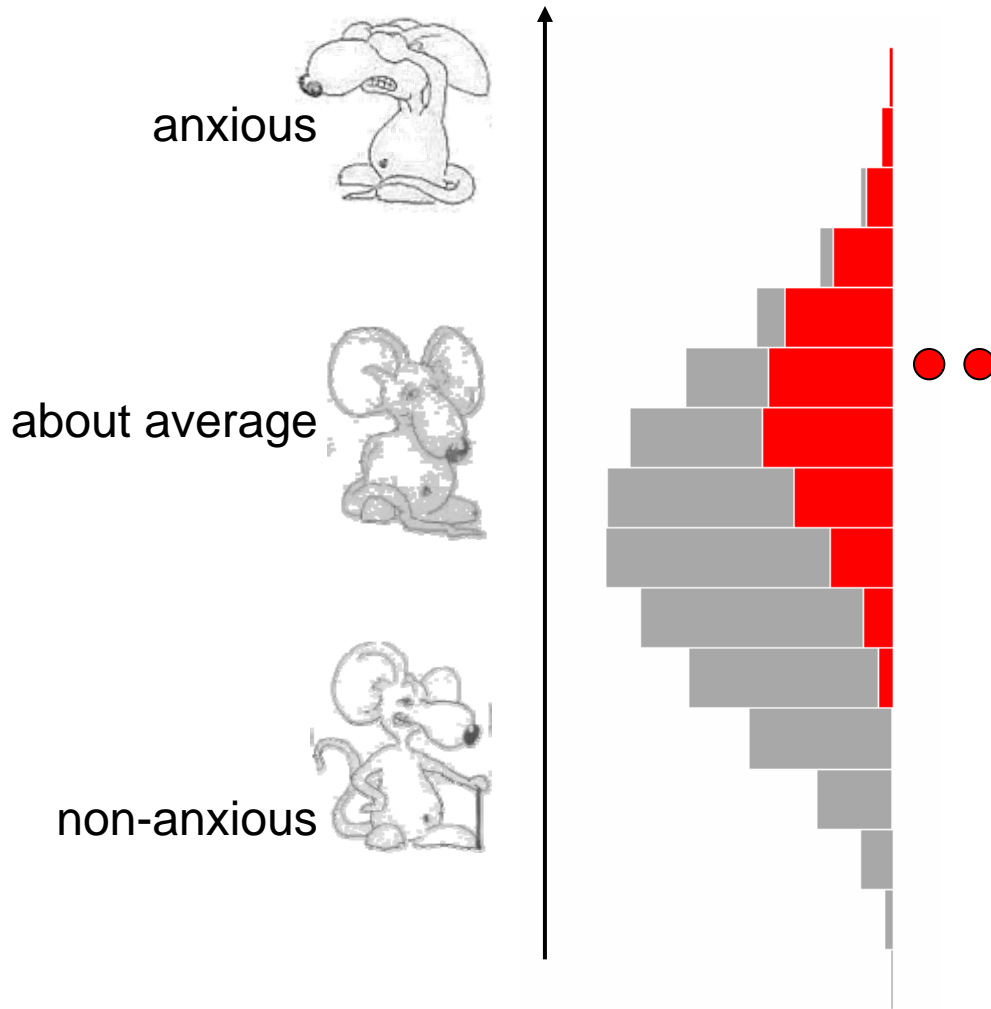
non-anxious



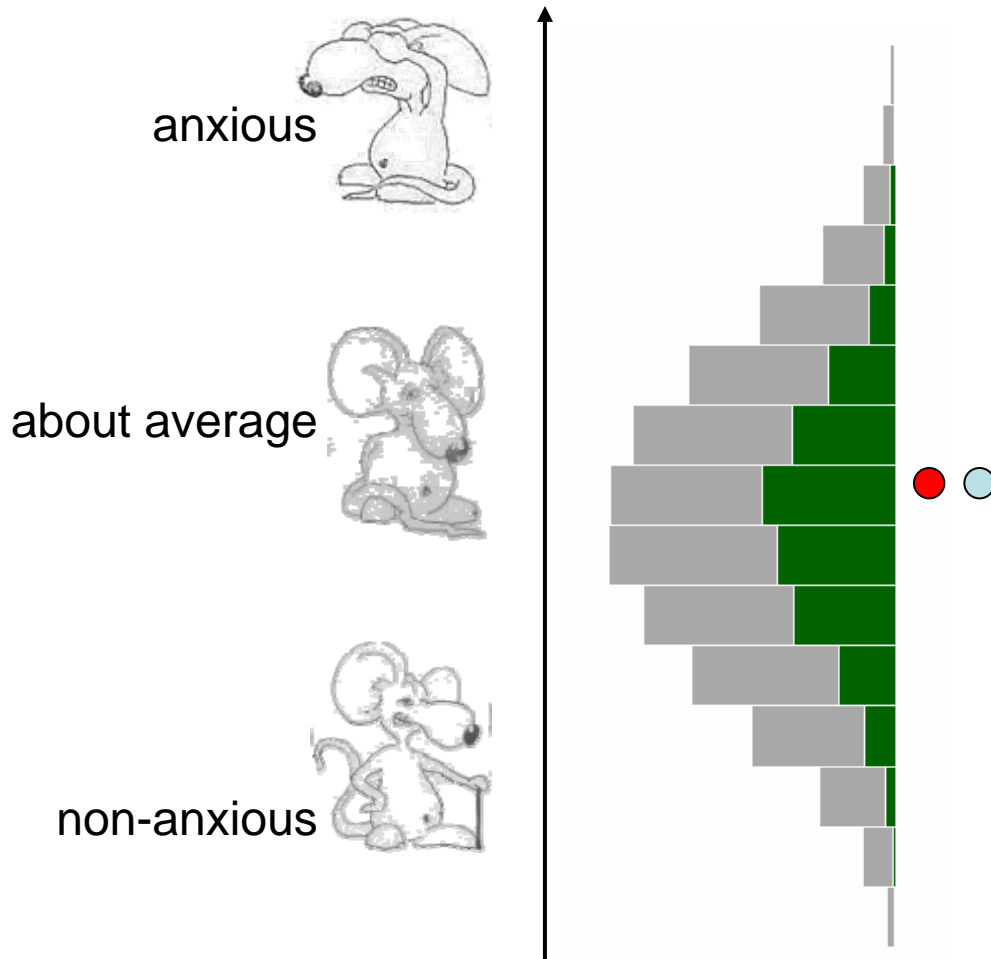
Quantitative Trait Locus



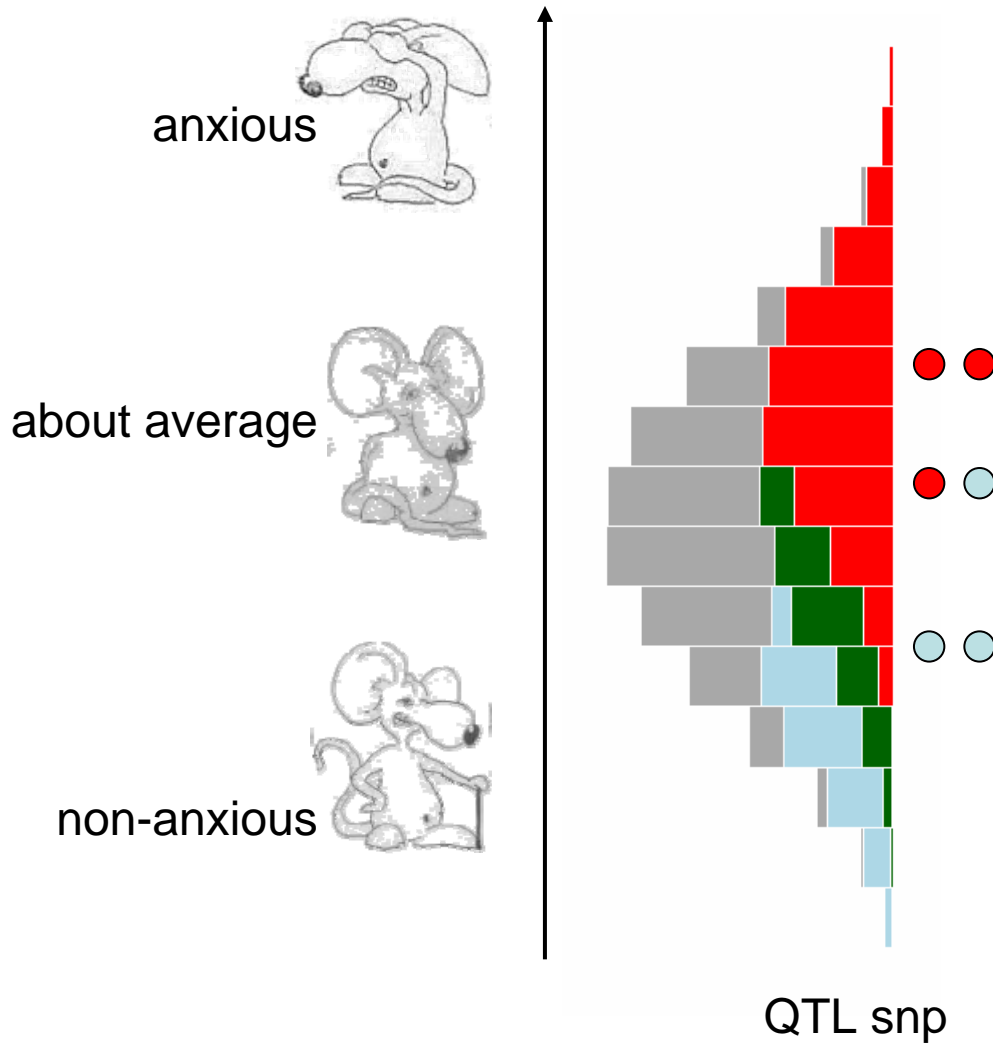
Quantitative Trait Locus



Quantitative Trait Locus



Quantitative Trait Locus



Linear models

Also known as

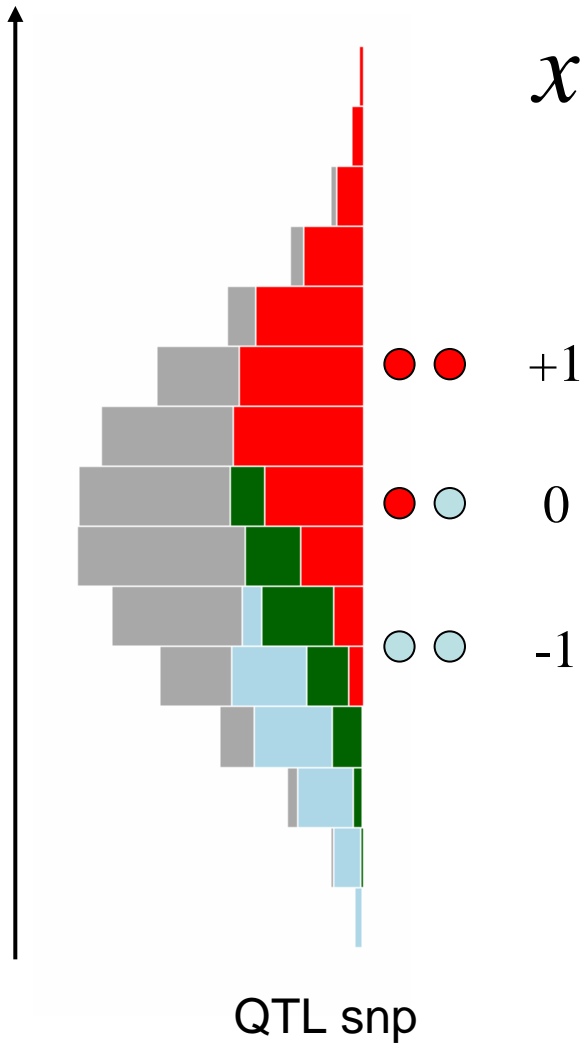
ANOVA

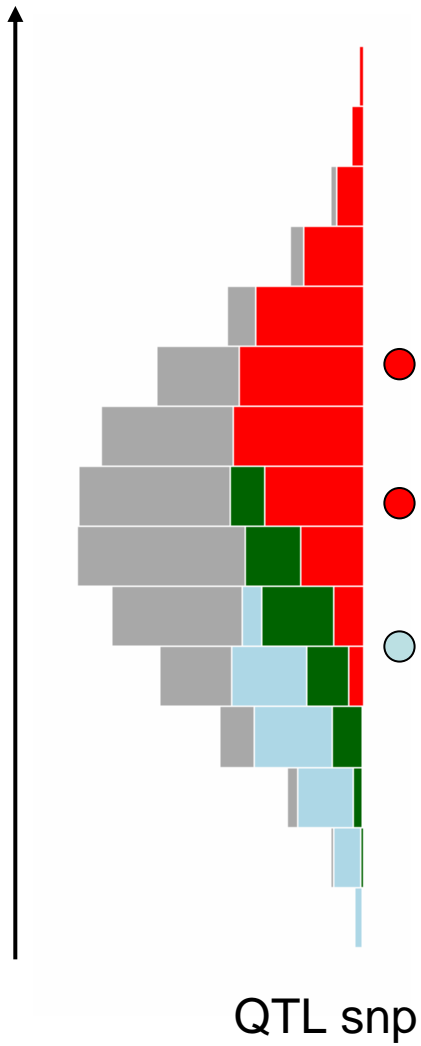
ANCOVA

regression

multiple regression

linear regression





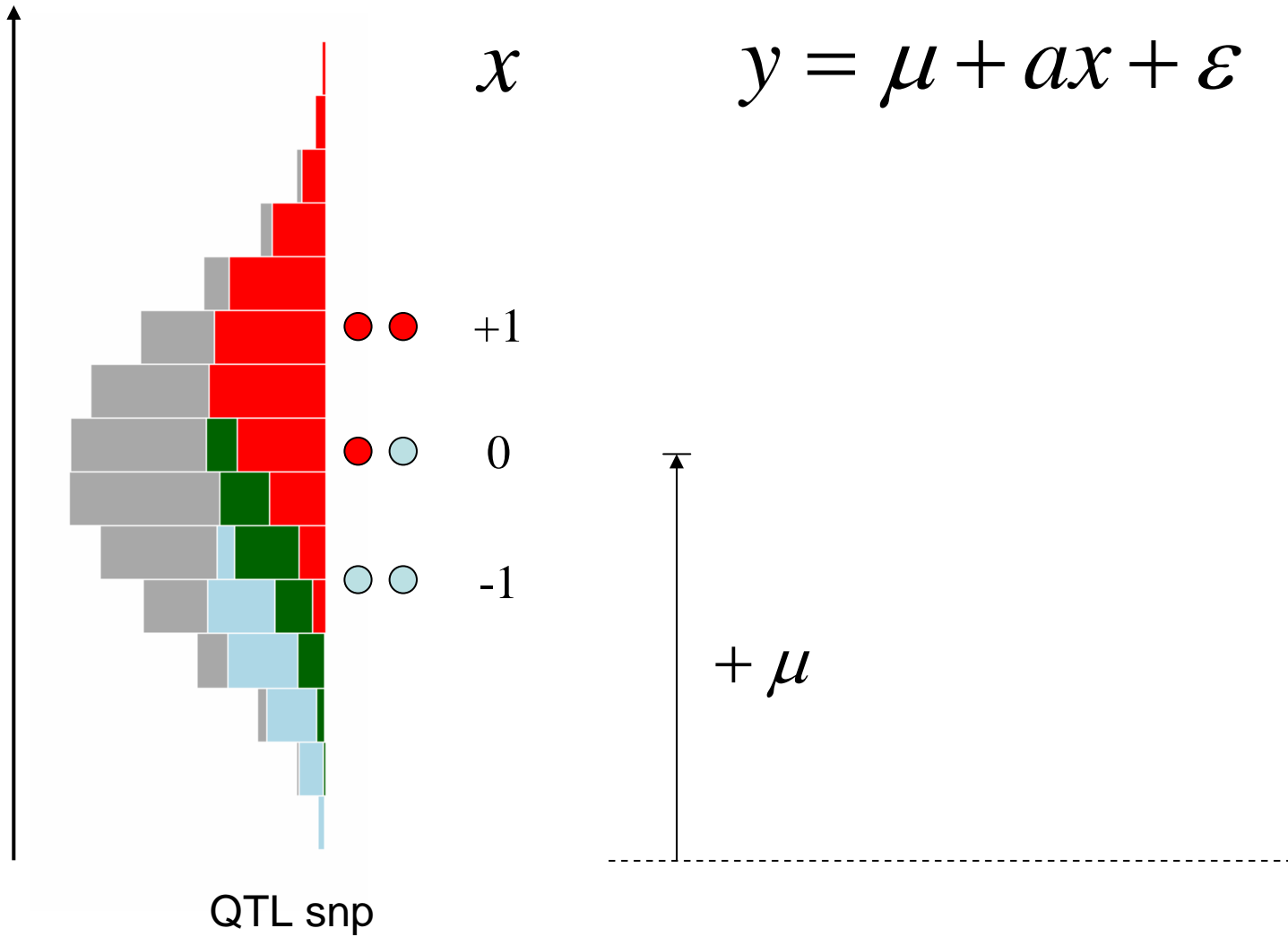
x

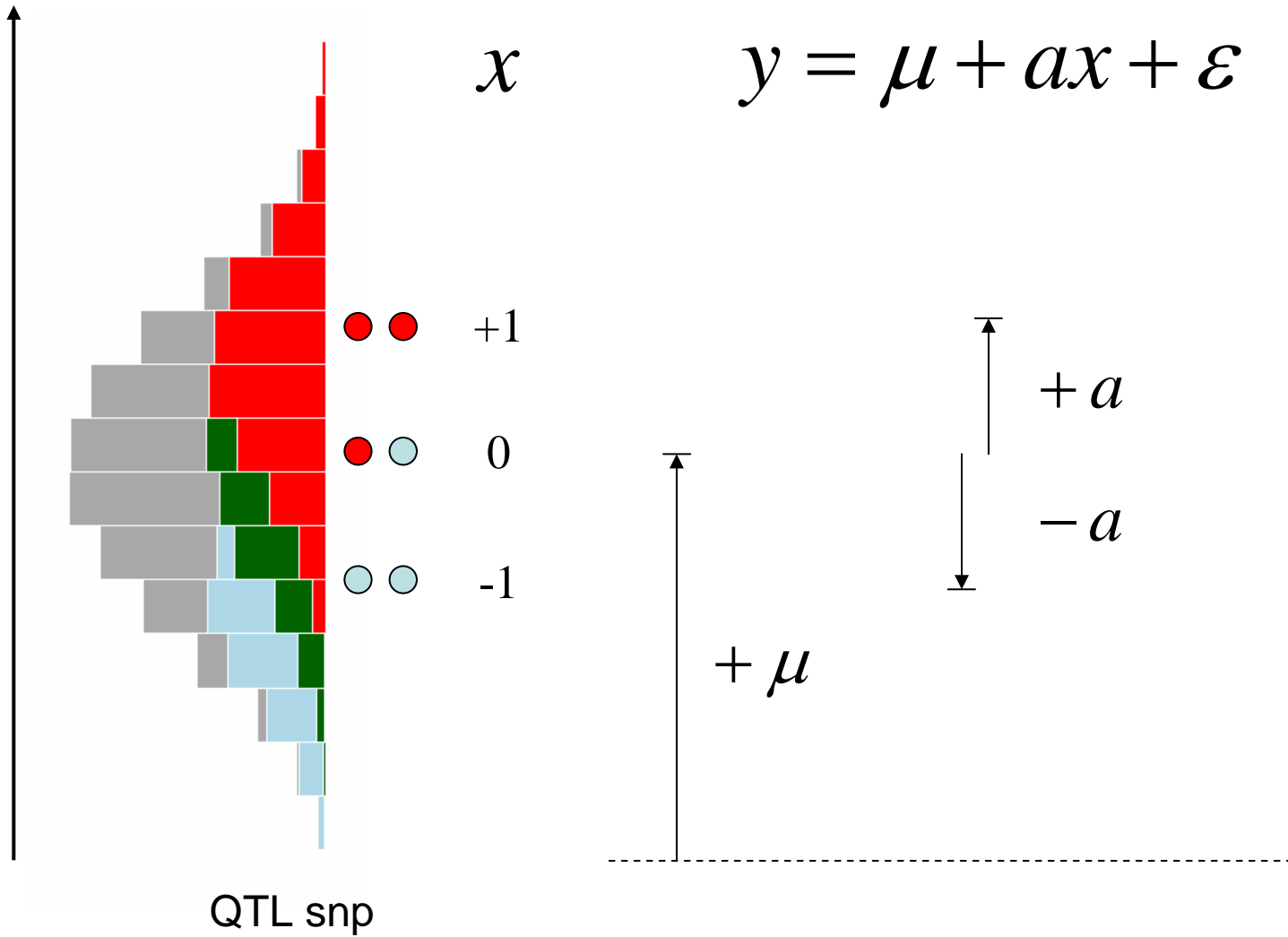
$$y = \mu + ax + \varepsilon$$

● ● +1

● ○ 0

○ ○ -1





Hypothesis testing

$$H_0: y = \mu + \varepsilon$$

$$H_1: y = \mu + ax + \varepsilon$$

Hypothesis testing

$$H_0: y \sim 1$$

$$y = \mu + \varepsilon$$

$$H_1: y \sim 1 + \mathbf{x}$$

$$y = \mu + ax + \varepsilon$$

Hypothesis testing

$$H_0: y \sim 1$$

$$y = \mu + \varepsilon$$

$$H_1: y \sim 1 + \mathbf{x}$$

$$y = \mu + ax + \varepsilon$$

H_1 vs H_0 : Does \mathbf{x} explain a significant amount of the variation?

Hypothesis testing

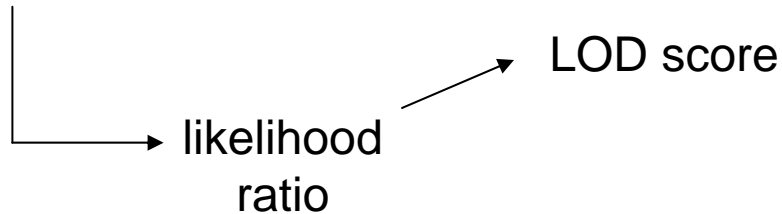
$$H_0: y \sim 1$$

$$y = \mu + \varepsilon$$

$$H_1: y \sim 1 + \mathbf{x}$$

$$y = \mu + ax + \varepsilon$$

H_1 vs H_0 : Does \mathbf{x} explain a significant amount of the variation?



Hypothesis testing

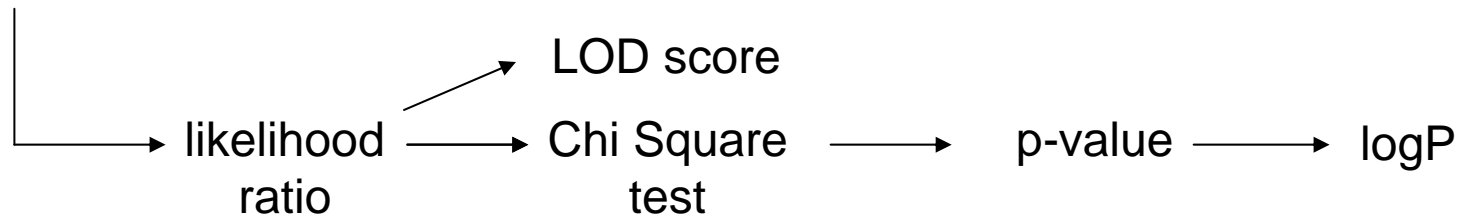
$$H_0: y \sim 1$$

$$y = \mu + \varepsilon$$

$$H_1: y \sim 1 + \mathbf{x}$$

$$y = \mu + ax + \varepsilon$$

H_1 vs H_0 : Does \mathbf{x} explain a significant amount of the variation?



Hypothesis testing

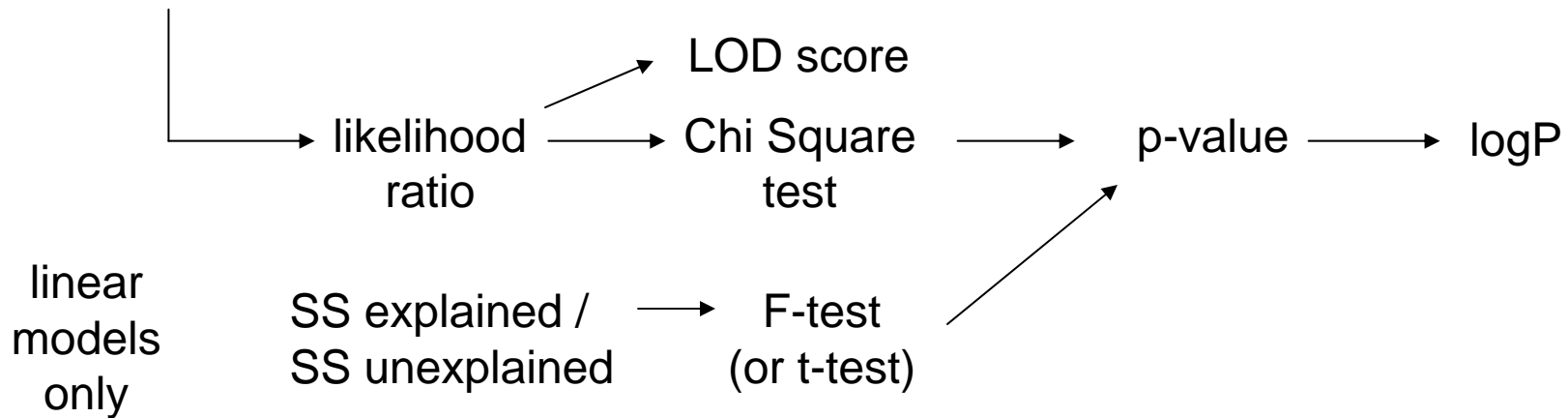
$$H_0: y \sim 1$$

$$y = \mu + \varepsilon$$

$$H_1: y \sim 1 + \mathbf{x}$$

$$y = \mu + ax + \varepsilon$$

H_1 vs H_0 : Does \mathbf{x} explain a significant amount of the variation?



Hypothesis testing

$$H_0: y \sim 1 + x_1$$

$$y = \mu + a_1 x_1 + \varepsilon$$

$$H_1: y \sim 1 + x_1 + \mathbf{x_2}$$

$$y = \mu + a_1 x_1 + a_2 x_2 + \varepsilon$$

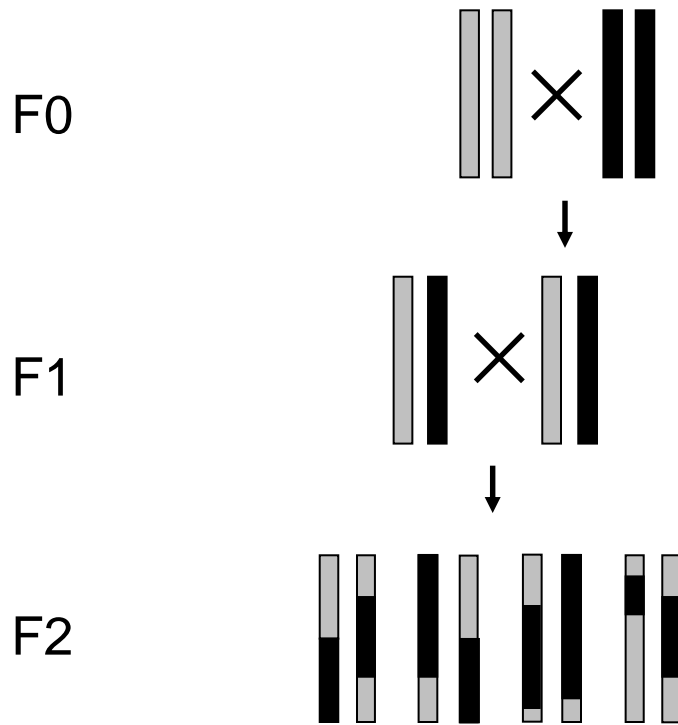
H_1 vs H_0 : Does **x2** explain a significant amount of the variation after accounting for x_1 ?

or

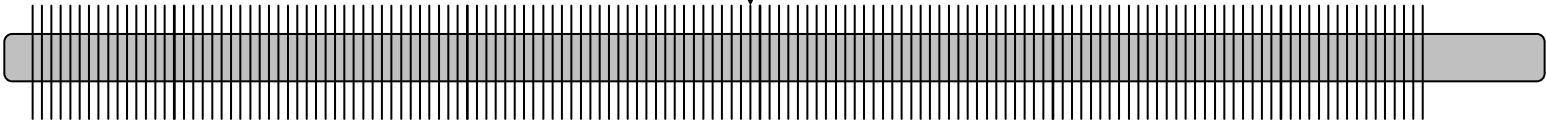
is **x2** significant conditional on x_1 ?

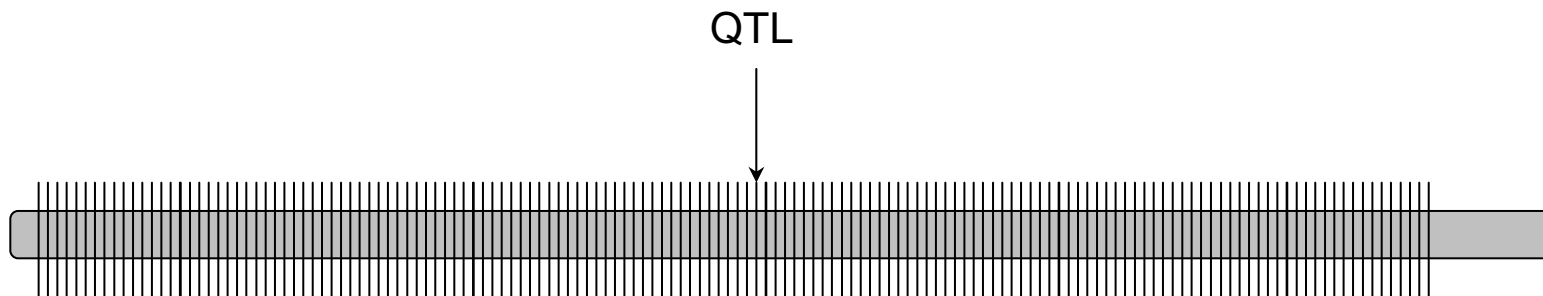
F2 cross

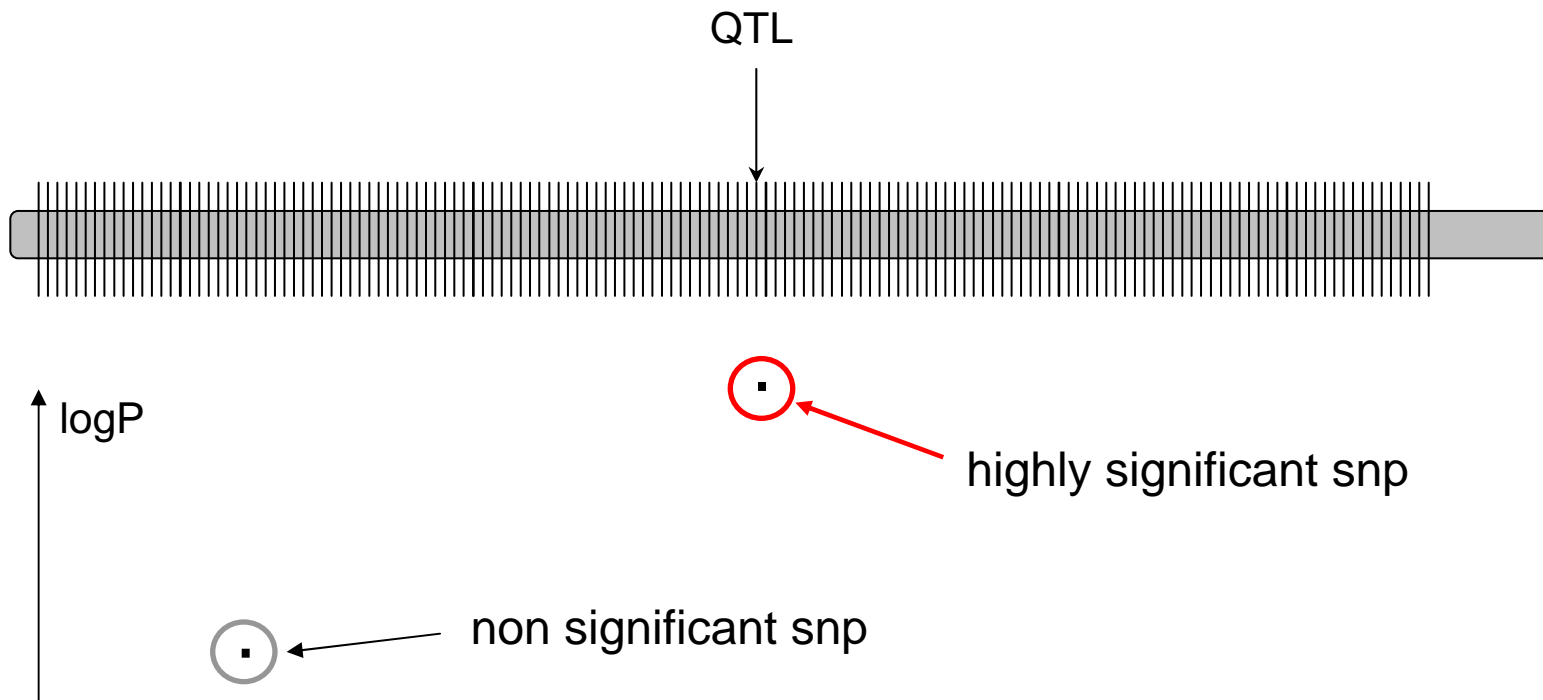
Generation

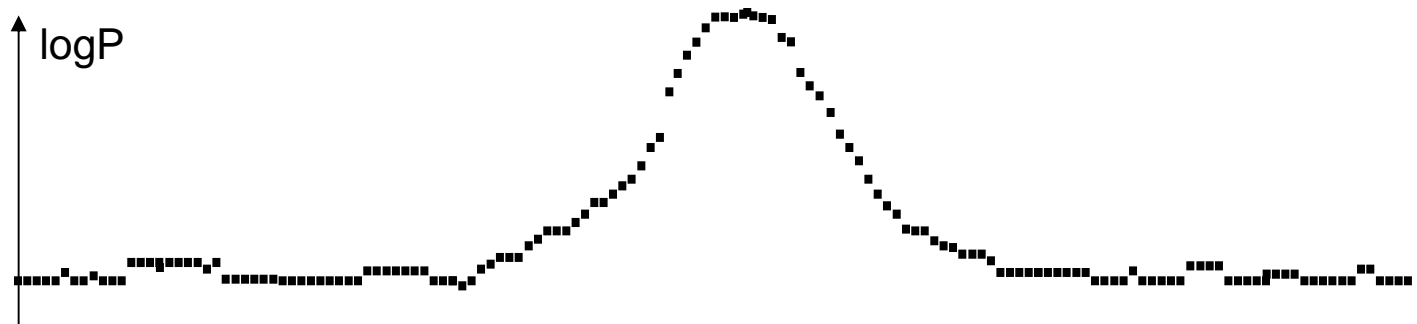
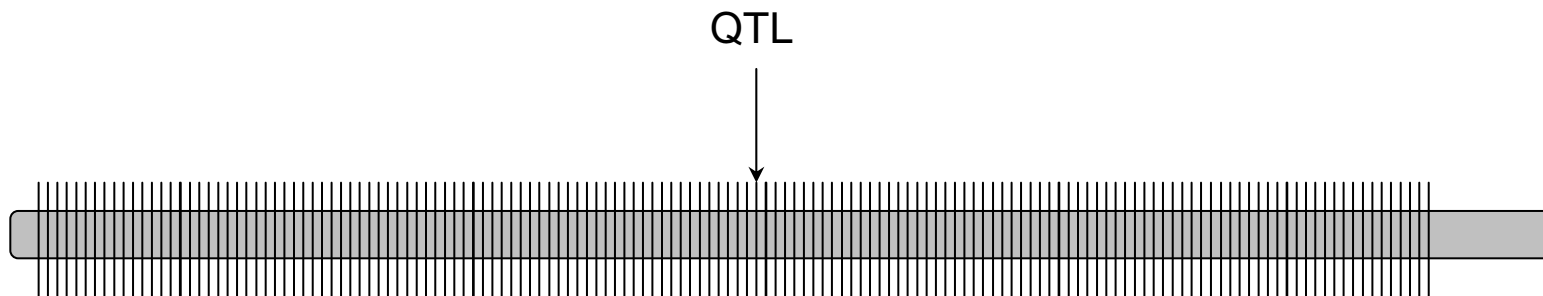


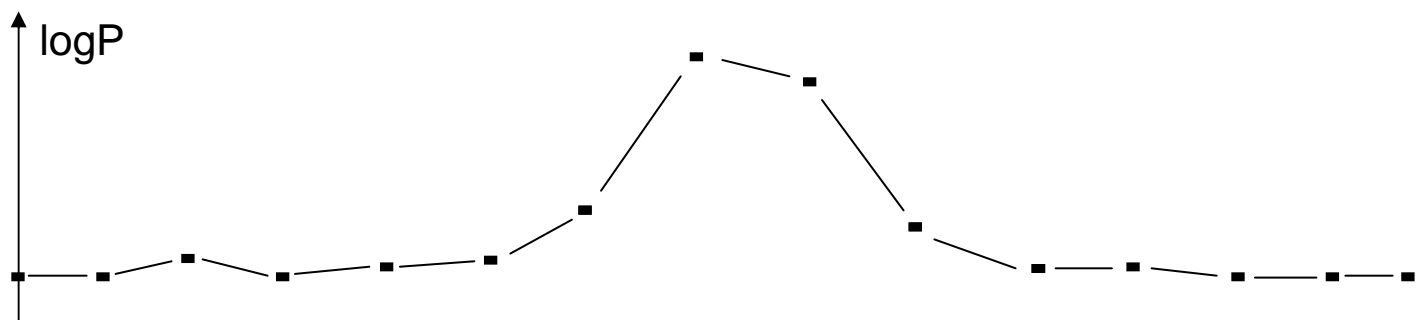
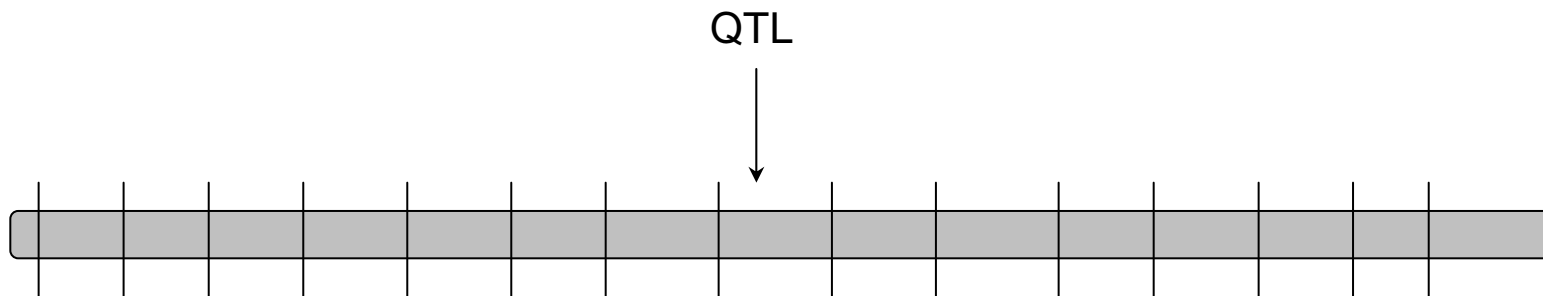
QTL



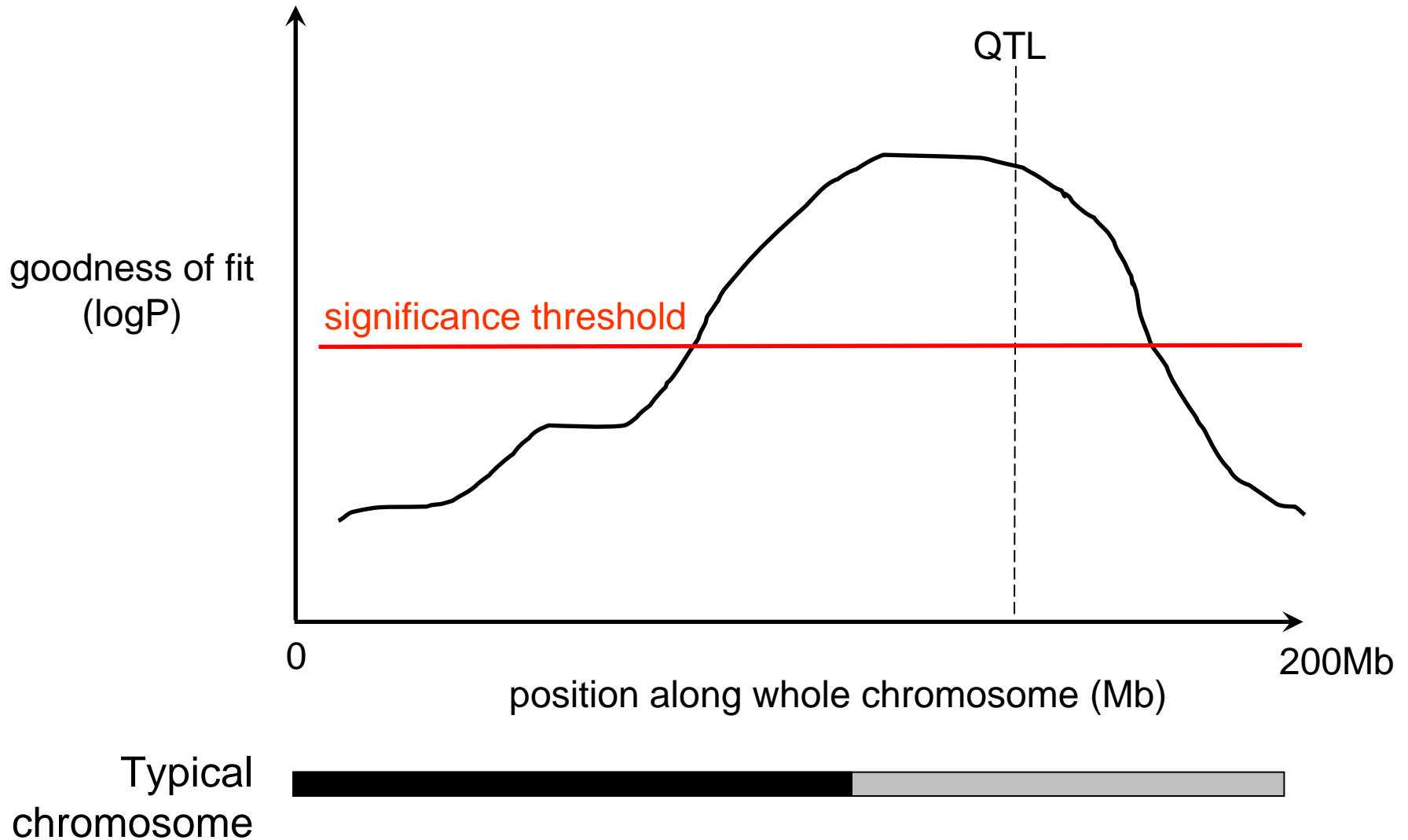




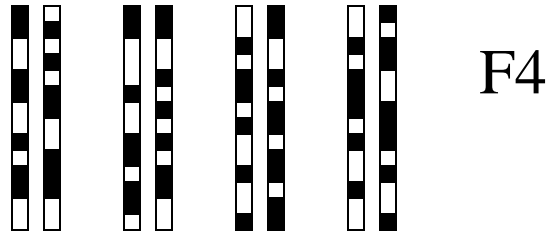
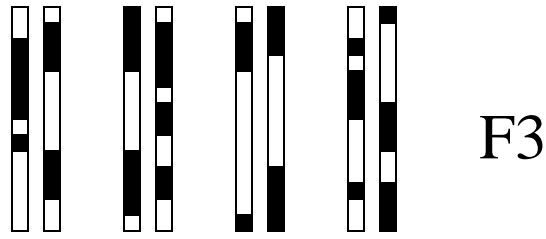
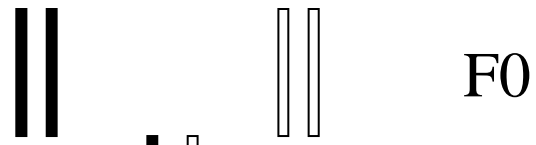




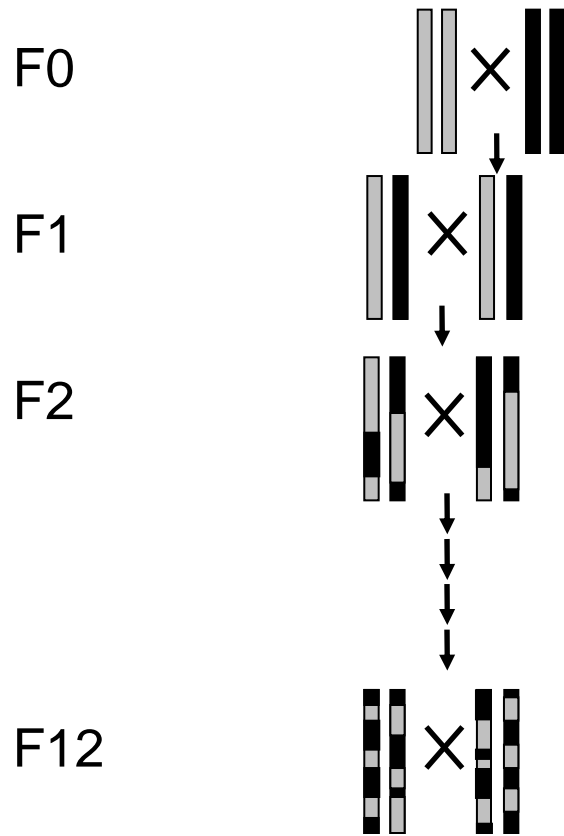
Chromosome scan for F2



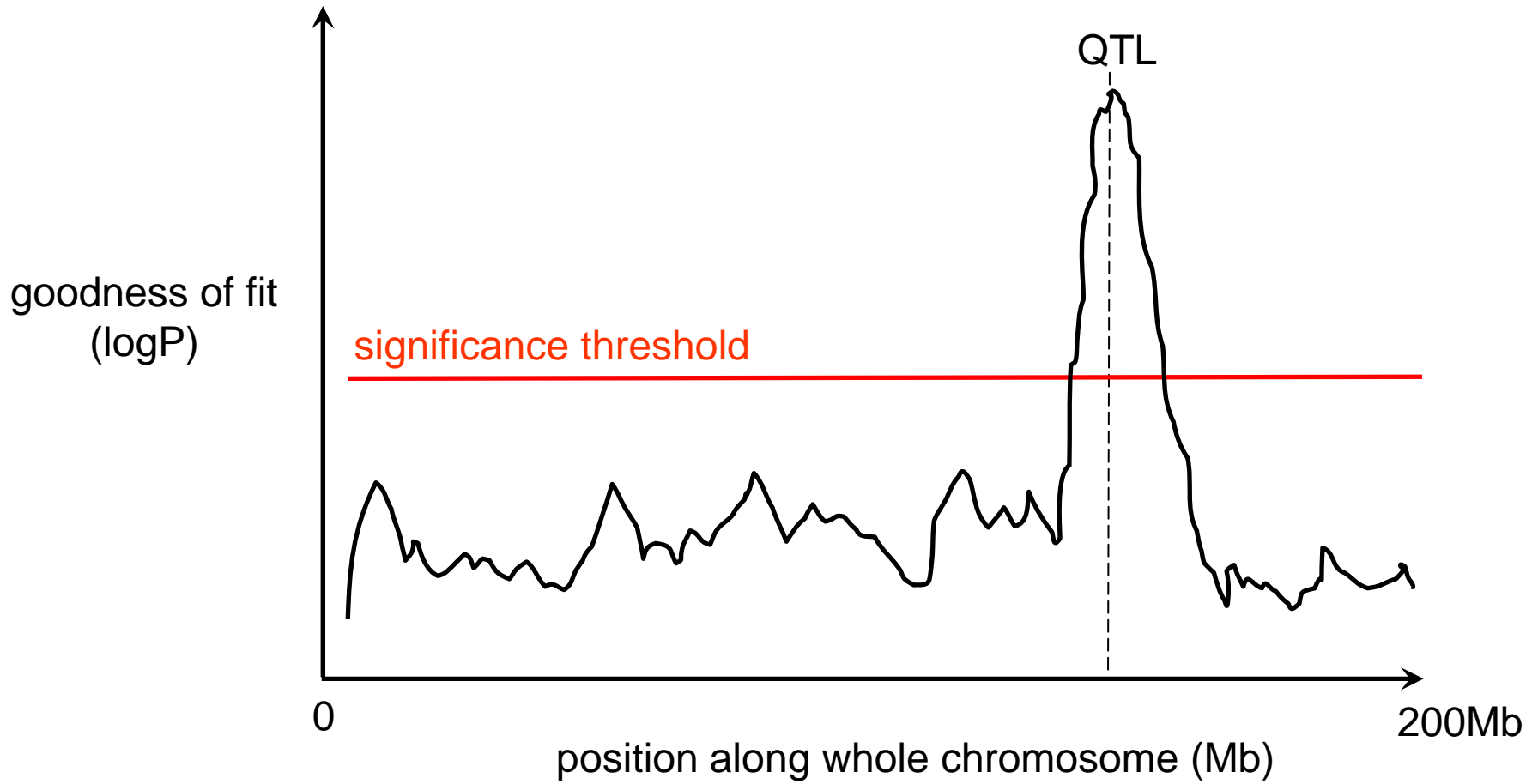
Advanced intercross lines (AILs)



F12 cross



Chromosome scan for F12



Typical
chromosome



Practical

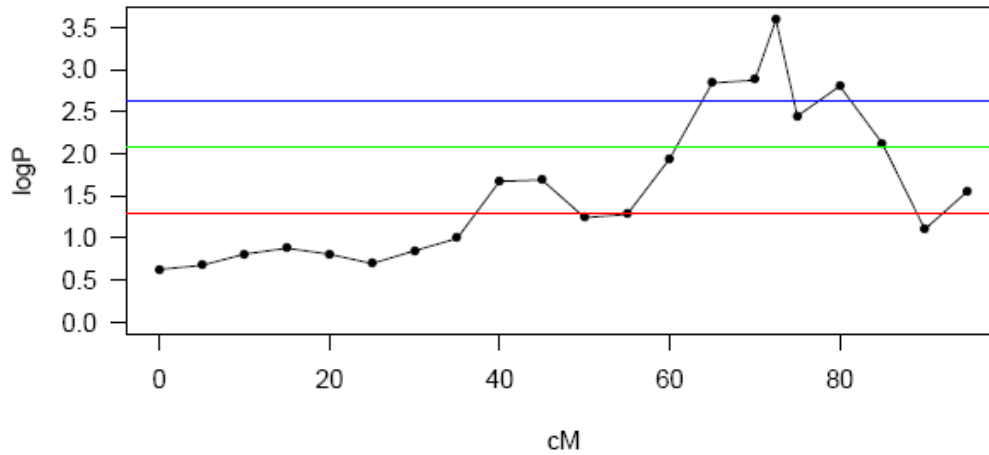
1. Fitting a linear model to test a marker-phenotype association
2. Single marker association on an F2
3. Permutation test
4. Single marker association on an AIL (F12)
5. Conditional modelling of loci

Start Firefox, File->Open and go to

F:\valdar\ThursdayAfternoonAnimals\practical.R

Start R

Practical: F2 cross

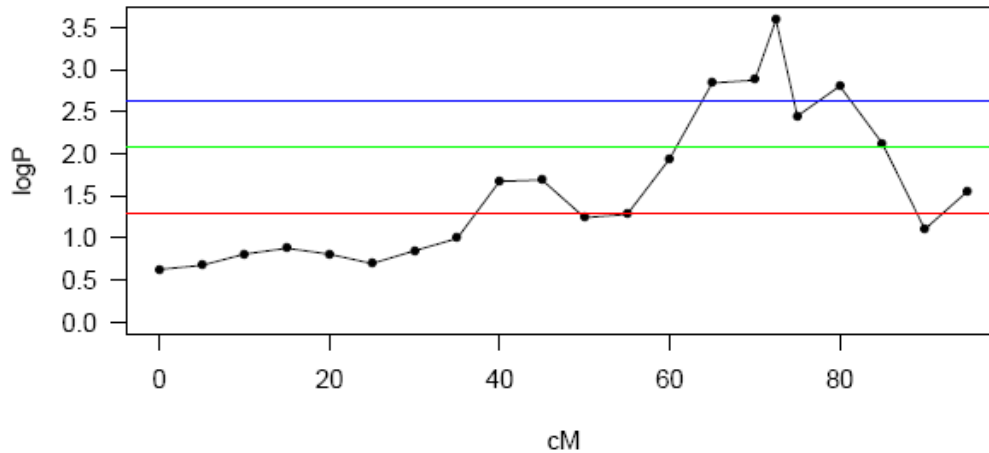


Bonferroni = 2.6

permutation ~ 2.1

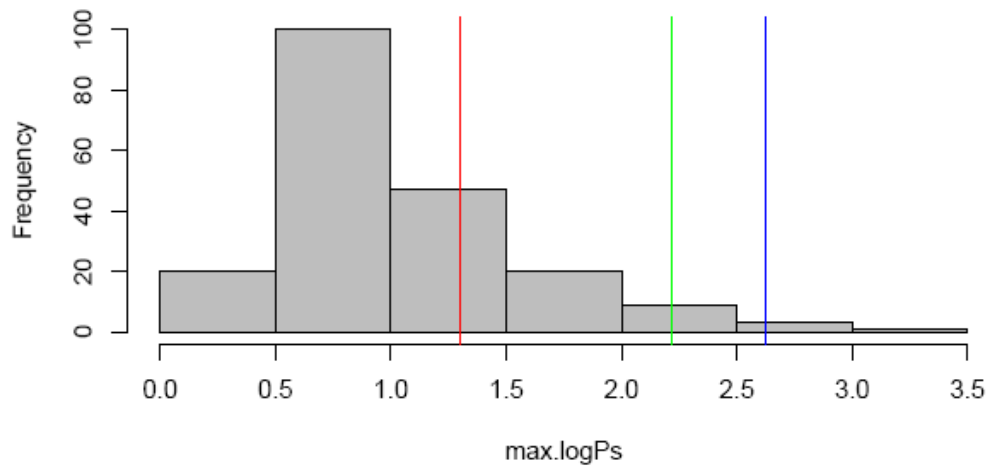
uncorrected = 1.3

Practical: F2 cross



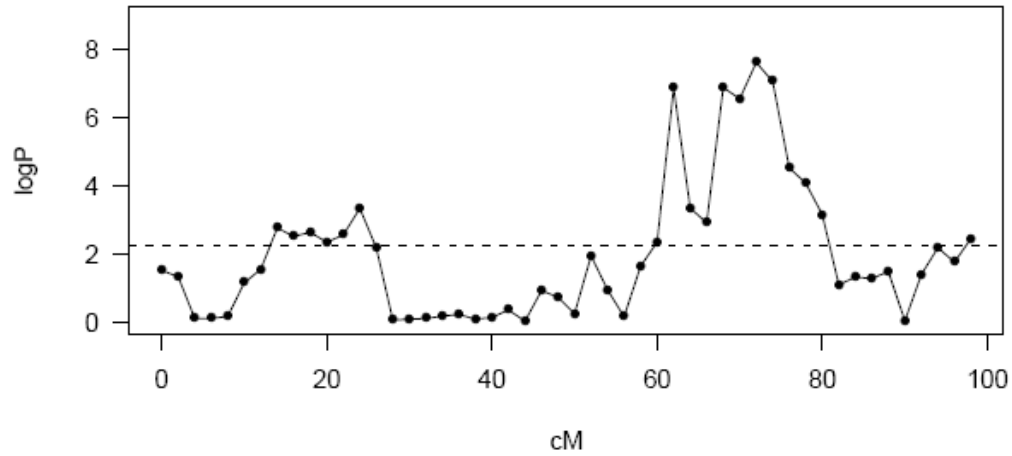
Bonferroni = 2.6
permutation ~ 2.1
uncorrected = 1.3

Histogram of max.logPs



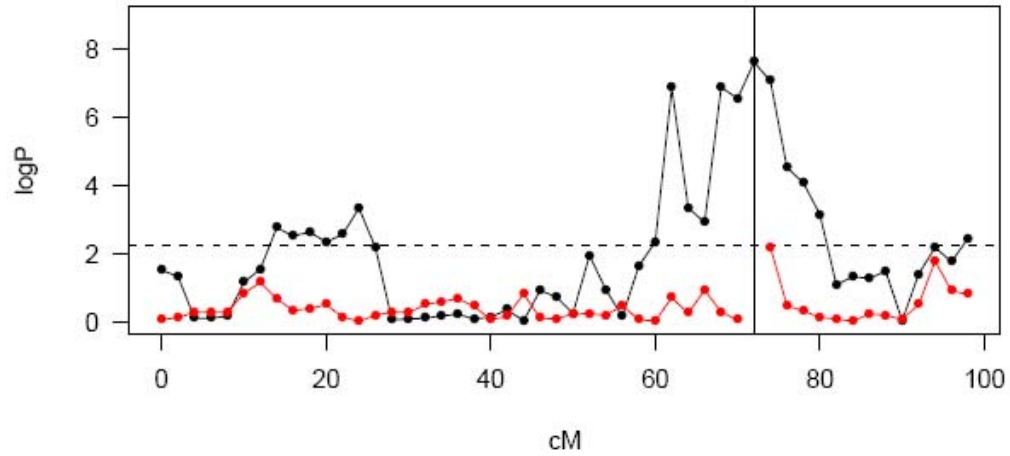
generalized extreme value
(GEV) distribution

Practical: F12



phenotype ~ MARKER

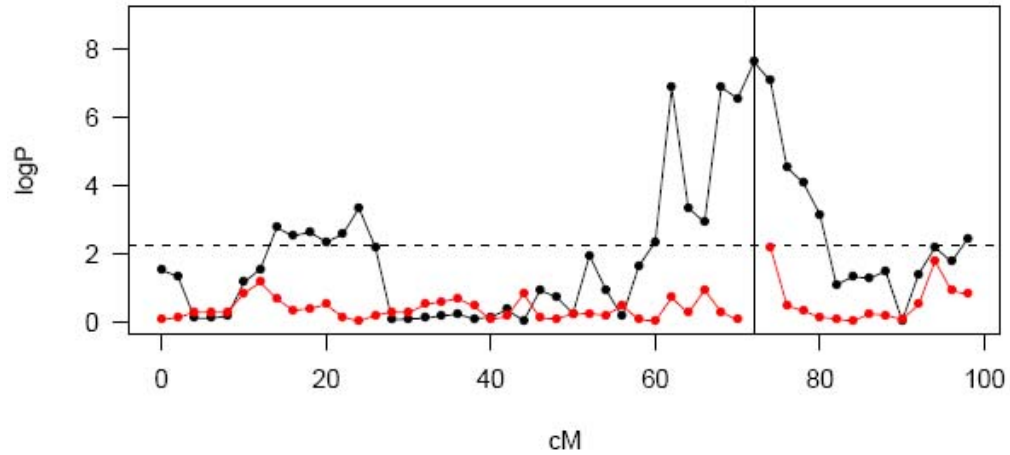
Practical: F12



phenotype ~ MARKER

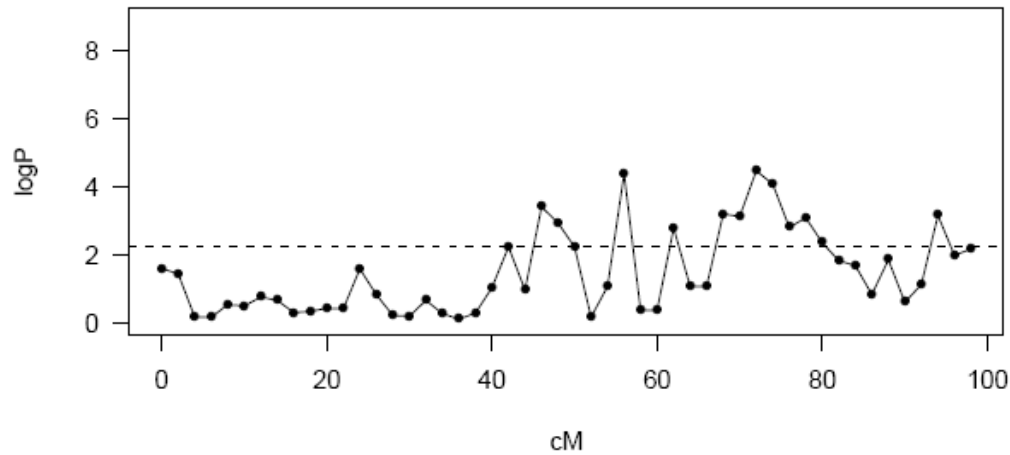
phenotype ~ m37 + MARKER

Practical: F12



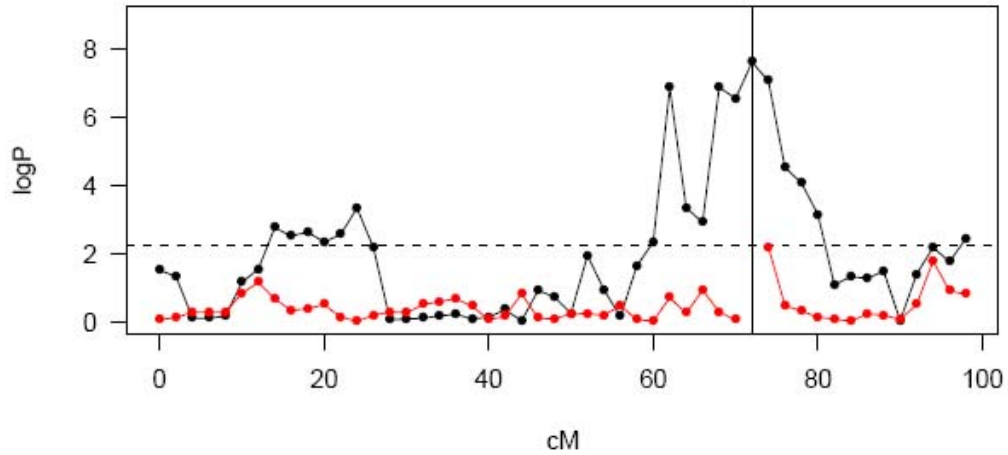
phenotype ~ MARKER

phenotype ~ m37 + MARKER



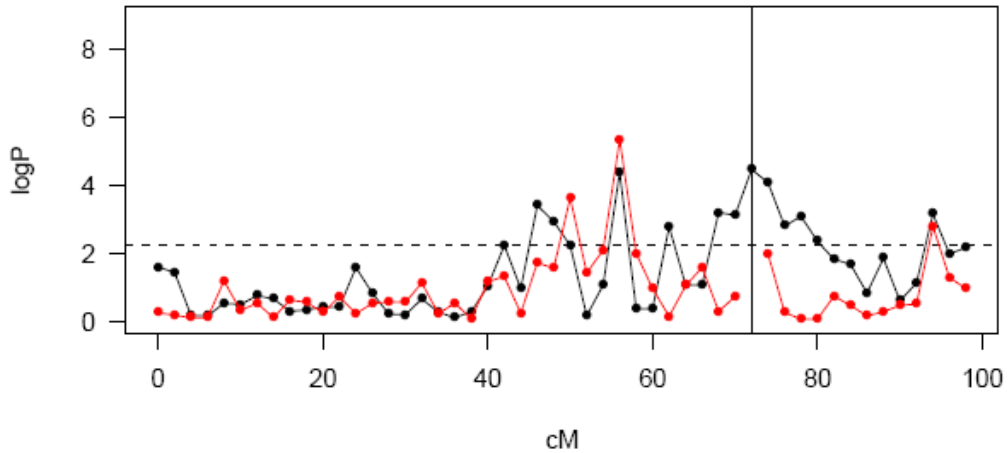
phenotype ~ MARKER

Practical: F12



phenotype ~ MARKER

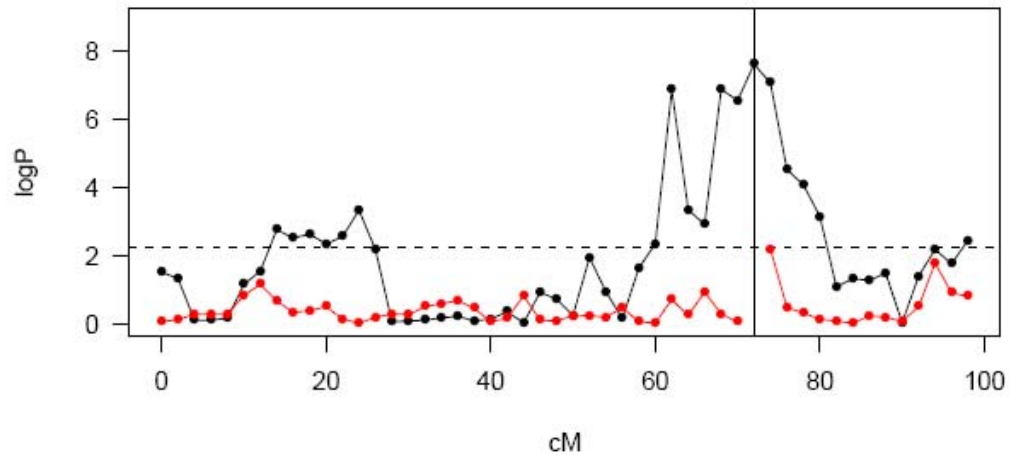
phenotype ~ m37 + MARKER



phenotype ~ MARKER

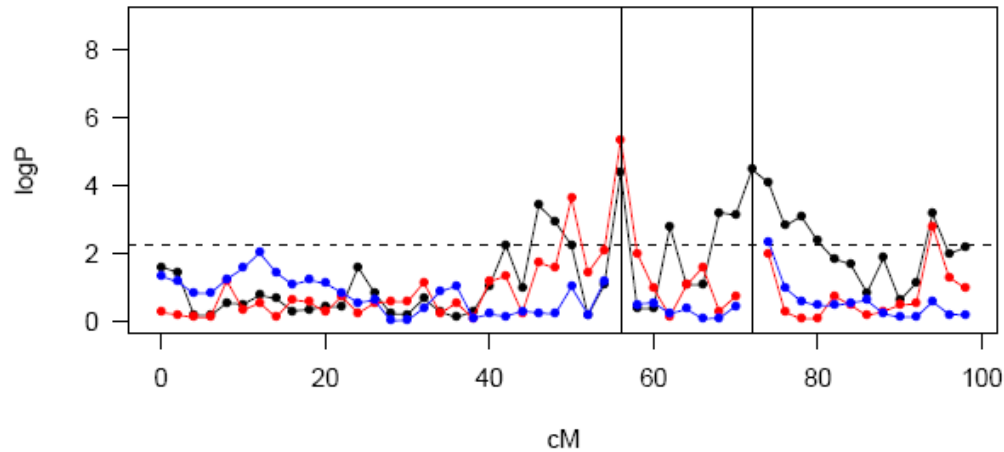
phenotype ~ m37 + MARKER

Practical: F12



phenotype ~ MARKER

phenotype ~ m37 + MARKER

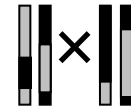


phenotype ~ MARKER

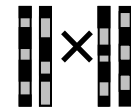
phenotype ~ m37 + MARKER

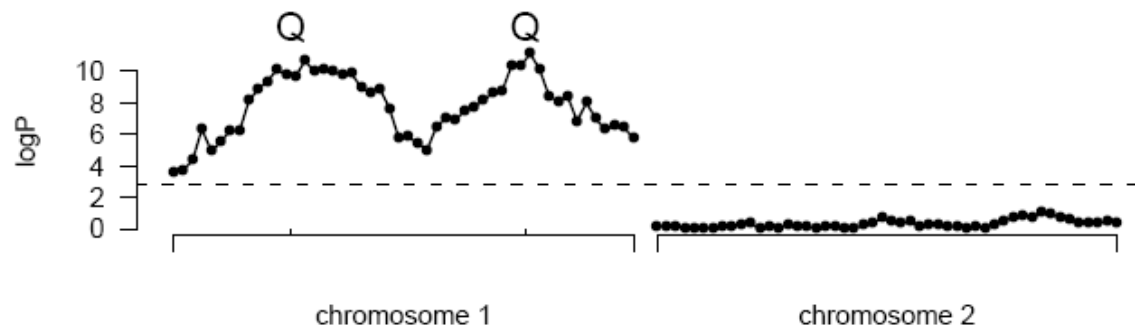
phenotype ~ m37 + m29 + MARKER

F2

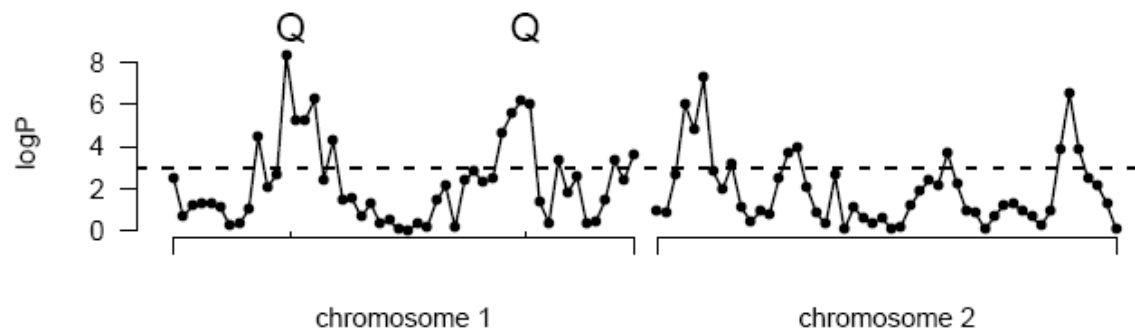
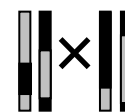


F18

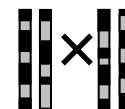


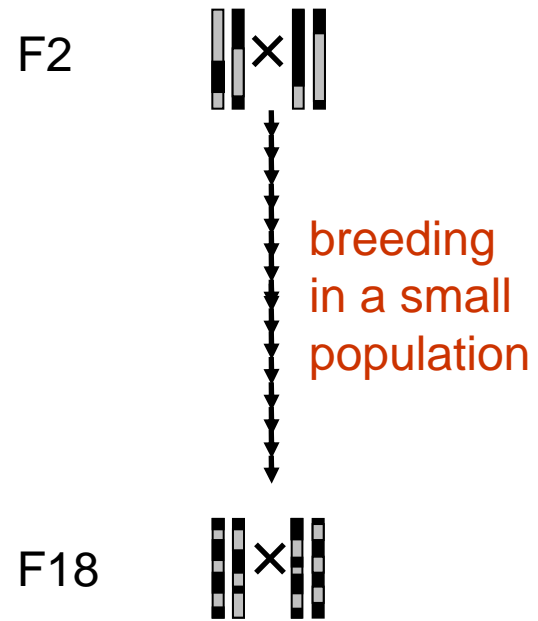
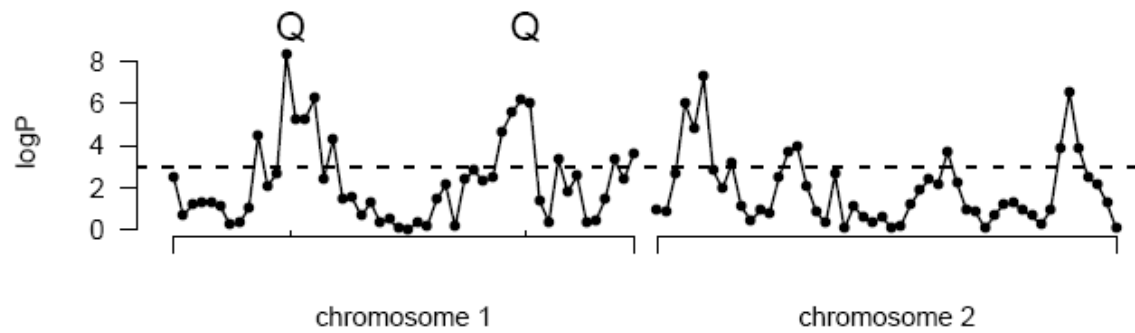
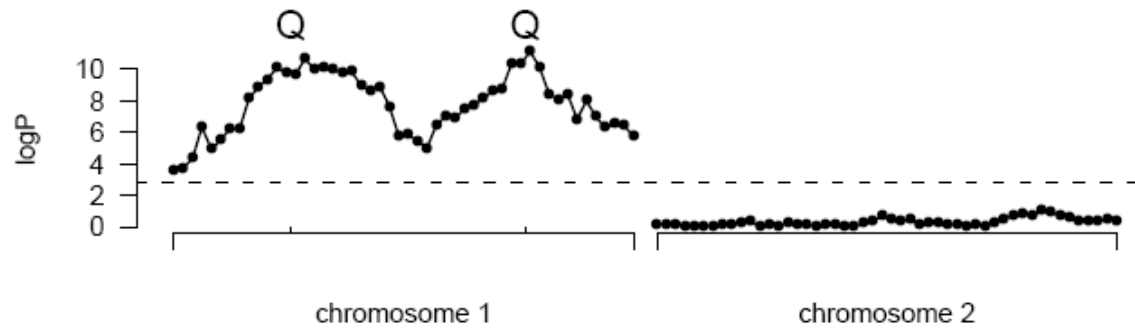


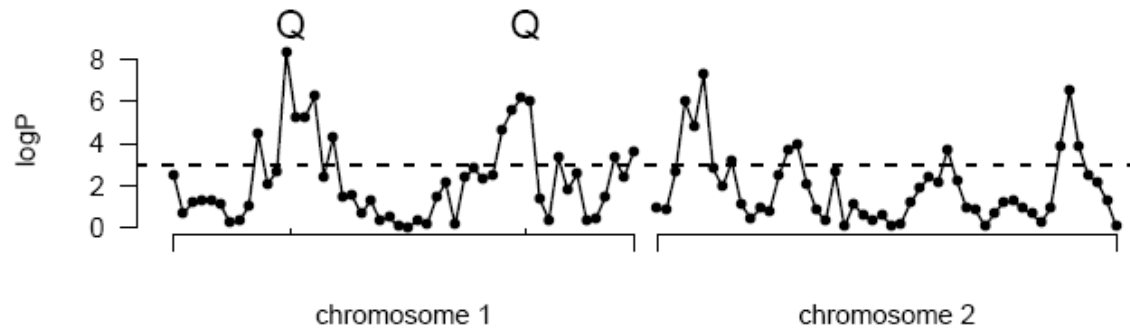
F2



F18



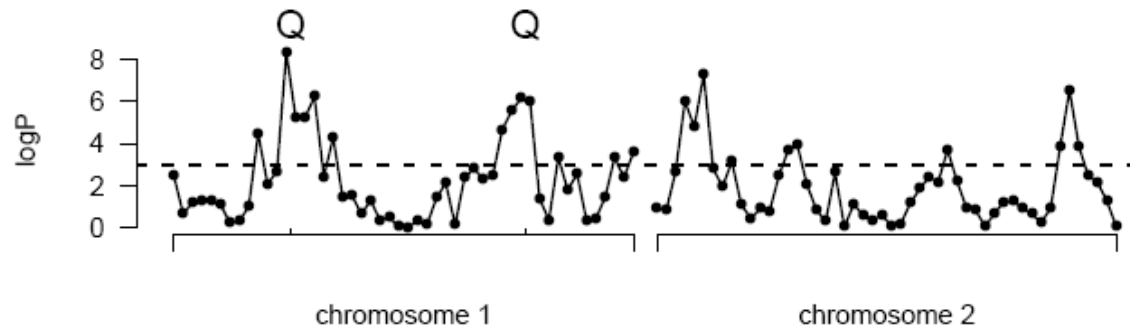




population structure

gross genetic differences
between groups

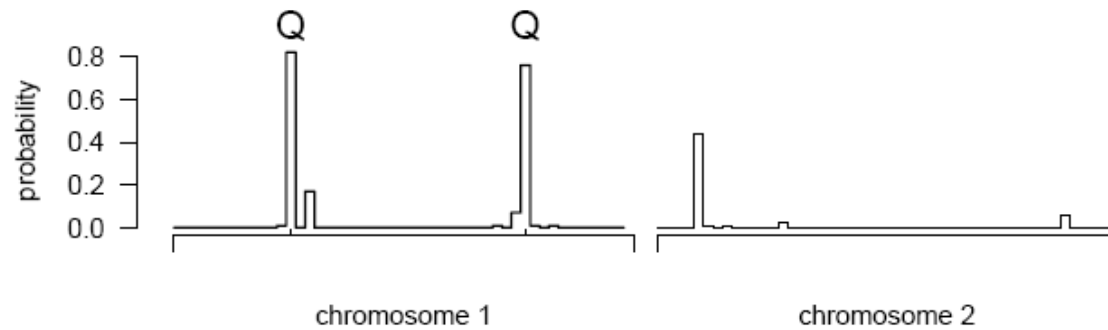
where groups = families



population structure

gross genetic differences
between groups

where groups = families

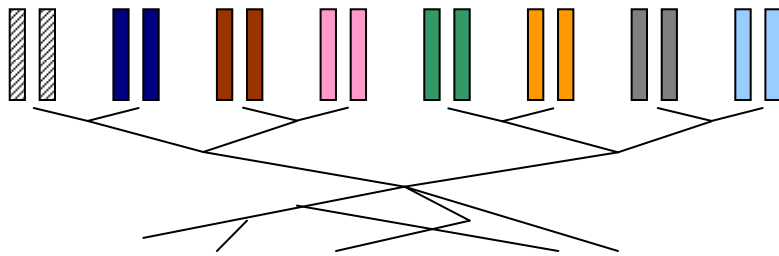


multilocus approach

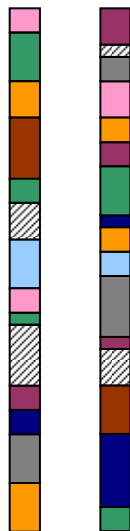
Heterogeneous Stocks



Heterogeneous Stock



Pseudo-random mating
for 50 generations



Avg. Distance Between
Recombinations:

HS
~2 cM

Heterogeneous Stock



Pseudo-random mating
for 50 generations



Avg. Distance Between
Recombinations:

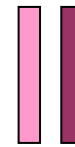
HS
~2 cM

F2 intercross
~30 cM

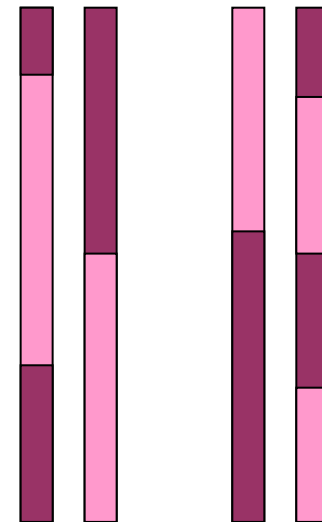
F2 Intercross



X



F1



F2

124 Phenotypes

Anxiety [24]

Asthma [13]

Biochemistry [15]

Bone Morphology [23]

Diabetes [16]

Haematology [15]

Immunology [9]

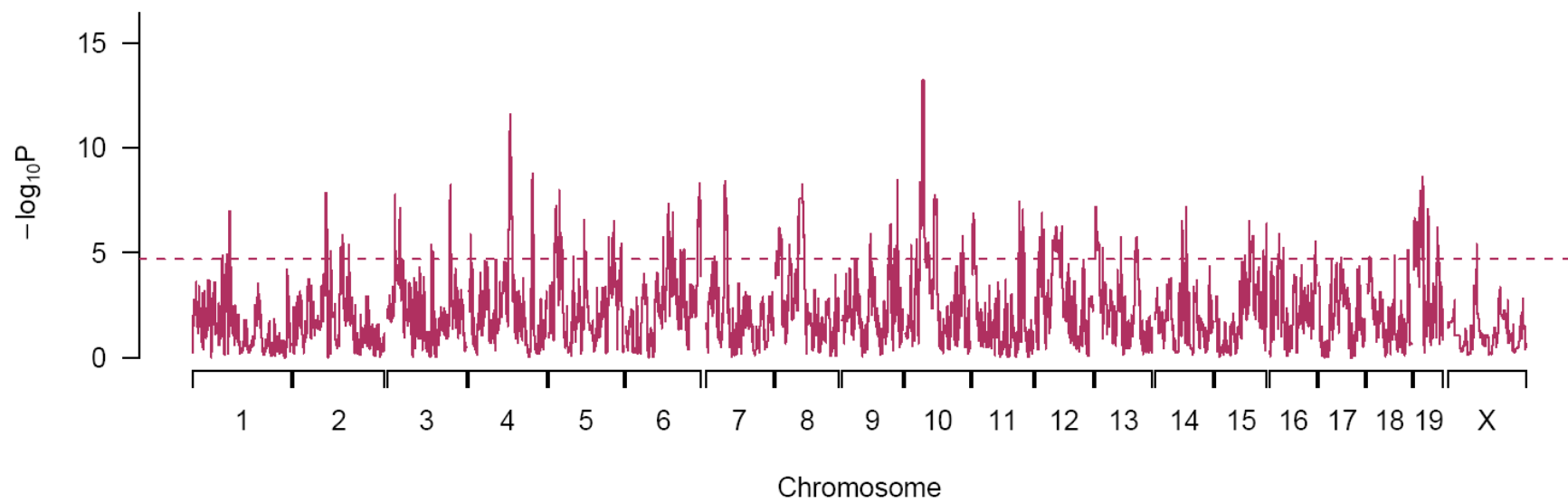
Weight/size related [8]

Wound Healing [1]

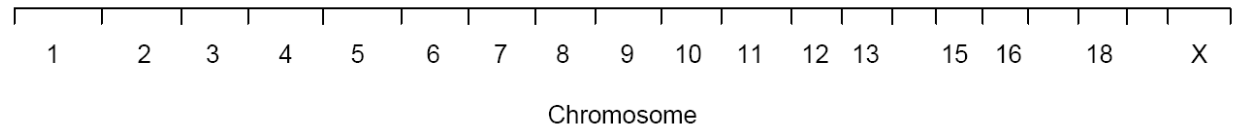


Intraperitoneal Glucose Tolerance Test

Glucose AUC



How to select peaks: a simulated example



How to select peaks: a simulated example

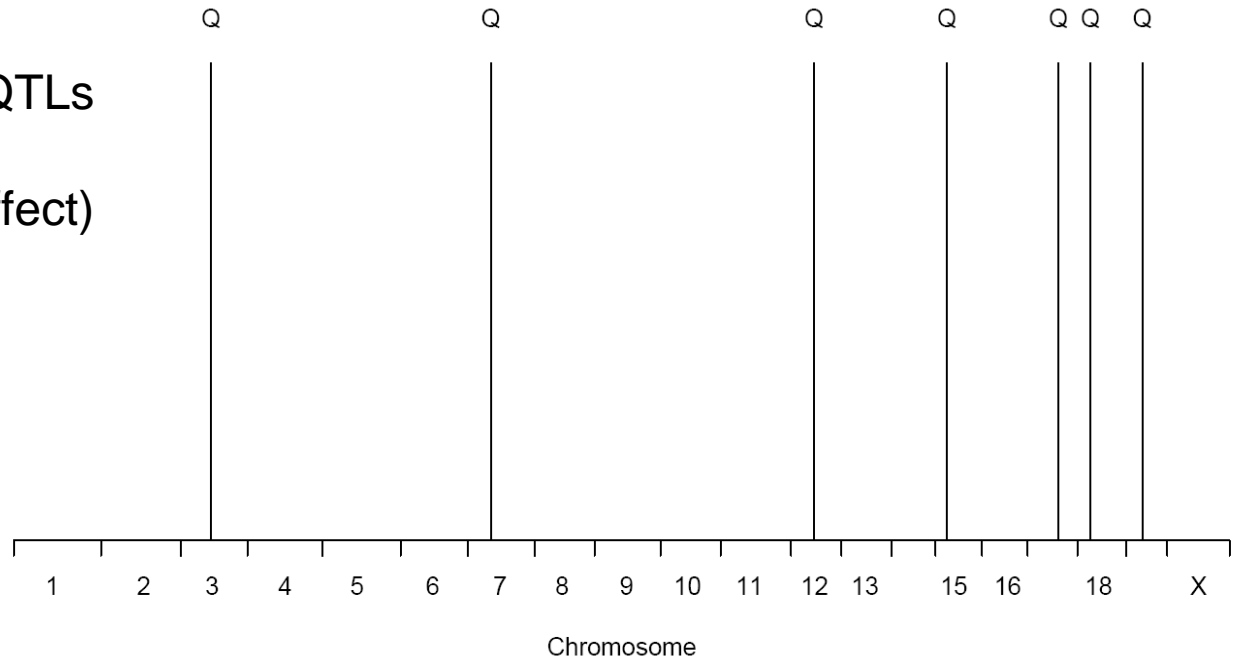
Simulate 7 x 5% QTLs

(ie, 35% genetic effect)

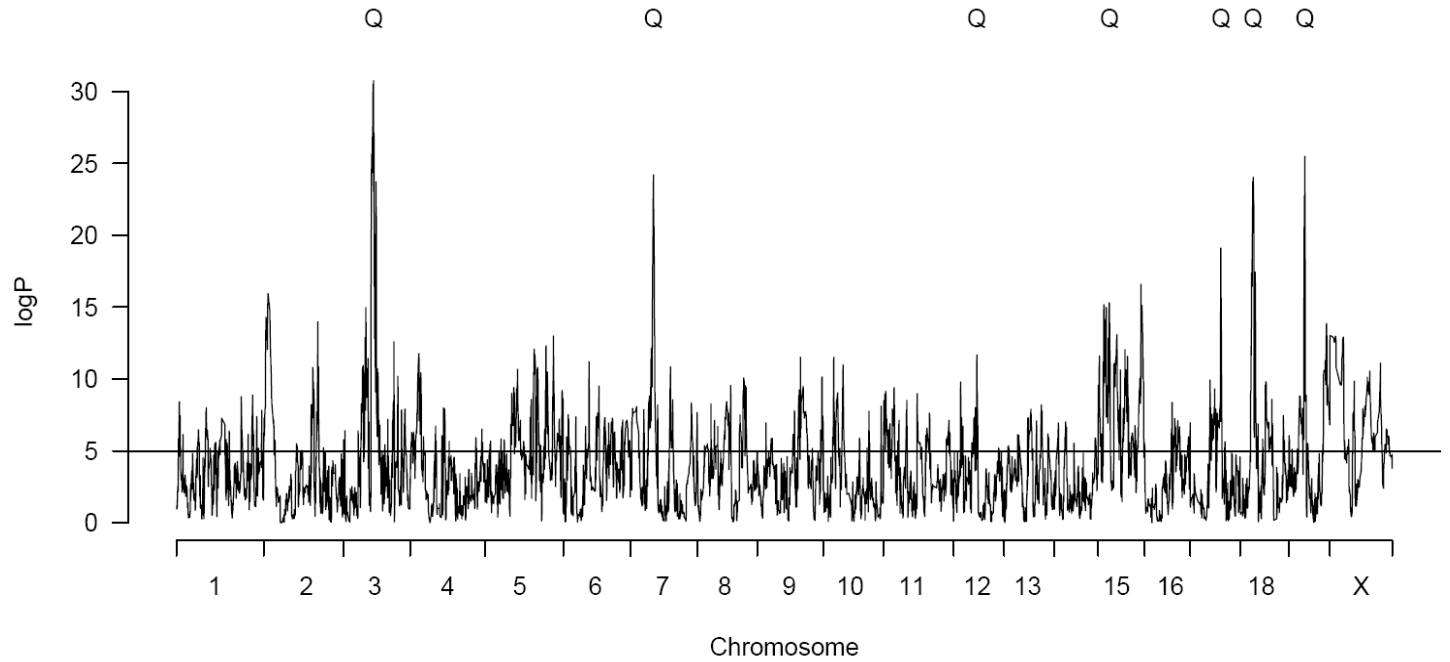
+ 20% shared
environment effect

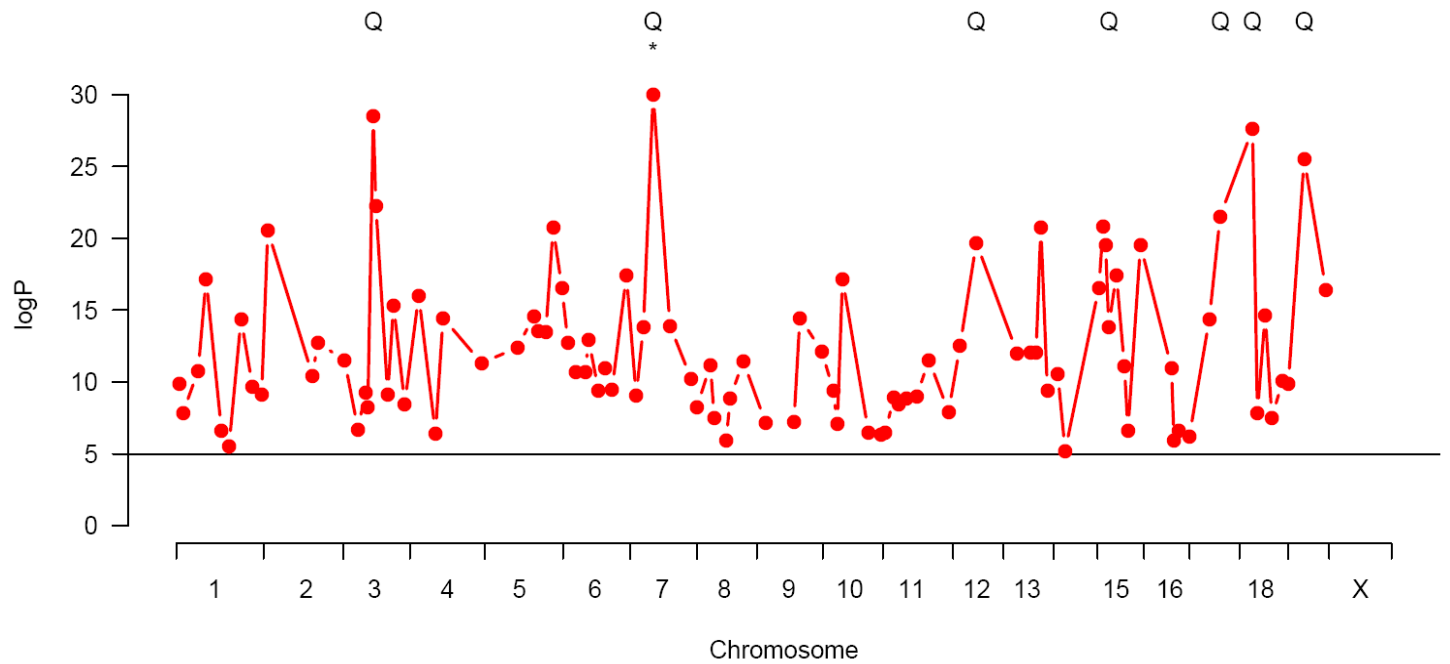
+ 45% noise

= 100% variance



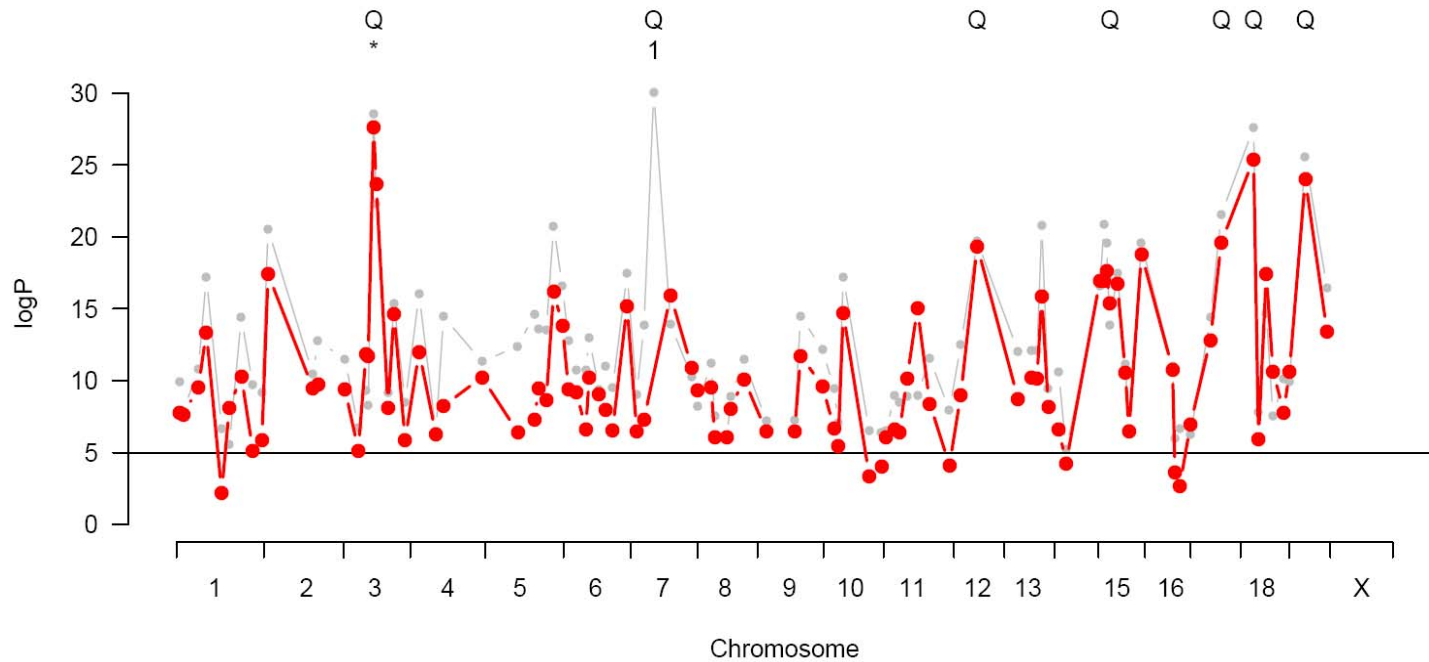
Simulated example





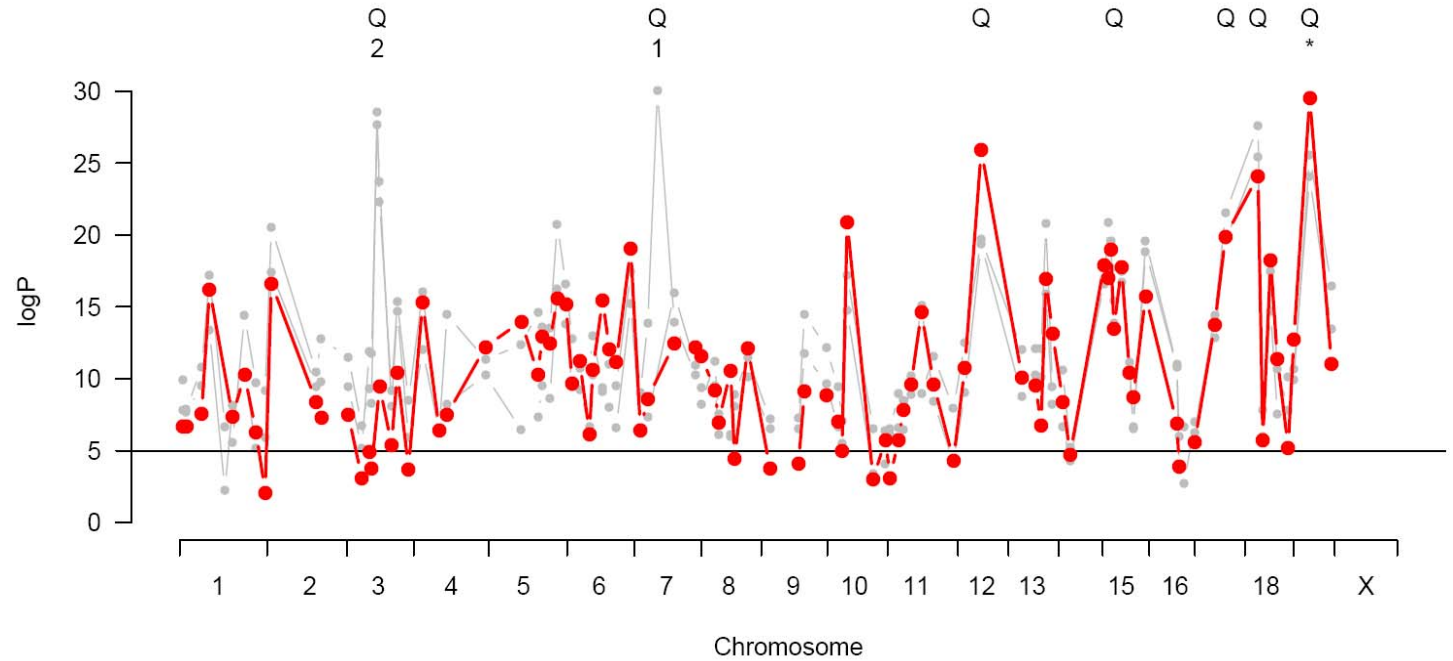
phenotype ~ ?

condition on 1 peak



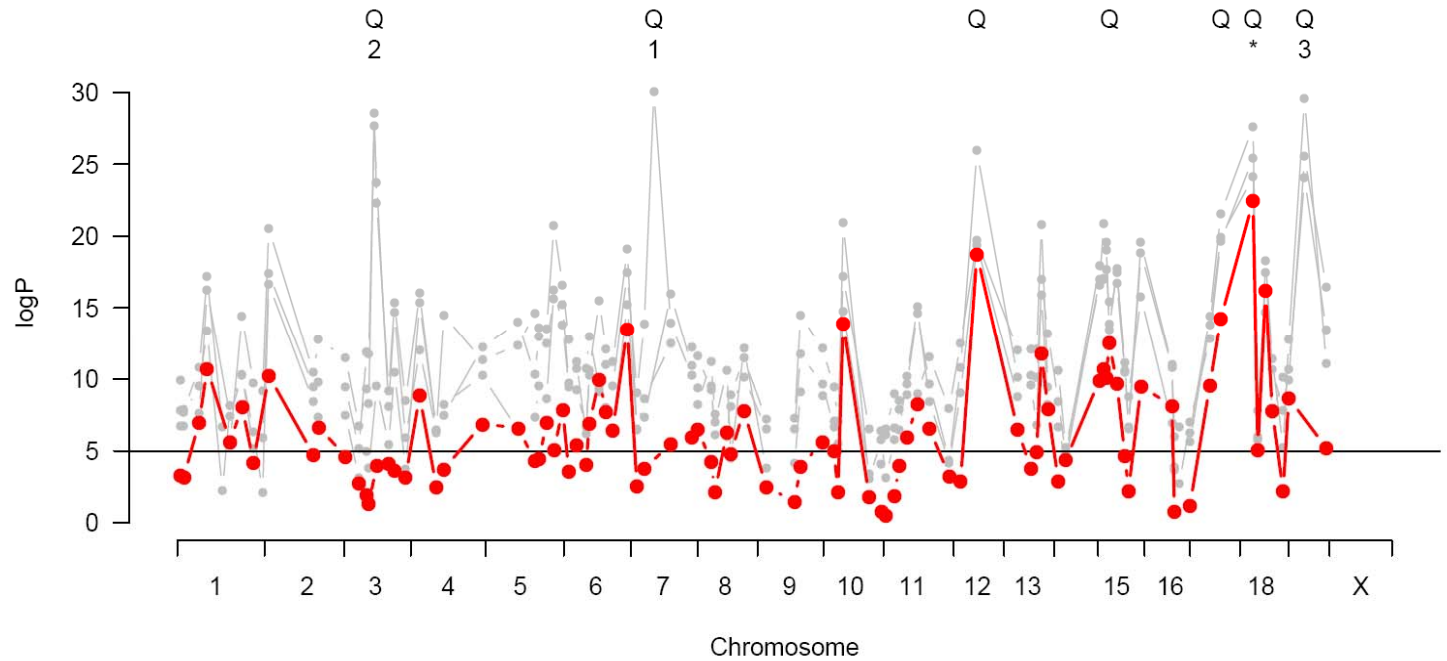
phenotype \sim peak 1 + ?

condition on 2 peaks



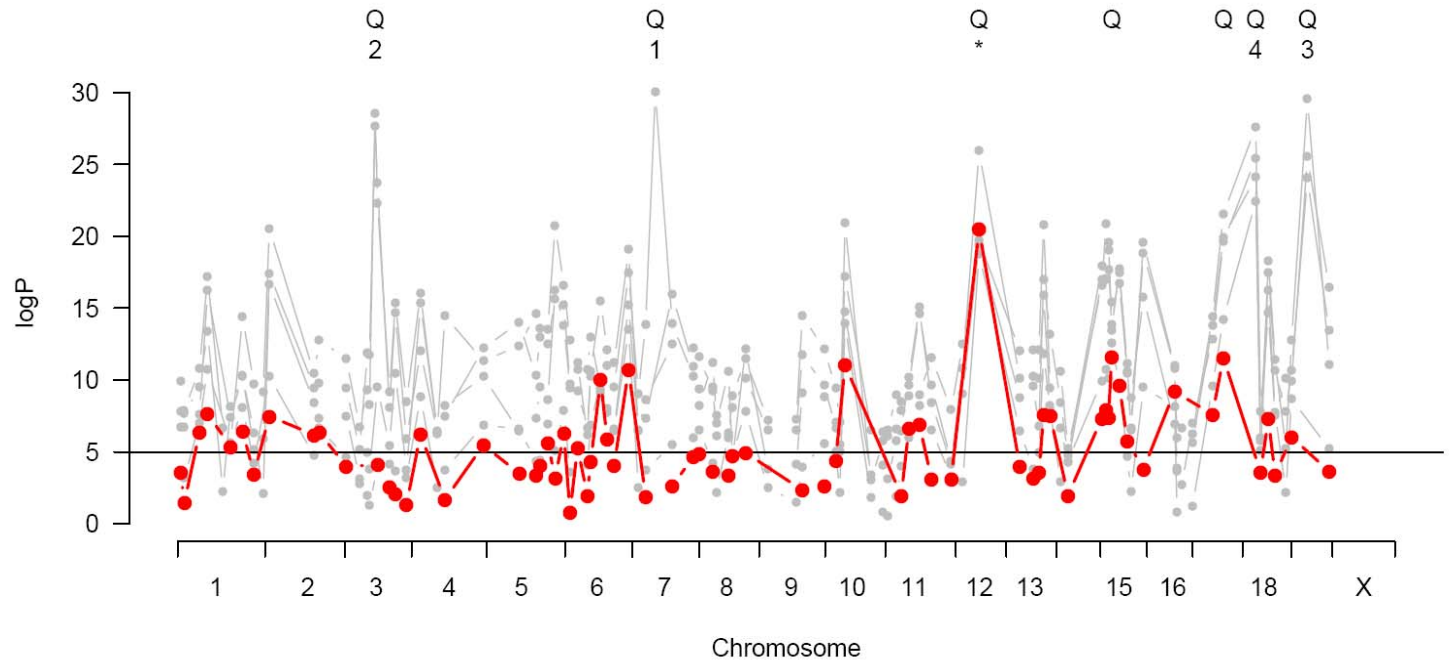
phenotype \sim peak 1 + peak 2 + ?

condition on 3 peaks



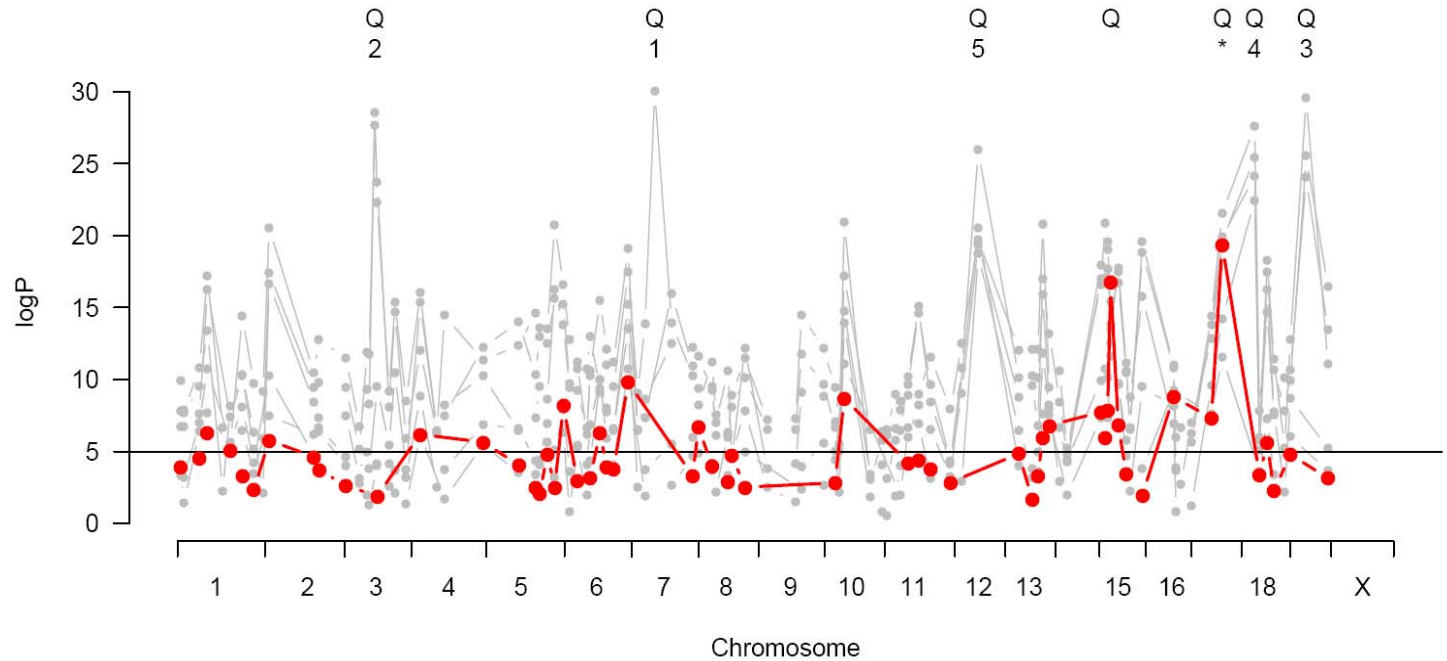
phenotype \sim peak 1 + peak 2 + peak 3 + ?

condition on 4 peaks



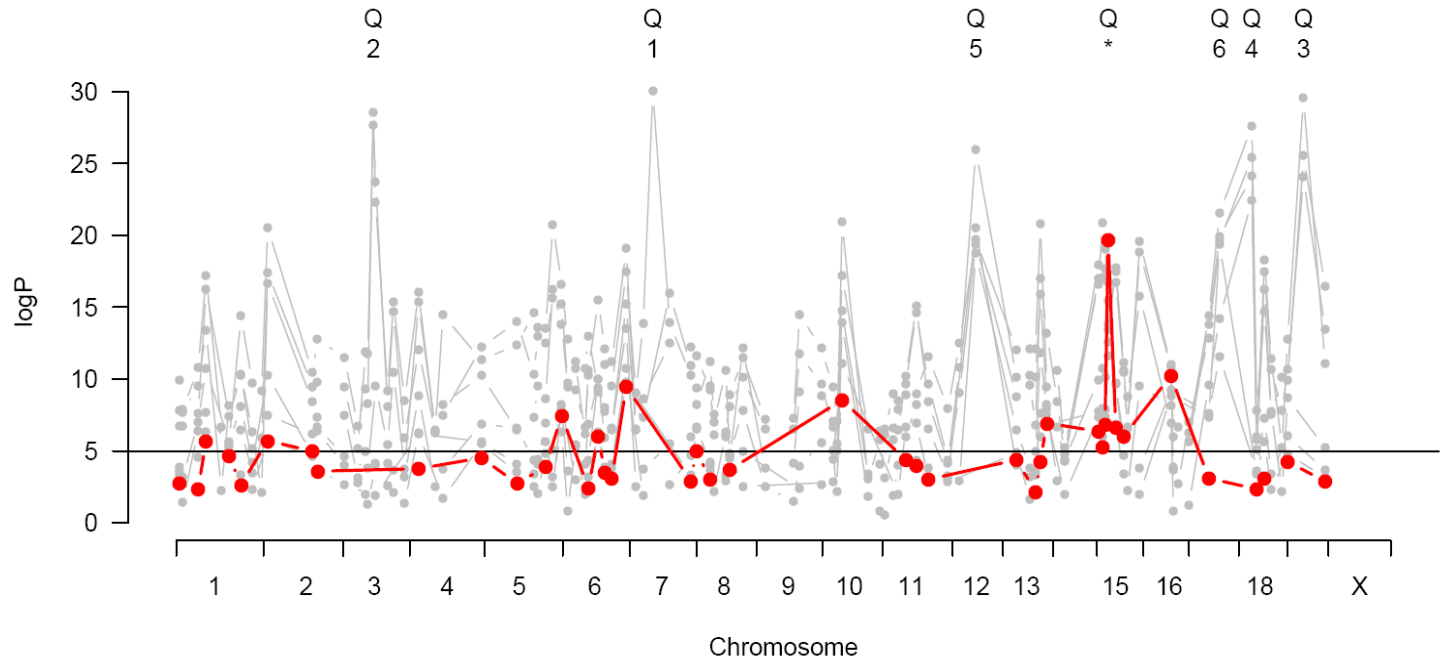
phenotype \sim peak 1 + peak 2 + peak 3 + peak 4 + ?

condition on 5 peaks



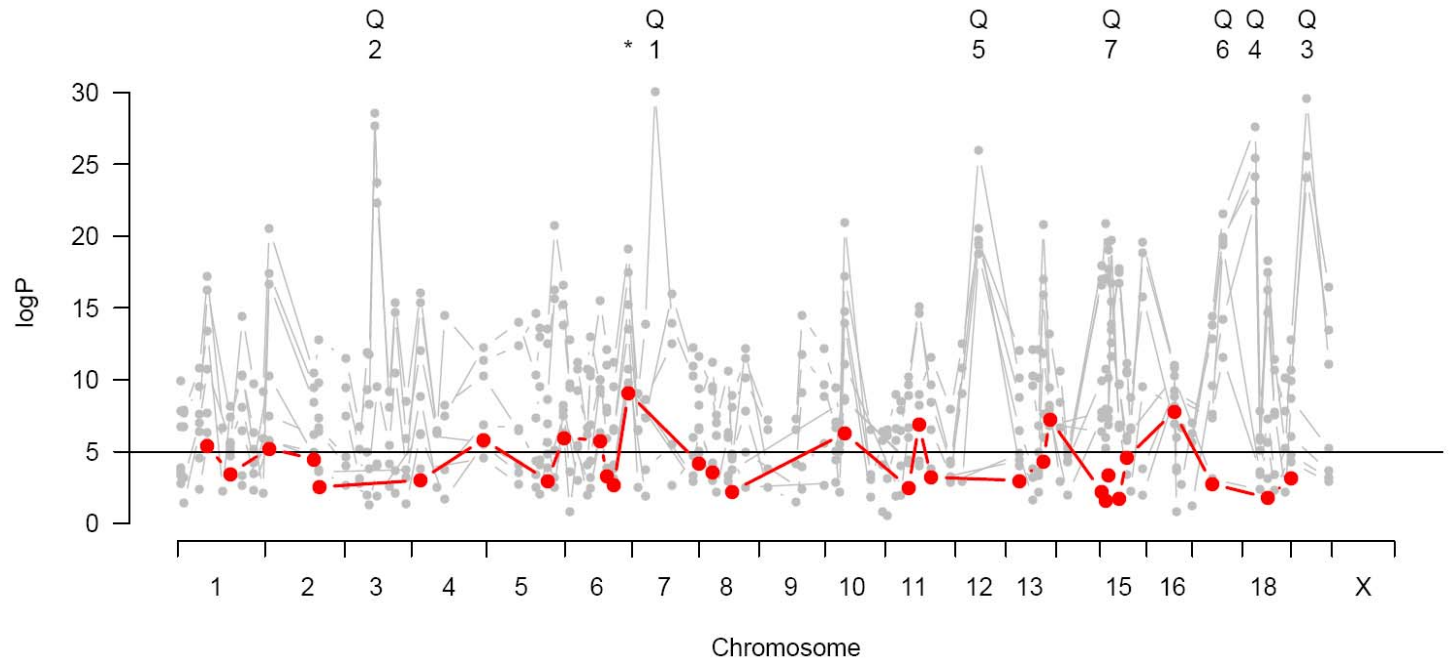
phenotype \sim peak 1 + peak 2 + peak 3 + peak 4 +
peak 5 + ?

condition on 6 peaks



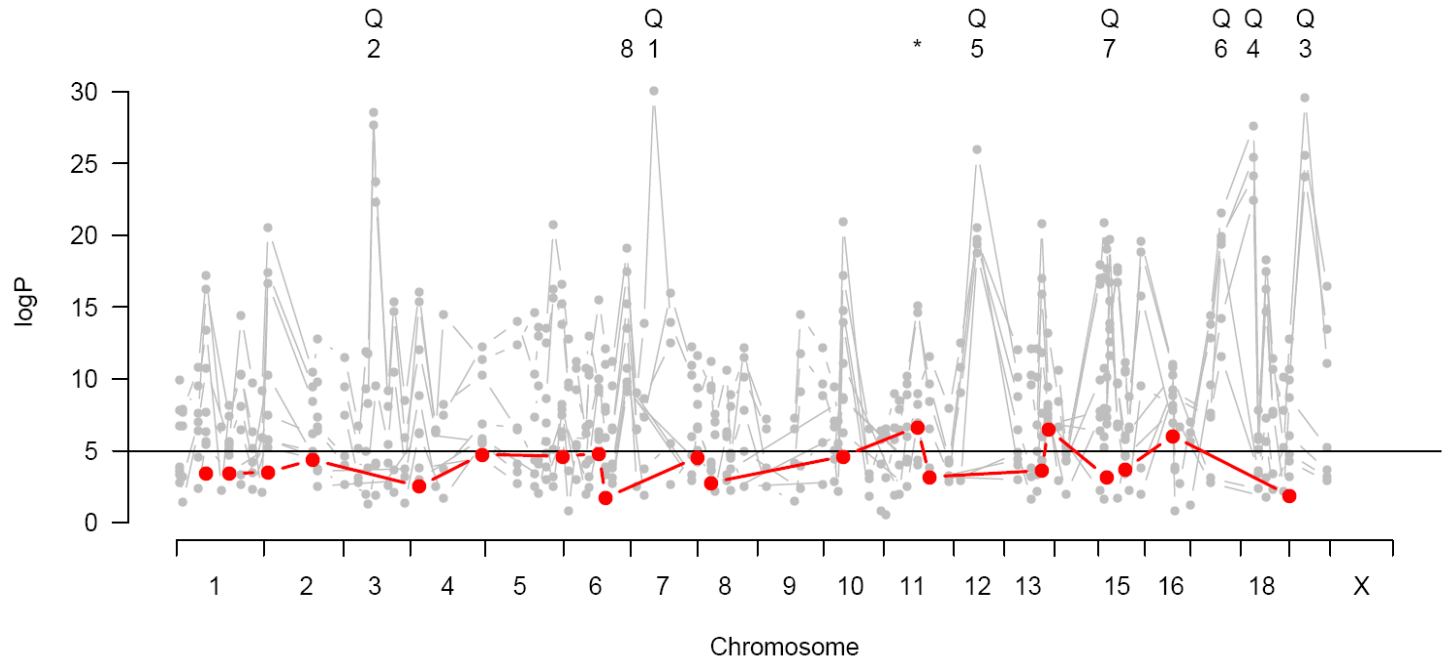
phenotype \sim peak 1 + peak 2 + peak 3 + peak 4 +
peak 5 + peak 6 + ?

condition on 7 peaks



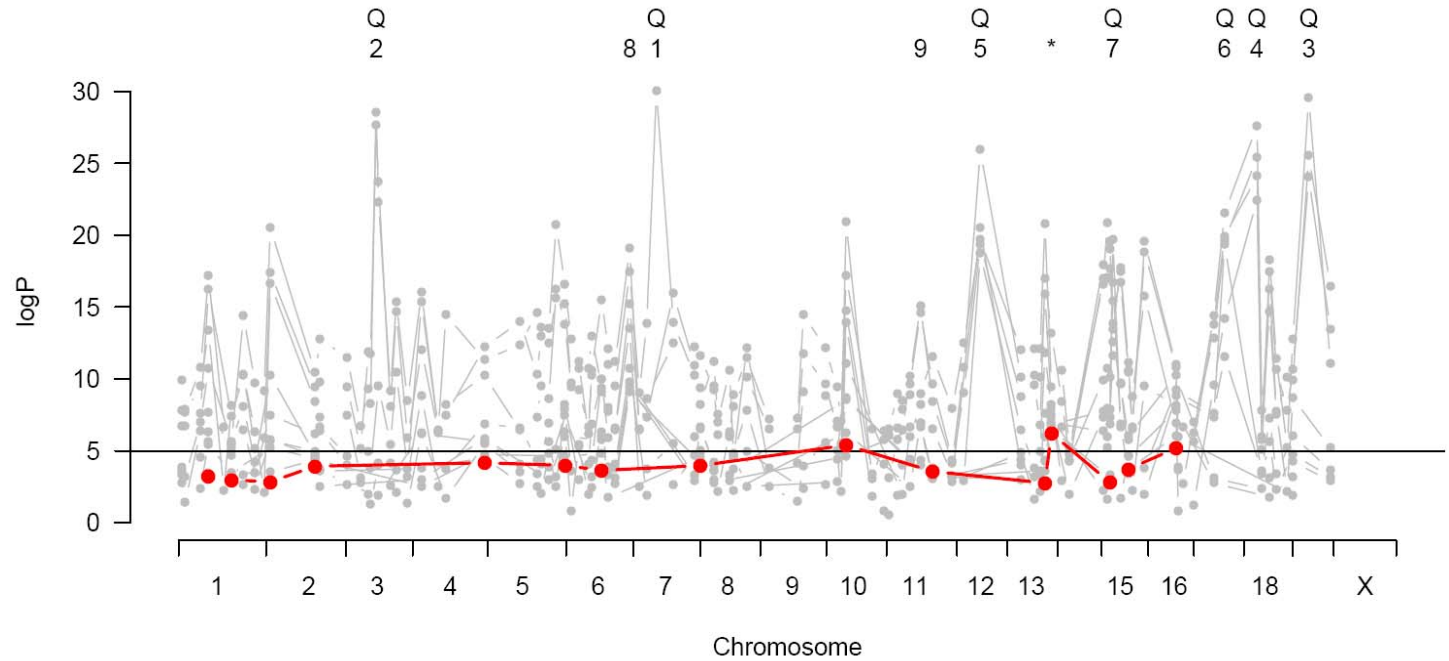
phenotype \sim peak 1 + peak 2 + peak 3 + peak 4 +
peak 5 + peak 6 + peak 7 + ?

condition on 8 peaks



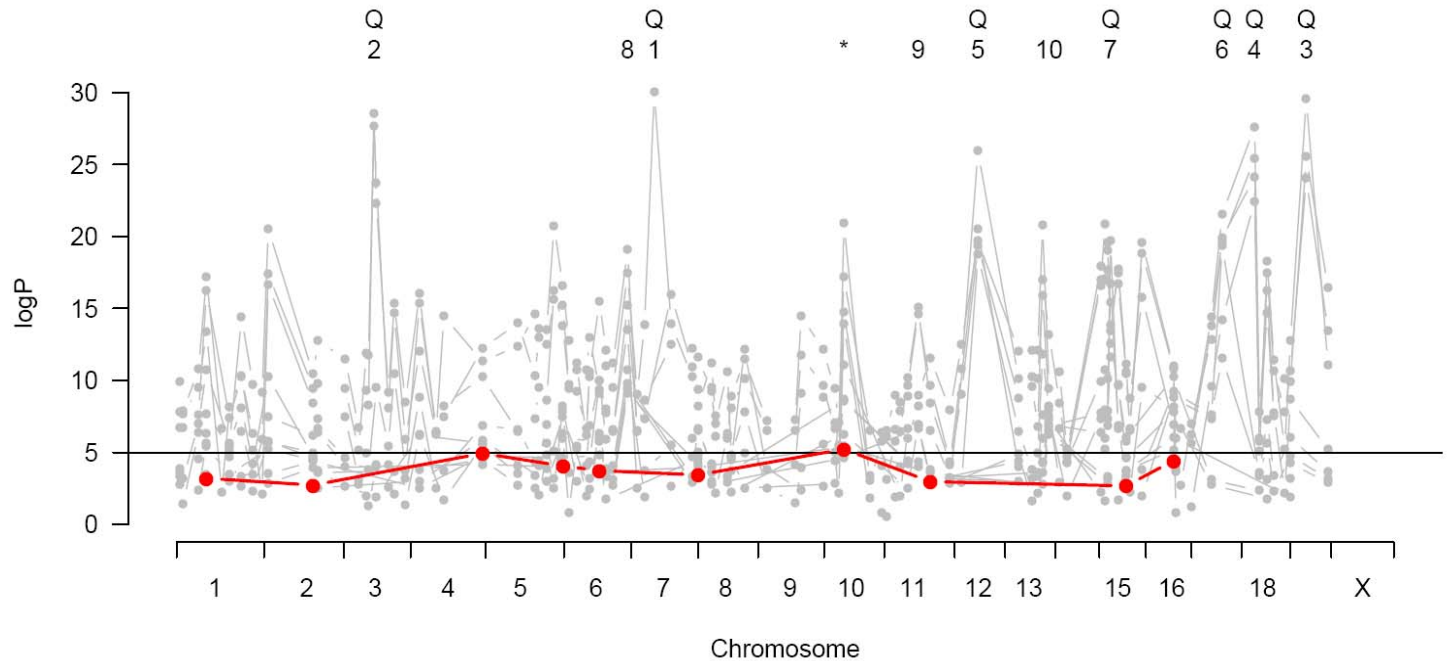
phenotype \sim peak 1 + peak 2 + peak 3 + peak 4 +
peak 5 + peak 6 + peak 7 + peak 8 + ?

condition on 9 peaks



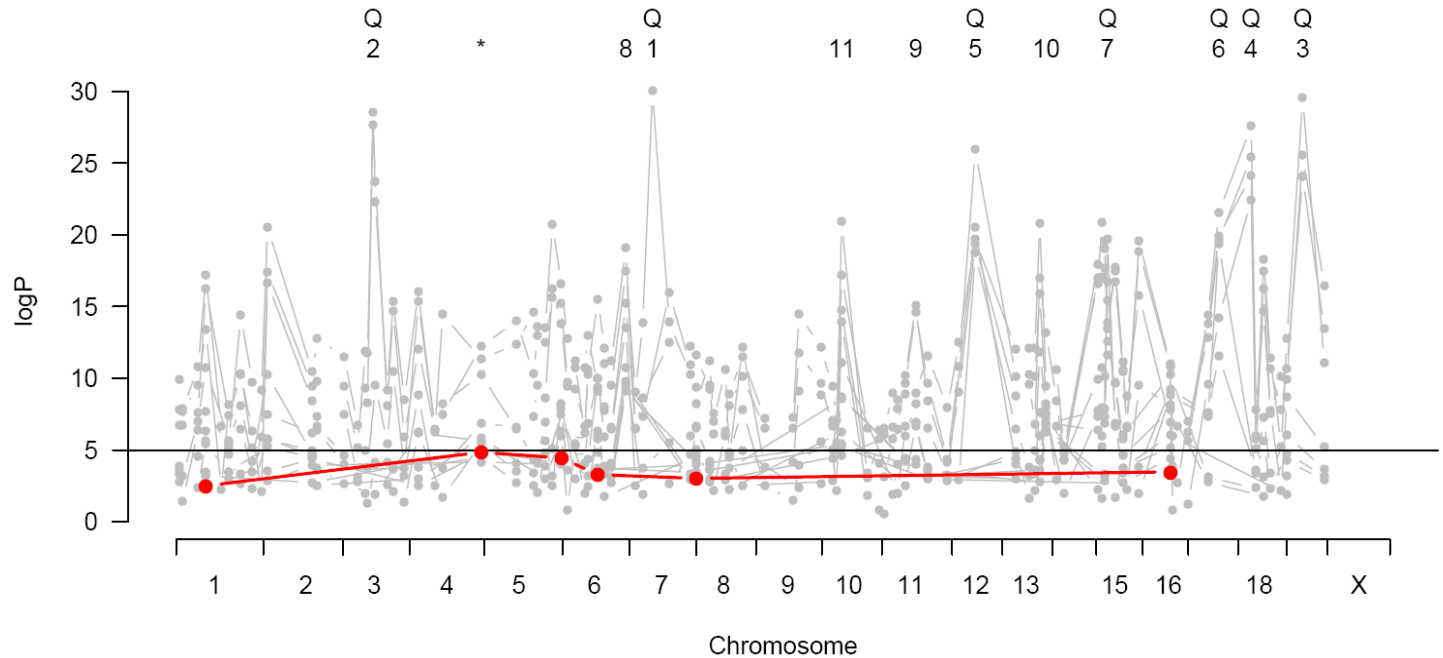
phenotype \sim peak 1 + peak 2 + peak 3 + peak 4 +
peak 5 + peak 6 + peak 7 + peak 8 + peak 9 + ?

condition on 10 peaks



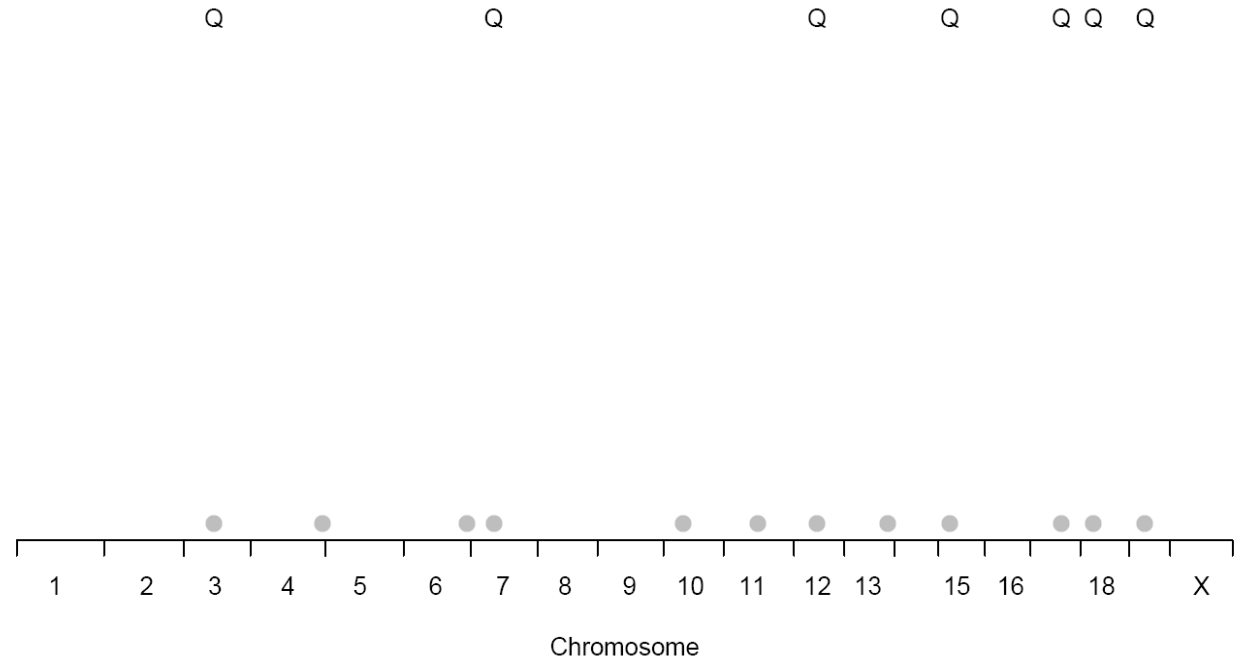
phenotype \sim peak 1 + peak 2 + peak 3 + peak 4 +
peak 5 + peak 6 + peak 7 + peak 8 + peak 9 + peak
10 + ?

condition on 11 peaks



phenotype \sim peak 1 + peak 2 + peak 3 + peak 4 +
peak 5 + peak 6 + peak 7 + peak 8 + peak 9 + peak
10 + peak 11 + ?

Peaks chosen by forward selection



Bootstrap sampling

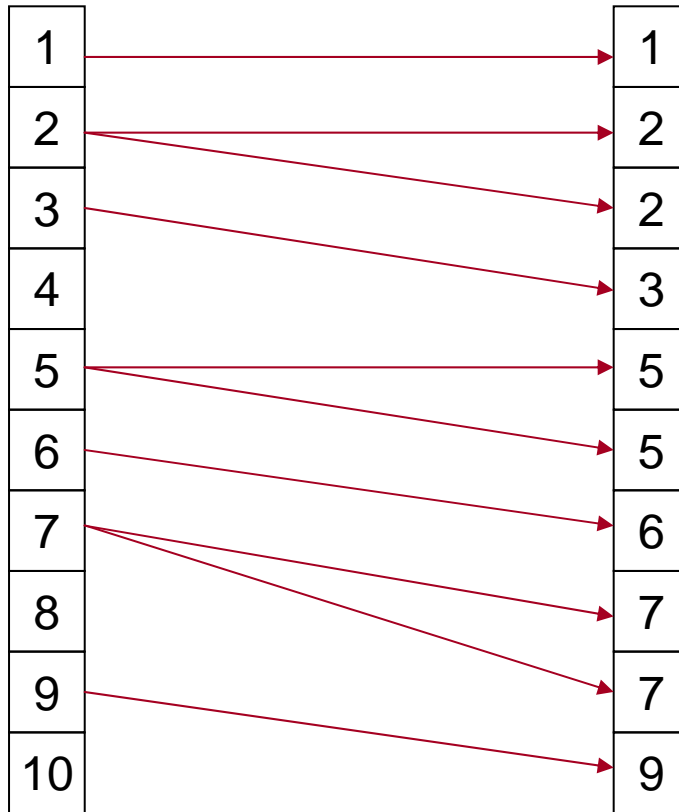
10 subjects

1
2
3
4
5
6
7
8
9
10

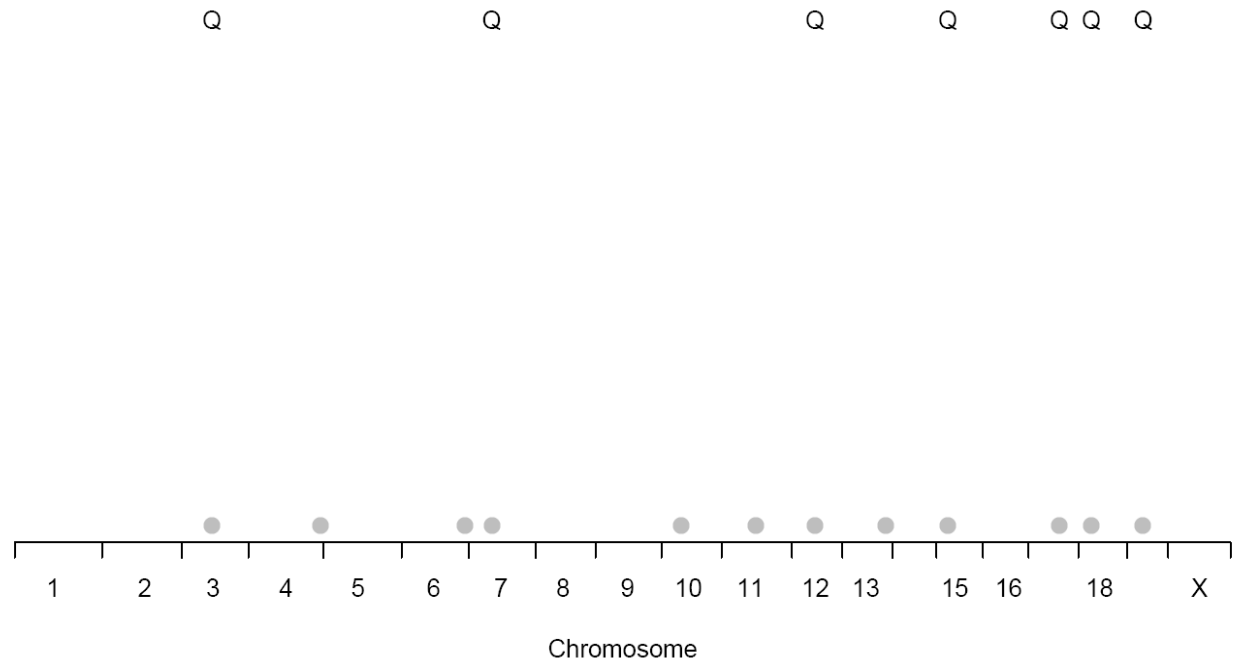
Bootstrap sampling

sample with
replacement

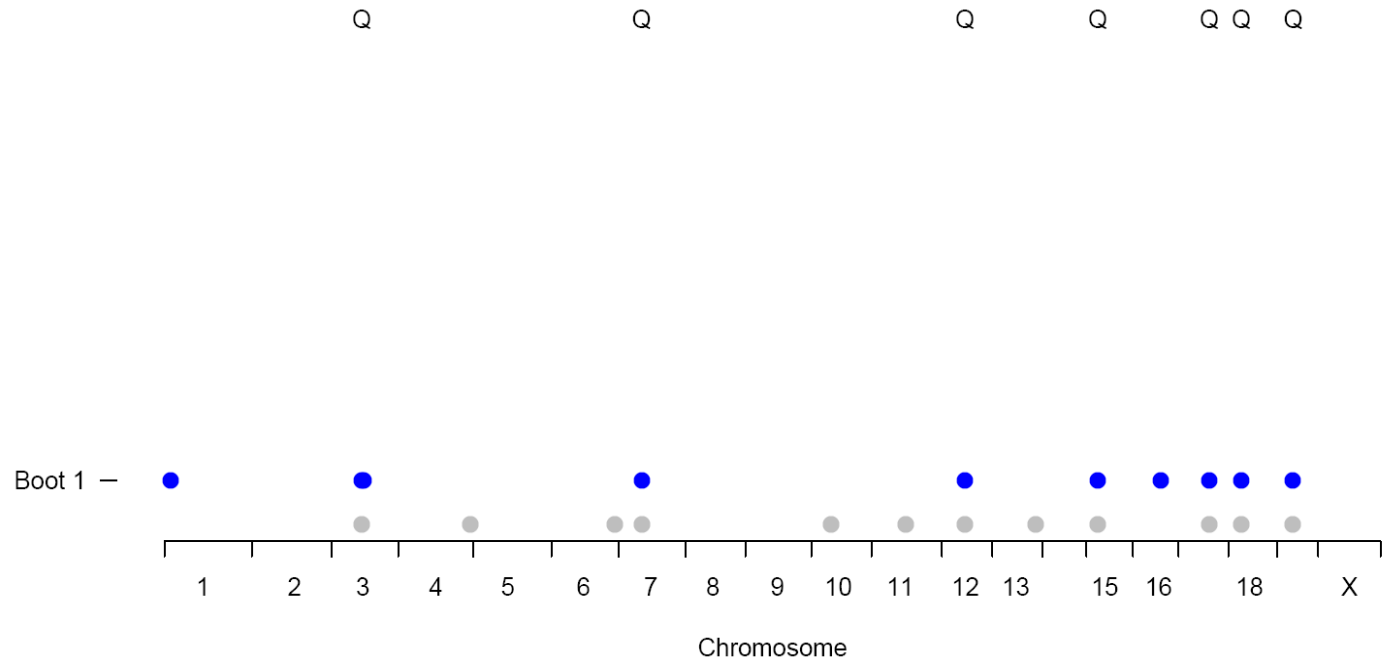
10 subjects



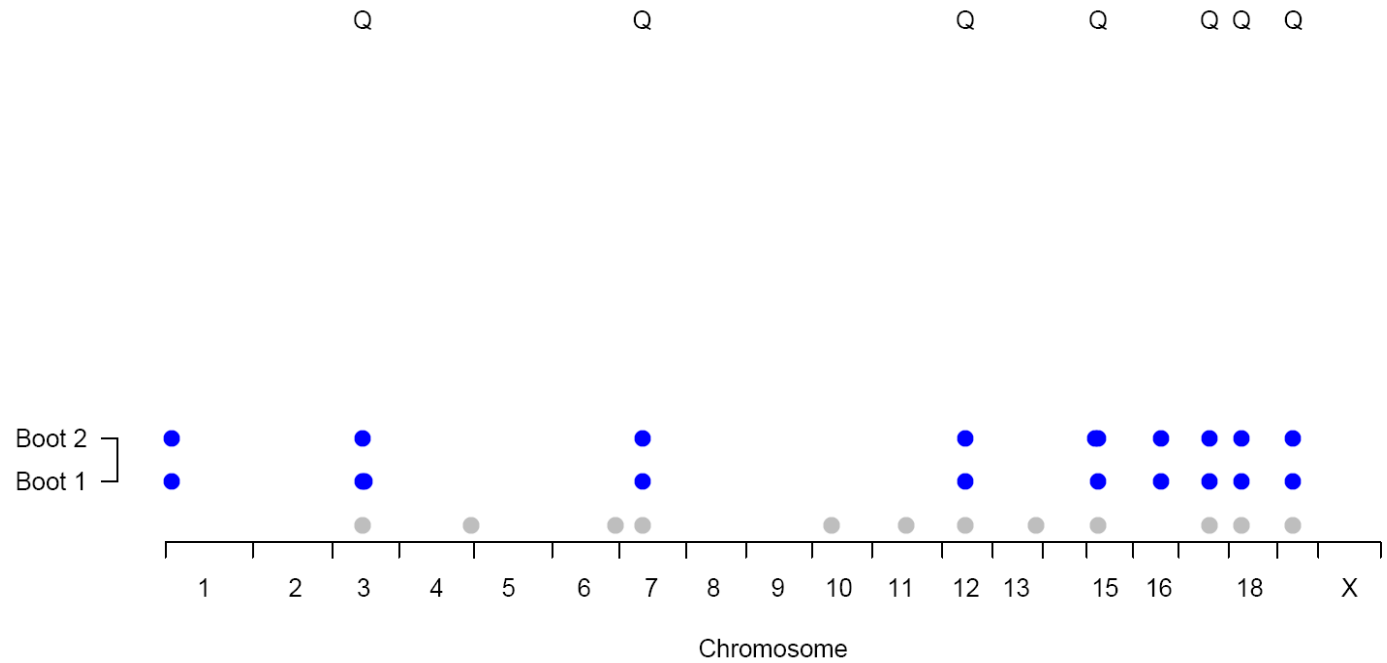
bootstrap sample
from
10 subjects



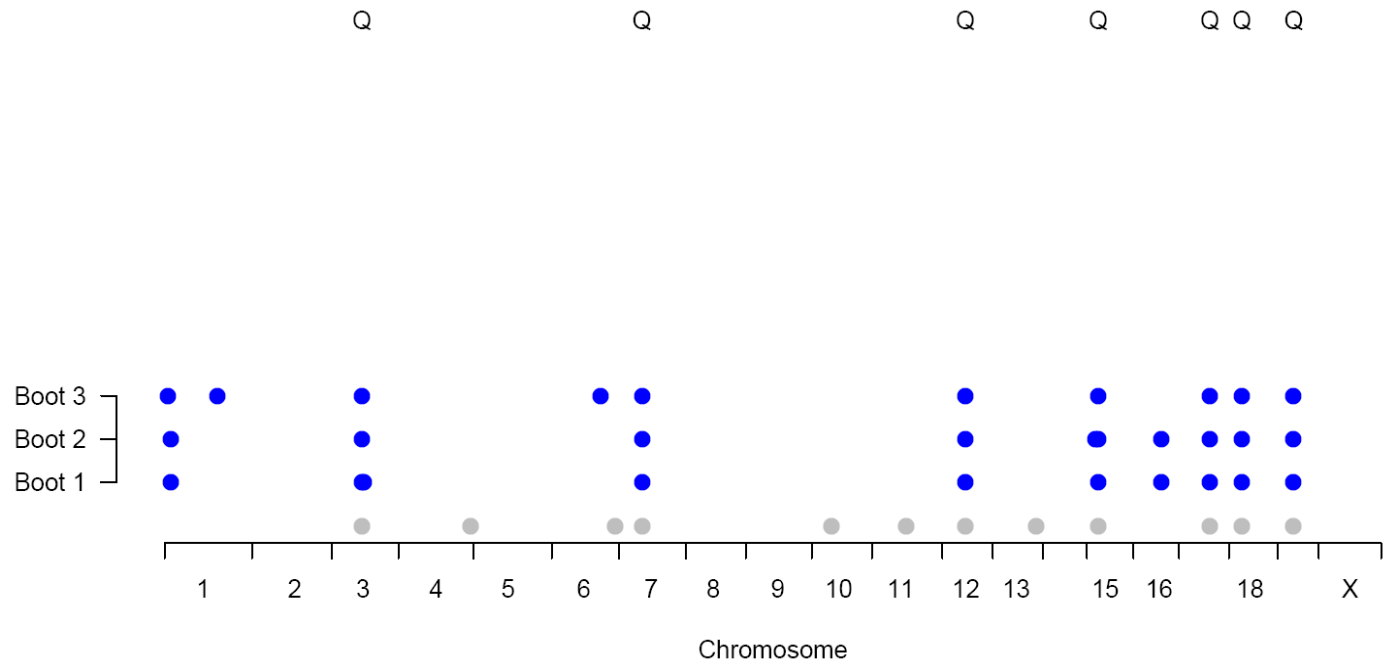
Forward selection on a bootstrap sample



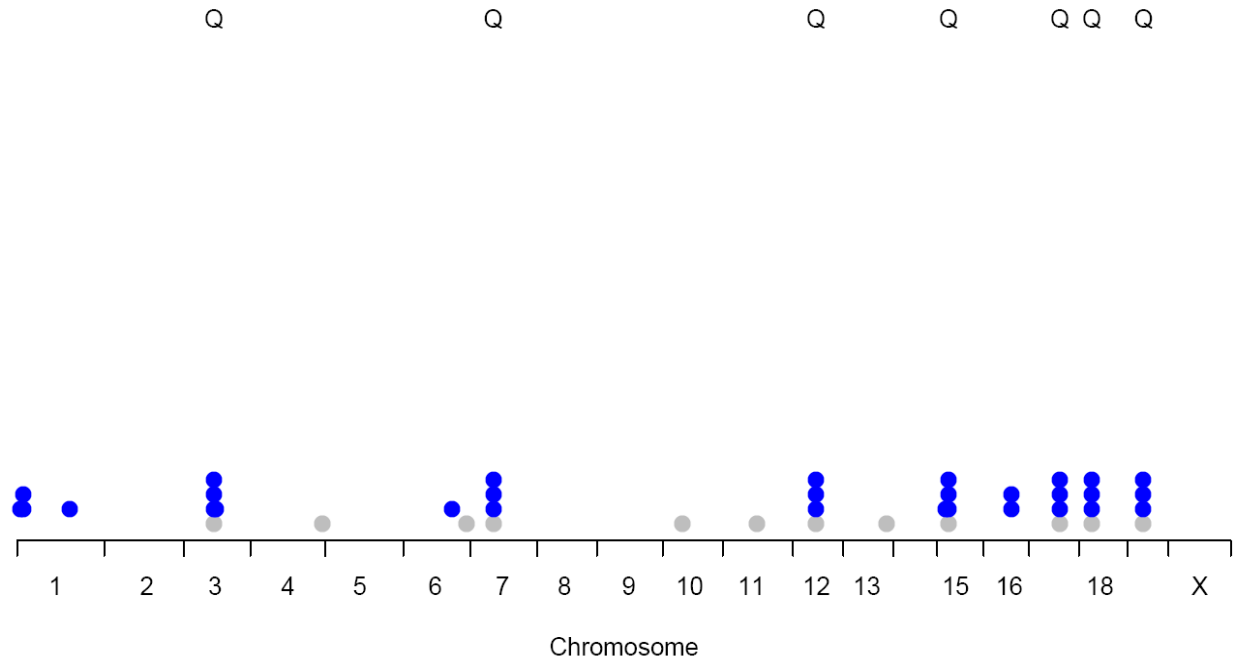
Forward selection on a bootstrap sample



Forward selection on a bootstrap sample

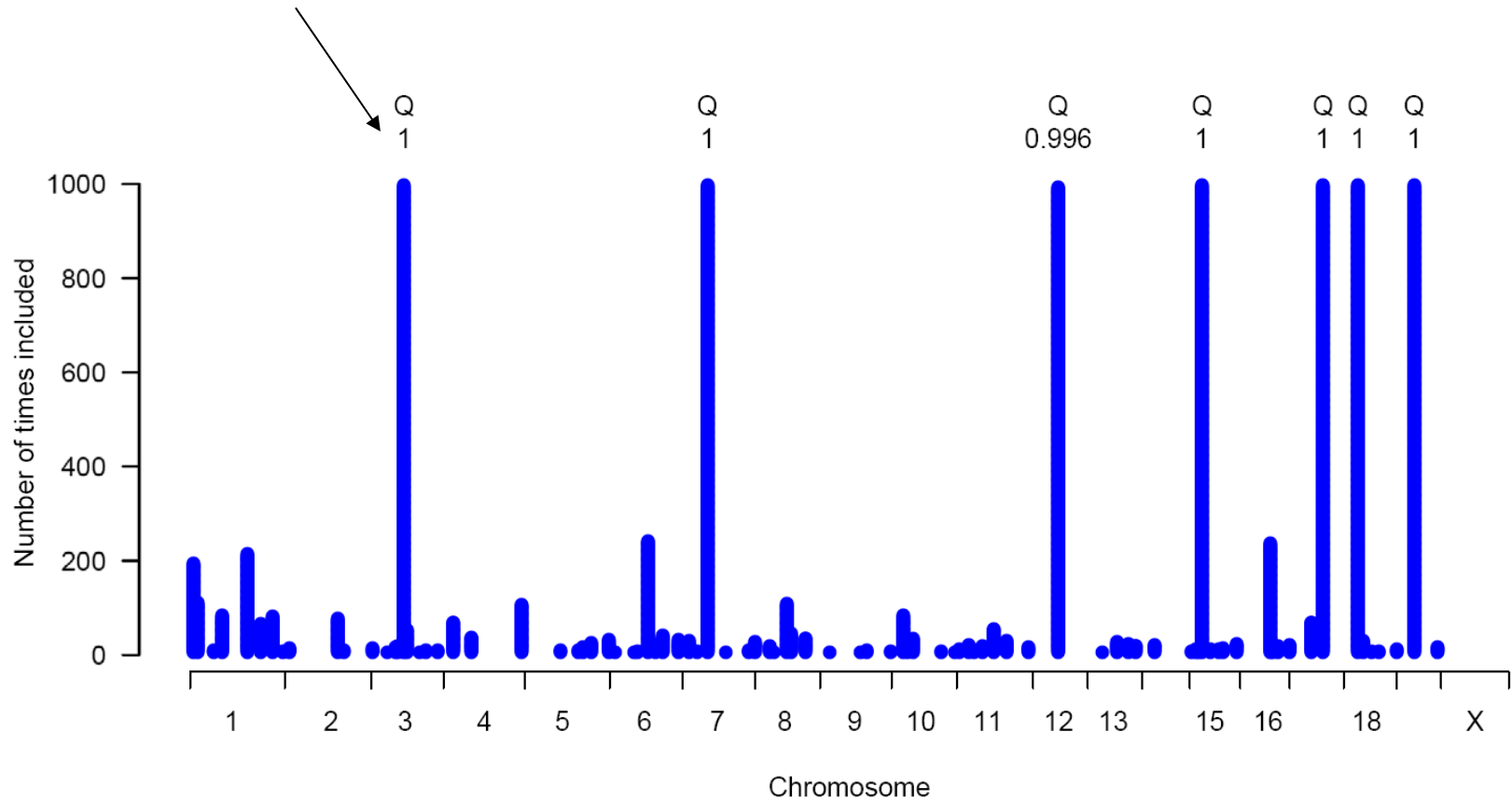


Bootstrap evidence mounts up...

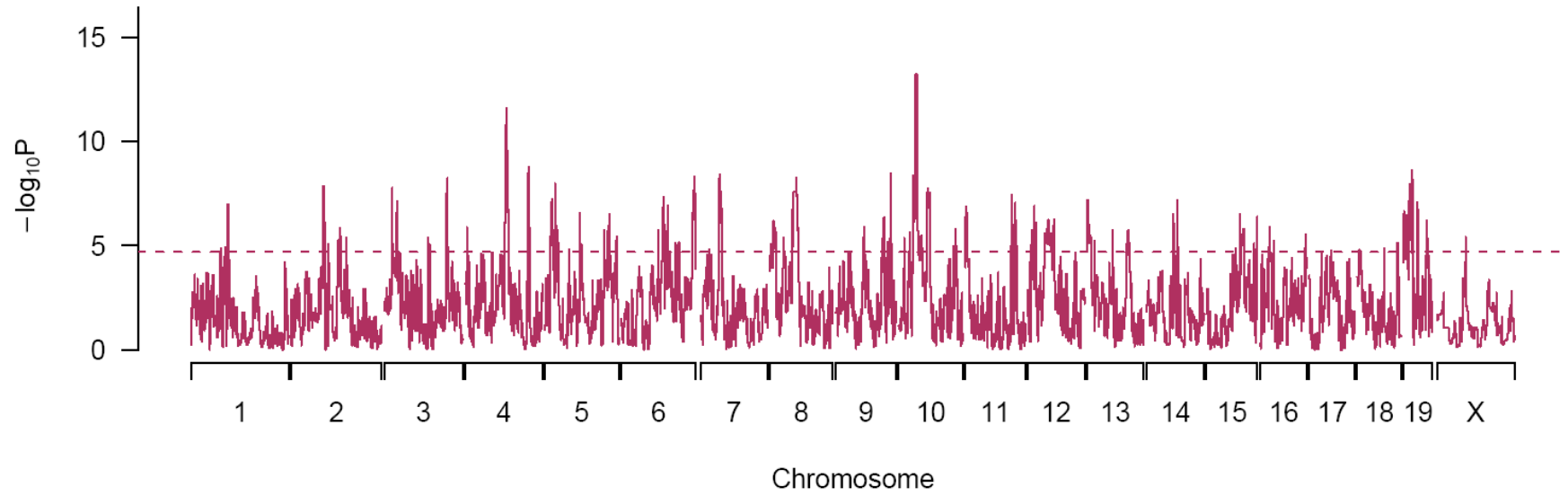


In 1000 bootstraps...

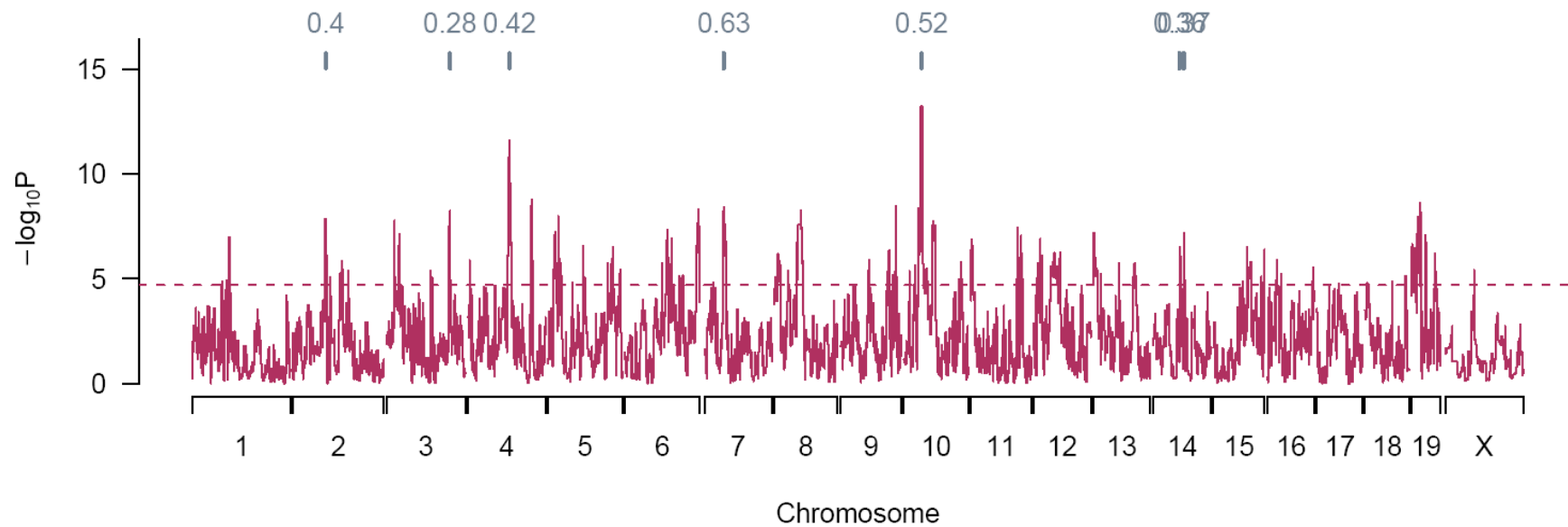
Model Inclusion Probability



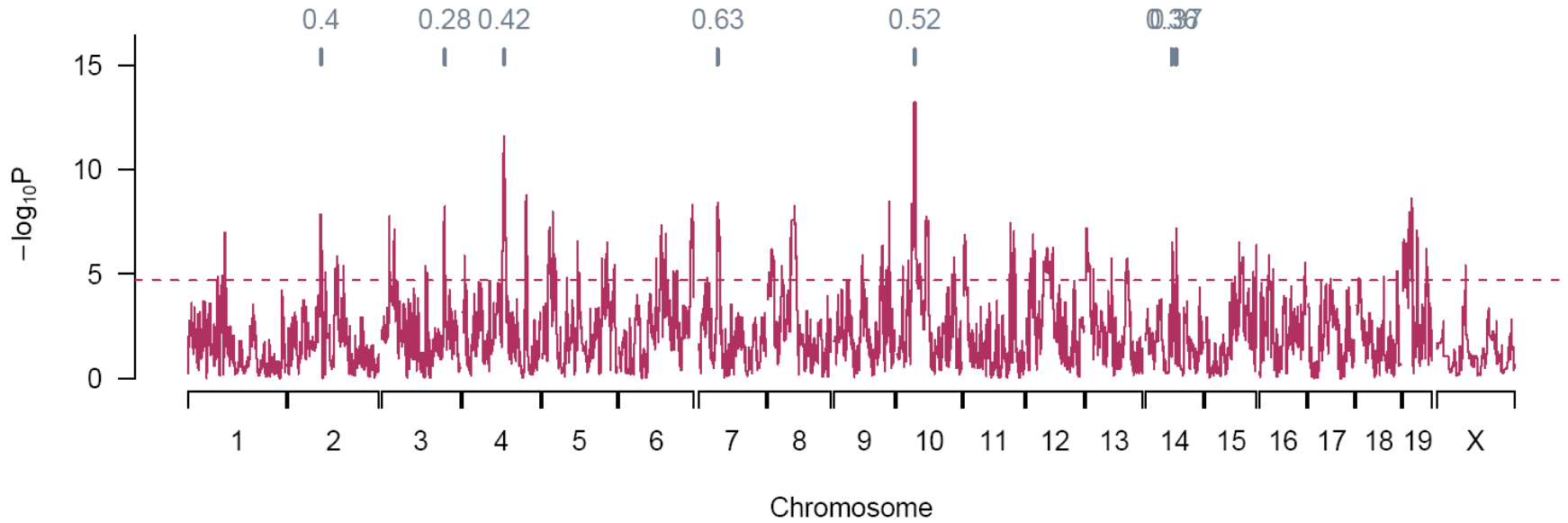
Glucose AUC



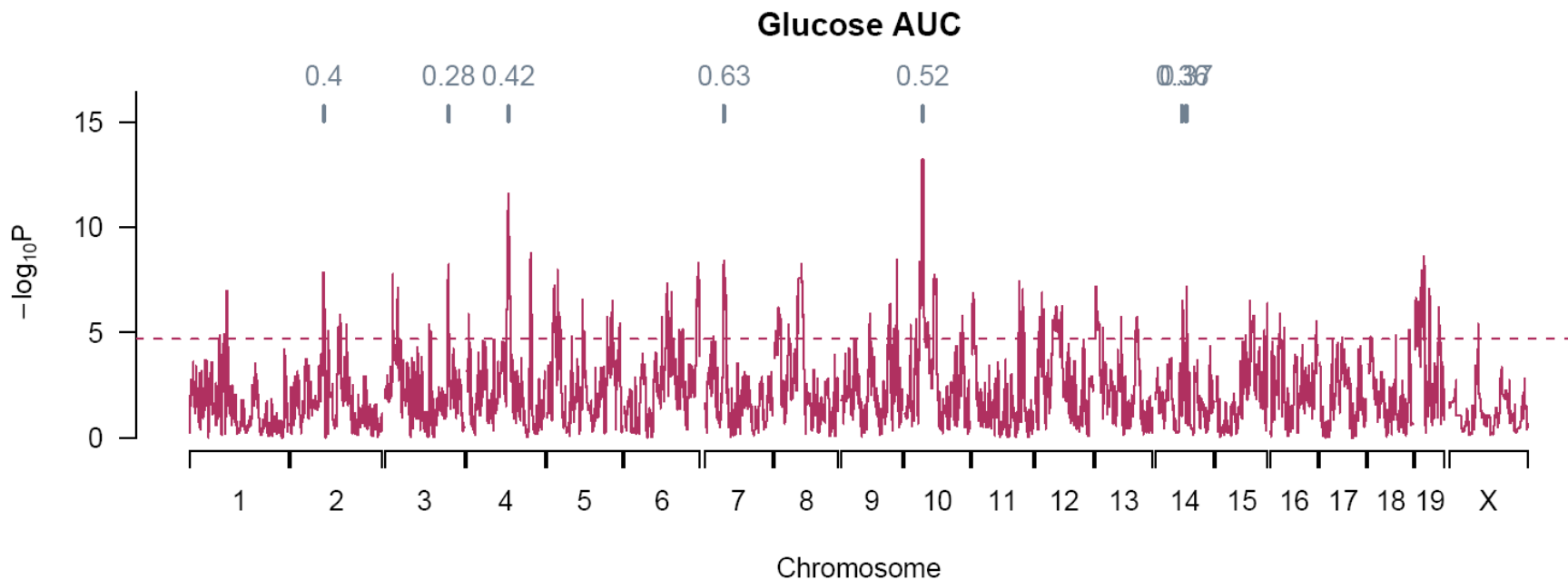
Glucose AUC



Glucose AUC



854 loci in all phenotypes, 84 diabetes loci



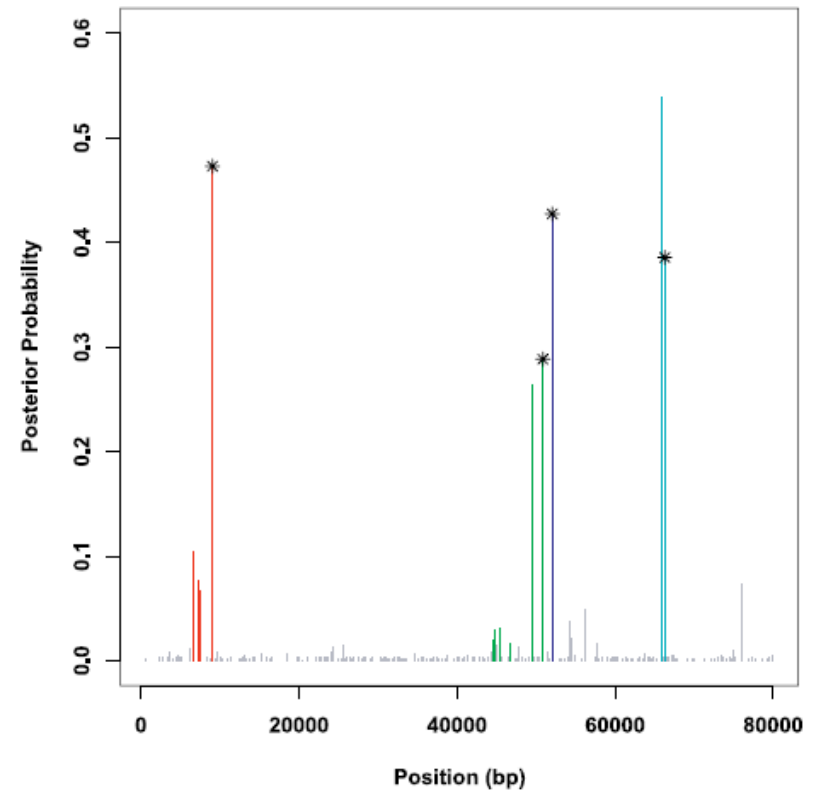
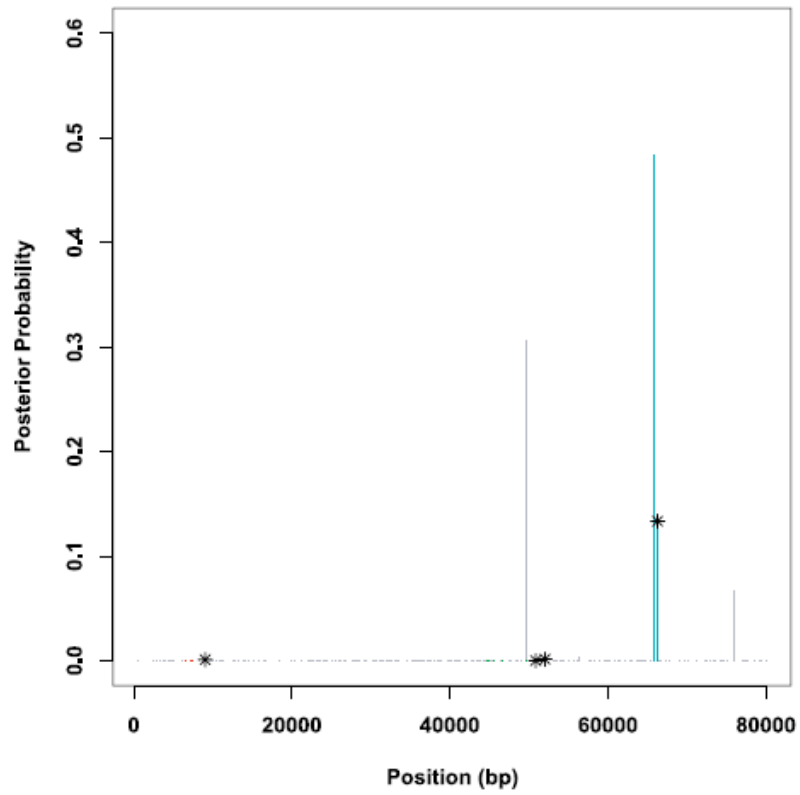
854 loci in all phenotypes, 84 diabetes loci

ARTICLES

nature
genetics

Genome-wide genetic association of complex traits in heterogeneous stock mice

William Valdar¹, Leah C Solberg^{1,4}, Dominique Gauguier¹, Stephanie Burnett¹, Paul Klenerman², William O Cookson¹, Martin S Taylor¹, J Nicholas P Rawlins³, Richard Mott¹ & Jonathan Flint¹



Servin B, Stephens M (2007)

Bayesian Multiple QTL modelling

Kilpikari R, Sillanpaa MJ (2003) Bayesian analysis of multilocus association in quantitative and qualitative traits. *Genet Epidemiol* 25: 122-135

Yi N (2004) A unified Markov chain Monte Carlo framework for mapping multiple quantitative trait loci. *Genetics* 167: 967-975

Servin B, Stephens M (2007) Imputation-based analysis of association studies: candidate regions and quantitative traits. *PLoS Genet* 3: e114

Fridley BL (2008) Bayesian variable and model selection methods for genetic association studies. *Genet Epidemiol*.

The Collaborative Cross

