

1 Coding Categorical Variables

1.1 Why code categorical variables?

Why go to the trouble of coding ANOVA factors? Let us illustrate via example. One of the major neurotrophins, BDNF (brain-derived neurotrophic factor) protects certain types of neurons from cell death. A lab has established that two types of amphetamine can cause cell death in certain types of neurons and is interested in whether BDNF can prevent this. They use microinjections to infuse the targeted brain area in rats with these two different types of amphetamine and a vehicle control. Along with this infusion, they also add four different doses of BDNF—0, 1, 10, and 100 ng per volume. After a suitable time, the rats are sacrificed, their brains dissected, and slices of the region are assessed for neuronal death.

This design can be looked upon as a two way ANOVA. The two factors are type of Drug (with three levels—Control, Amphetamine1, and Amphetamine2) and Dose of BDNF which has four levels. Suppose that the lab has already studied 8 rats per cell and wants to get a preliminary look at the data. Hence, they plot the means (see Figure 1.1) and perform a two-way ANOVA on the data, the results of which are given in Figure 1.2.

The initial plot of the means is very encouraging. The two amphetamine groups have higher cell-death indices than the controls, and there appears to be a linear decrease with the category of BDNF dose. The error bars, however, are quite large.

The results of the ANOVA, however, suggest that the study is not ready for publication. There is a trend towards significance for Drug, but the error bars in Figure 1.2 are too large to get even a meaningful trend for Dose. Faced with such data, the lab decides to test several more rats per cell¹. Given that there are 12 cells in this design, adding just one rat per cells means 12 different surgeries and assays. Ask yourself, how much time might it take to add just one rat per cell?

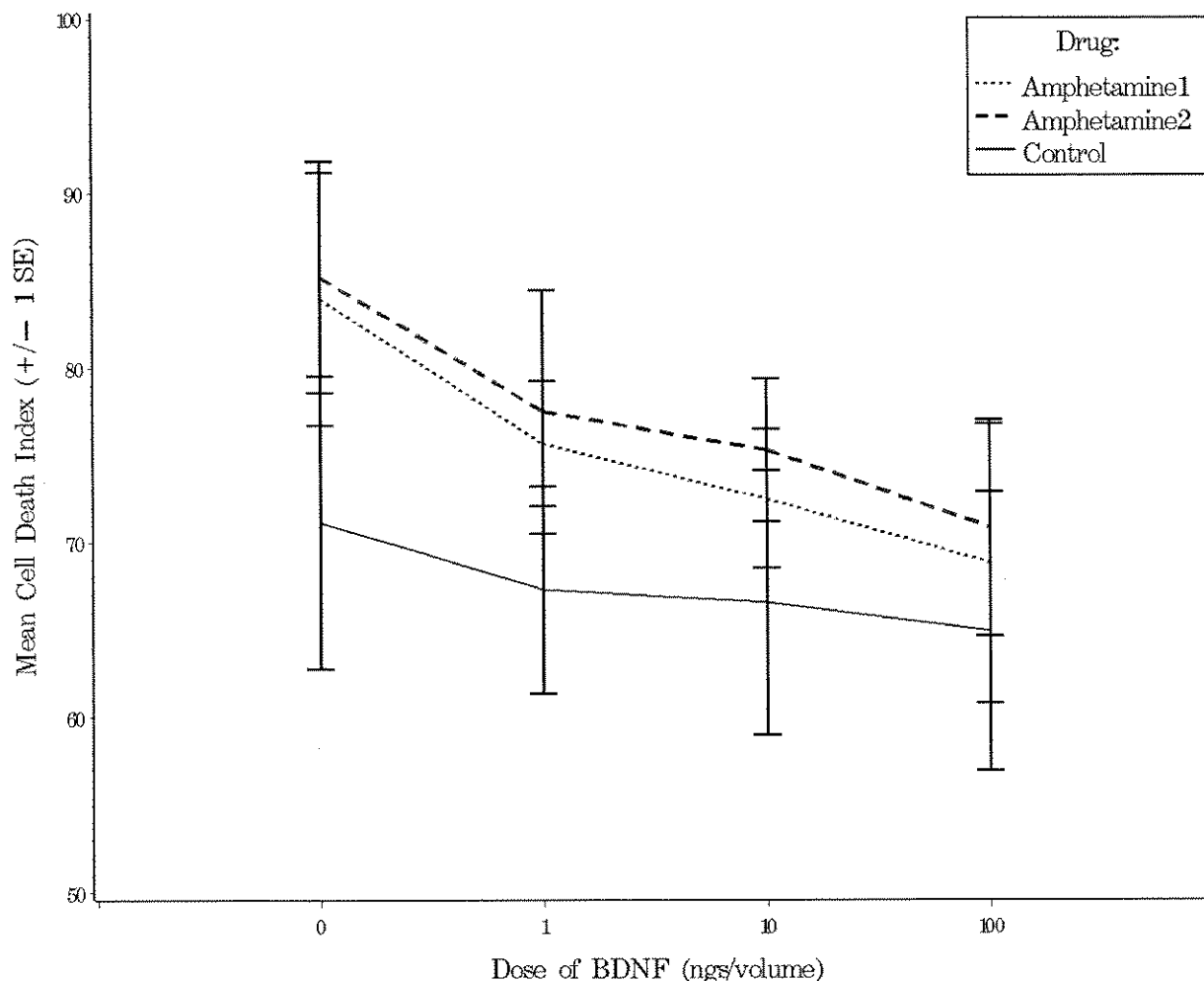
The importance of coding is that this extra effort might be wasted time. Let us explore this issue for a minute by recalling the purpose of the study. The lab has already established that both types of amphetamine produce cell death. Hence, they know that both amphetamine groups will differ from controls. This knowledge can be used to construct an independent variable for the analysis that effectively tests whether the average of the two means for the amphetamine groups differs from the control mean². (We outline the mechanics of how to do this later in Section X.X. Right now, we only want to convince you to read that.)

Let us call this new independent variable “Contrast1” because the coding scheme is called *contrast coding*. We will also construct a second new independent variable, called “Contrast2,” that tests whether the means of the two amphetamine group differ from each other. We now rerun the analysis treating Contrast1 and Contrast2 as continuous variables. The results of this GLM are given in Figure 1.3.

¹ The proper statistical course of action is to do an a posteriori power analysis (a topic discussed later in Section X.X) to determine the desired sample size.

² The means referred to here are the marginal means for the Control and the two amphetamine groups.

Figure 1.1 Mean (\pm 1 SEM) cell death index for as a function of type of drug and dose of BDNF.



Now, variable Contrast1 is significant. This implies that the average of the two amphetamine means depicted in Figure 1.1 differs significantly from the Control mean. Contrast2, however, is not significant. Hence, there is no evidence that the mean for Amphetamine1 differs from that for Amphetamine2.

Before discussing the reason for this, compare the omnibus F statistic, its p value, and the R^2 of the classic ANOVA (Figure 1.2) to those statistics from the GLM using the two contrast coded variables (Figure 1.3). The two sets of statistics are identical. Now compare the SS , MS , F , and p for variable Dose in the two Figures. These statistics are also identical. Now, add together the SS for Contrast1 and Contrast2 in Figure 1.3 and compare the result to the SS for Drug in the classic ANOVA. They are the same number. Finally, add the SS for the Contrast1*Dose interaction to the SS for the Contrast2*Dose interaction in Figure 1.3. Compare this result to the SS for the Drug*Dose interaction in Figure 1.2. Once again, they are the same.

Figure 1.2 Classic ANOVA results on BDNF data set.

Dependent Variable: Cell_Death						
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F	
Model	11	3724.49500	338.59045	0.98	0.4729	
Error	84	29084.42500	346.24315			
Corrected Total	95	32808.92000				
R-Square	Coeff Var	Root MSE	Cell_Death Mean			
0.113521	25.37690	18.60761	73.32500			
Source	DF	Type III SS	Mean Square	F Value	Pr > F	
Drug	2	1689.135625	844.567812	2.44	0.0934	
Dose	3	1823.155000	607.718333	1.76	0.1620	
Drug*Dose	6	212.204375	35.367396	0.10	0.9960	

Figure 1.3 GLM results using contrast codes on the BDNF data set.

Dependent Variable: Cell_Death						
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F	
Model	11	3724.49500	338.59045	0.98	0.4729	
Error	84	29084.42500	346.24315			
Corrected Total	95	32808.92000				
R-Square	Coeff Var	Root MSE	Cell_Death Mean			
0.113521	25.37690	18.60761	73.32500			
Source	DF	Type III SS	Mean Square	F Value	Pr > F	
Contrast1	1	1626.922969	1626.922969	4.70	0.0330	
Contrast2	1	62.212656	62.212656	0.18	0.6727	
Dose	3	1823.155000	607.718333	1.76	0.1620	
Contrast1*Dose	3	207.377656	69.125885	0.20	0.8964	
Contrast2*Dose	3	4.826719	1.608906	0.00	0.9996	

This similarity is far from coincidental. The contrast coding is actually performing the same ANOVA in Figure 1.2—it is just expressing the hypotheses in a different form, one that both increases statistical power and provides more information about group differences. Recall the logic of ANOVA. In the classic ANOVA, the null hypothesis states that the means for all three groups are sampled from the same hat of means. The alternative hypothesis, however,

encompasses two different situations. Alternative hypothesis 1 is that each of the three means is sampled from a different hat of means. Alternative hypothesis 2 states that one mean is sampled from one hat of means, but the other two means come out of another hat of means. This hypothesis, however, comes in three forms: (2a) the Control mean comes from one hat and the two amphetamine means from the other hat; (2b) the Amphetamine1 mean comes from one hat and the Control and Amphetamine2 mean from the second hat; and (2c) the Amphetamine2 mean is from the first hat and the Control and Amphetamine1 means from the second hat.

In a very loose sense, the F test for Drug in the classic ANOVA has no clue as to the relative likelihood of alternative hypothesis 1 and the three forms of alternative hypothesis 2. Hence, this statistic tries to test something akin to the “average” of these four alternative hypotheses. In developing the coding scheme, we capitalized on the prior results of this lab by suspecting that if any mean is sampled from a different hat, it will most likely be the Control mean. Hence, we considered alternative hypotheses 2b and 2c as unlikely and developed the coding scheme to examine the relative merits of alternative hypothesis 1 versus alternative hypothesis 2a. The result was a significant increase in statistical power.

Before moving on, note that both the classic ANOVA and the GLM with contrast codes treated variable Dose as if it were truly categorical. Figure 1.4 illustrates the effect of using the quantitative information in Dose by treating it as a continuous variable. The actual variable was $\text{Log}_{10}(\text{Dose} + 1)$.

Figure 1.4 GLM results using contrast codes and a quantitative variable for dose of BDNF.

Dependent Variable: Cell_Death					
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	5	3352.20203	670.44041	2.05	0.0793
Error	90	29456.71797	327.29687		
Corrected Total	95	32808.92000			
R-Square	Coeff Var	Root MSE	Cell_Death Mean		
0.102173	24.67282	18.09135	73.32500		
Parameter		Estimate	Standard Error	t Value	Pr > t
Intercept		77.57618720	2.720302	28.52	<.0001
Contrast1		-3.95676243	1.923544	-2.06	0.0426
Contrast2		-0.82375000	3.331676	-0.25	0.8053
Log10_Dose		-5.08098274	2.387603	-2.13	0.0361
Contrast1*Log10_Dose		1.24996105	1.688291	0.74	0.4610
Contrast2*Log10_Dose		-0.19384512	2.924205	-0.07	0.9473

Now both Contrast1 and the dose of BDNF are significant. Despite the large error bars in Figure 1.1, the analysis now suggests that the results are “publishable.” The time spent pointing and clicking in a modern statistical package to get these results is trivial—about a minute. How

much time do you think it would take to add animals to achieve statistical significance using the classic ANOVA?

1.2 Methods of Coding

1.2.1 Coding According to a Mathematical Model

Sometimes existing mathematical model that can be used to code groups. Consider the protein kinase C- γ (PKC- γ) data given previously in Section X.X. To recap, this data set involved mice that are genetically identical save for their genotypes at the PKC- γ locus. Genotype ++ is the homozygote for the wild-type allele, genotype +- is heterozygote with one wild-type allele and one knockout allele, and genotype -- is homozygous for two knockout alleles. The dependent variable is percentage of time spent in the open arm of an elevated plus-maze. Low scores on this variable are assumed to be associated with high levels of anxiety.

There is a standard model for quantitative data on a single genetic locus. Figure 1.5 presents this model using the notation of Falconer (19xx). Here m is the mathematical midpoint between the means of the two homozygotes. Parameter a gives the distance between the midpoint and means of the two homozygotes. Hence, the mean of the A_1A_1 homozygote equals $m - a$ and the mean of the A_2A_2 homozygote is $m + a$. Parameter d gives the distance of the heterozygote from the midpoint, so mean for this genotype is $m + d$.

Figure 1.5 A model for the analysis of a quantitative phenotype for a genetic locus with two alleles, A_1 and A_2 .

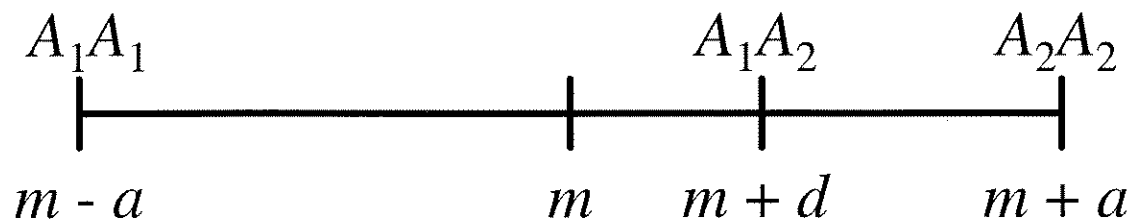


Table 1.1 gives the genetic model along with a coding scheme for two independent variables— X_1 and X_2 —derived from the genetic model. The overall equation to predict the mean of the i th genotype is

$$\bar{Y}_i = \alpha + \beta_1 X_{i1} + \beta_2 X_{i2}.$$

Read this equation as “the mean for the i th genotype (\bar{Y}_i) equals a constant (α) plus the slope of the first independent variable (β_1) times the value of the i th genotype on the first independent variable (X_{i1}) plus the slope for the second independent variable (β_2) times the value of the i th genotype on the second independent variable (X_{i2}).”

Table 1.1

Genotype:	Genetic Model:	Coded Independent Variables:		Regression Model:
		X_1	X_2	
++	$m - a$	-1	0	$\alpha - \beta_1$
+-	$m + d$	0	1	$\alpha + \beta_2$
--	$m + a$	1	0	$\alpha + \beta_1$

The mean for a given genotype may be found by substituting the values of the two coded independent variables for that genotype into this equation. For example, the mean for genotype ++ is

$$\bar{Y}_{++} = \alpha + \beta_1(-1) + \beta_2(0) = \alpha - \beta_1.$$

Continuing with this logic gives the genotypic means under the column in Table 1.1 labeled “Regression Model.” Comparing this column to the one for the genetic model, we see that the intercept α estimates the genetic parameter m , the regression coefficient β_1 estimates the genetic parameter a , and the regression coefficient β_2 estimates the genetic parameter d .

1.2.2 Dummy Coding

Dummy codes assign numbers of 0 or 1 to groups. When there are k groups (or, more technically, k levels to an ANOVA factor), then there can be as many as $(k - 1)$ dummy codes. In a regression using dummy-coded independent variables, the intercept gives the mean for one group (called the *reference group* herein) and the slope for a dummy-coded group gives the difference in the means of the reference group and the group given a code of 1.

To examine this statement, plug the dummy code scheme into the following equation for each group

$$\bar{Y}_i = \alpha + \beta_1 X_{1i} + \beta_2 X_{2i} + \dots + \beta_k X_{ki}. \quad (\text{X.1})$$

Here \bar{Y}_i equals the mean on the dependent variable for the i^{th} group and X_{ji} is the value of the j^{th} dummy code for the i^{th} group. An example can illustrate this principle without all those confusing i^{th} s and j^{th} s.

In the example given above, there are three genotypes, so the analysis has three groups (i.e., $k = 3$). Hence, we can construct up to 2 dummy code variables. When the groups have a rank order to them—as they do in the case of genotypes—then one informative dummy coding system is to let the *second* group equal 1 on the *first* dummy code, the *third* group equal 1 on the *second* dummy code, the *fourth* equal 1 on the *third* dummy code, and so on. The reference group in this case will be the first group.

We apply this scheme by letting genotype ++ be the reference group. Let X_1 denote the first dummy code for the genotypes. We will set X_1 to 1 for genotype +-; otherwise X_1 will equal 0. Let X_2 denote the second dummy code. Here, $X_2 = 1$ if the genotype is --; otherwise, $X_2 = 0$.

Using Equation (X.1), the mean for the ++ or reference genotype will equal

$$\bar{Y}_{++} = \alpha + \beta_1 0 + \beta_2 0 = \alpha.$$

Hence, the intercept in the regression output will equal the mean of the ++ genotypes.

The mean for genotype +- may be found by plugging its values on X_1 and X_2 into Equation (X.1). The result is

$$\bar{Y}_{+-} = \alpha + \beta_1 1 + \beta_2 0 = \alpha + \beta_1.$$

Because α equals the mean for genotype ++, we can substitute that mean into the above equation in place of α and solve for β_1 ,

$$\bar{Y}_{+-} = \alpha + \beta_1 = \bar{Y}_{++} + \beta_1,$$

so

$$\beta_1 = \bar{Y}_{+-} - \bar{Y}_{++}.$$

In short, the regression coefficient β_1 equals the difference in means between genotype +- and wild type genotype ++. If β_1 is statistically different from 0, then there is a significant difference between the mean for the heterozygote and the ++ homozygote.

Finally, the equation for the mean for genotype -- will be

$$\bar{Y}_{--} = \alpha + \beta_1 0 + \beta_2 1 = \alpha + \beta_2.$$

Without reproducing the algebra,

$$\beta_2 = \bar{Y}_{--} - \bar{Y}_{++}.$$

If β_2 is significant, then the difference in means between the two homozygotes is significant.

Clearly, dummy coding is a useful scheme when one level of a factor is a control. By letting the control level be the reference level, the dummy coded variables effectively test the mean difference between any other level of the factor and the control level. In the PKC-gamma example, by letting the wild type, ++ genotype be the “control,” then parameter β_1 tests the effect of knocking out one pkc-gamma allele and β_2 tests the effect of knocking out both alleles.

1.2.3 Contrast Coding

Contrast coding creates a new variable by assigning numeric weights (denoted here as w) to the levels of an ANOVA factor under the constraint that the sum of the weights equals 0, or

$$\sum_{i=1}^k w_i = 0. \quad (\text{X.X})$$

Later, we consider how to develop two or more contrast coded variables, but for the moment, let us simply consider the three weights that can be used in the present example to create a single contrast-coded variable.

As in dummy coding, the meaning of any contrast coded variable is expressed in terms of the group means. Hence selection of the numbers assigned to the levels of the ANOVA factor should reflect meaningful comparisons of group means. For an ANOVA factor with k levels, the overall null hypothesis tested by a contrast is

$$\sum_{i=1}^k w_i \bar{Y}_i = w_1 \bar{Y}_1 + w_2 \bar{Y}_2 + \dots + w_k \bar{Y}_k = 0, \quad (\text{X.X})$$

where, as before, \bar{Y}_i denotes the mean on the dependent variable for the i th level of the ANOVA factor. The alternative hypothesis is that the weighted sum of the means is not equal to 0.

To understand contrast coding, it is helpful to have a numerical example. Table 1.2 presents the sample sizes, means, and standard deviations for the three PKC-gamma genotypes. We use these data below.

Table 1.2 Descriptive statistics for the PKC-gamma data set.

Genotype:	N	Mean	St. Dev.
++	15	8.62	6.40
+-	15	8.66	6.03
--	15	19.39	9.03

Table 1.3 gives five examples of contrast codes that could be used for the PKC-gamma genotypes. All five of these codes meet the mathematical necessity that the weights sum to 0. To derive null hypothesis tested by a contrast coded variable, do the following three algebraic steps: (1) multiply each group mean by its coefficient; (2) add the terms together; and (3) equate the sum to 0. For example, for the first set of contrast codes in Table 1.3, we have

$$0 = -1\bar{Y}_{++} + 1\bar{Y}_{+-} + 0\bar{Y}_{--} = \bar{Y}_{+-} - \bar{Y}_{++},$$

so this contrast code tests for the difference in means between the heterozygote and the wild type homozygote. In terms of the numeric values of the means, this code tests whether

$$0 = 8.66 - 8.62 = .04.$$

Of course, the number 0 is not equal to the number .04. Instead, the test is whether the observed difference in means (.04) is within *sampling error* of 0.

Table 1.3 Example contrast codes for the three levels of PKC-gamma genotype.

Example:	Genotype:		
	++	+-	--
1	-1	1	0
2	1	0	-1
3	2	-1	-1
4	0	1	-1
5	-1	2	-1

For example 2 in Table 1.3, the equation is

$$0 = 1\bar{Y}_{++} + 0\bar{Y}_{+-} + 1\bar{Y}_{--} = \bar{Y}_{++} - \bar{Y}_{--},$$

and it tests for the difference in means between the two homozygotes. Specifically, it assesses the null hypothesis that $0 = 8.62 - 19.39 = -10.77$. In substantive terms, this code asks whether a difference in means of -10.77 units is significantly different from 0.

Example 3 gives

$$0 = 2\bar{Y}_{++} - 1\bar{Y}_{+-} - 1\bar{Y}_{--} = \bar{Y}_{++} - \frac{\bar{Y}_{+-} + \bar{Y}_{--}}{2}.$$

This tests whether the mean of the wild type homozygotes differs from the average of the heterozygote and the knockout homozygote means. Numerically, this is equivalent to

$$0 = 8.62 - \frac{8.66 + 19.39}{2} = -5.405.$$

Example 4 gives

$$0 = \bar{Y}_{+-} - \bar{Y}_{--},$$

the difference between the heterozygote and the knockout homozygote means. Example 5, giving

$$0 = \bar{Y}_{+-} - \frac{\bar{Y}_{++} + \bar{Y}_{--}}{2},$$

tests whether the heterozygote differs from the average of the homozygote means (i.e., a test for genetic dominance).

Many other codes meet the mathematical requirement that the weights sum to 0 but do not give meaningful comparison of the genotypic means. We could, for instance, assign the weight -5 to genotype $++$, -12 to genotype $+-$, and 17 to genotype $--$. The resulting null hypothesis, however, is

$$0 = -5\bar{Y}_{++} - 12\bar{Y}_{+-} + 17\bar{Y}_{--}.$$

This null hypothesis makes little sense. Clearly, substantive issues must prevail over mathematical ones in developing contrast codes.

1.2.3.1 Contrast Codes: Comparison to a Control Group

An investigator who spends time and resources gathering experimental data rarely is completely atheoretical about the anticipated mean differences between the control and the treatment (i.e., experimental) groups. The omnibus F statistic from a classic ANOVA, however, is completely atheoretical about mean differences. Hence, one of the most important uses of contrast coding is to compare the means of treatment groups to those of one or more control groups.

Let us first examine the simplest case—i.e., when the means of all treatment groups are expected to be uniformly higher or uniformly lower than the control group mean. With k total groups, and one control group, there will be $(k - 1)$ treatment groups. In this case, assign the numeric value of $(k - 1)$ to the control group and values of -1 to the treatment groups. The resulting contrast coded variable tests the hypothesis that

$$(k - 1)\bar{Y}_C - \bar{Y}_1 - \bar{Y}_2 - \dots - \bar{Y}_{k-1} = 0,$$

where \bar{Y}_C is the control mean and \bar{Y}_i is the mean of the i th treatment group. Substantively, this hypothesis tests whether the control mean differs significantly from the average of all treatment means. How? Divide this equation by $(k - 1)$:

$$\bar{Y}_C - \frac{\bar{Y}_1 + \bar{Y}_2 + \dots + \bar{Y}_{k-1}}{(k - 1)} = 0.$$

The equation now reads “the control mean minus the average of the $(k - 1)$ treatment means equals 0.” (Note that we could have assigned the value of 1 to the control mean and the value of $-1/(k - 1)$ to each of the treatment means and achieved the same result. It is usually easier, however, to use integers for contrast codes.)

In the two SSRI data sets, there was no control group (i.e., a group that was not pretreated with an SSRI) because the object of the study was to compare differences among the four SSRIs. If, however, a control group were present, one would contrast code the ANOVA factor by assigning a value of 4 to the controls and a value of -1 to each of the four SSRI groups. The resulting hypothesis to be tested would be

$$4\bar{Y}_C - \bar{Y}_{SSRI1} - \bar{Y}_{SSRI2} - \bar{Y}_{SSRI3} - \bar{Y}_{SSRI4} = 0.$$

Dividing this equation by 4 illustrates how the null hypothesis states that the control mean less the average of the four experimental means equals 0:

$$\bar{Y}_C - \frac{\bar{Y}_{SSR1} + \bar{Y}_{SSR2} + \bar{Y}_{SSR3} + \bar{Y}_{SSR4}}{4} = 0.$$

1.2.3.2 Contrast Coding: A second contrast-coded independent variable.

Let us turn attention to contrast coding a second independent variable from the same ANOVA factor. Again, substantive considerations as to which means should be compared should be the primary guide to construction of the codes. Mathematically, however, a second contrast code may be either *orthogonal* or *nonorthogonal* to the first. With k levels of an ANOVA factor *and* when there are equal N s in each cell, two sets of contrast codes are orthogonal when

$$\sum_{i=1}^k w_{1i} w_{2i} = 0. \tag{X.X}$$

Here, w_{1i} denotes the code assigned to the i th level of the ANOVA factor on the *first* contrast coded variable, and w_{2i} denotes the code assigned to the i th level of the ANOVA factor on the *second* contrast coded variable. When there are equal N s in each cell, two sets of contrast codes are nonorthogonal when Equation X.X does not hold.

Table 1.4 gives some of the possible pairs of contrast codes for those examples previously given in Table 1.3. Let us assume that the ANOVA has an equal number of observations at each level. Then, example codes 1 and 2 are nonorthogonal because

$$\sum_{i=1}^3 w_{1i} w_{2i} = -1.$$

Example codes 3 and 4 as well as example codes 2 and 5 are orthogonal.

Table 1.4 Examples of orthogonal and nonorthogonal contrast coded variables.

Example:	Genotype:			$\sum w_{1i} w_{2i} =$
	++	+-	--	
1:	-1	1	0	
2:	1	0	-1	
$w_{1i} w_{2i} =$	-1	0	0	-1
3:	2	-1	-1	
4:	0	1	-1	
$w_{1i} w_{2i} =$	0	-1	1	0
2:	1	0	-1	
5:	-1	2	-1	
$w_{1i} w_{2i} =$	-1	0	1	0

When there are unequal numbers of observations, then the definition of orthogonal contrast codes is somewhat different. Let N_i denote the number of observations in the i th level of the ANOVA factor. Then for an unbalanced ANOVA, two sets of contrast codes will be orthogonal when

$$\sum_{i=1}^k \frac{w_{1i}w_{2i}}{N_i} = \frac{w_{11}w_{21}}{N_1} + \frac{w_{12}w_{22}}{N_2} + \dots + \frac{w_{1k}w_{2k}}{N_k} = 0. \quad (\text{X.X})$$

With k levels for an ANOVA factor, it is possible to have up to $(k - 1)$ sets of contrast codes. (Note that it is not necessary to code all $(k - 1)$ sets, although doing so can have some statistical advantage. We discuss this later in Section X.X). If all pairs of contrast codes satisfy Equation X.X (equal N case) or Equation X.X (unequal N case), then the set of codes is completely orthogonal.

1.2.3.3 Orthogonal and non-orthogonal contrast codes

At this point, a short digression is necessary to discuss the concept of orthogonal and non-orthogonal contrast codes. First a comment about terminology is in order. Recall that the term “orthogonal” has the generic meaning of “being uncorrelated.” Hence, “non-orthogonal” implies a correlation. Both terms are applied to three separate concepts: (1) an ANOVA design (see Section X.X); (2) the series of numbers (i.e., contrast codes) assigned to the levels of an ANOVA factor; and (3) the independent variables generated from the contrast codes. The key point is that orthogonality is *not necessarily* transitive over these three concepts. That is, an orthogonal ANOVA design does *not* imply that a set of contrast codes is orthogonal; an orthogonal contrast code does *not* imply that the ANOVA design is orthogonal; and orthogonal contrast codes do *not* imply that the independent variables generated from those codes are uncorrelated.

There is one exception to this rule—when the ANOVA design is balanced and when contrast codes are orthogonal. Under these circumstances, the resulting independent variables will be uncorrelated. In addition, if the ANOVA factor in the balanced design has k levels, and there $(k - 1)$ orthogonal contrast codes, then the SS , summed over all the $(k - 1)$ independent variables, equals the SS for the ANOVA factor from a classic ANOVA. We saw an illustration of this in the BDNF example given above in Section X.X. Because the SS for the model are equal in this special case, orthogonal contrast codes effectively perform a classic ANOVA but with an important twist. The classic ANOVA tests one and only one null hypothesis—can the k group means be regarded as being sampled from a single hat of means? With orthogonal contrast codes, a *series* of null hypotheses about the means can be tested, each with one degree of freedom. In this way, the investigator usually learns more about the group means than just performing a classic ANOVA, while at the same time performing a statistical analysis that is mathematically equivalent to the ANOVA.

In a balanced ANOVA, orthogonal contrast codes have two major advantages over post hoc multiple comparison procedures (or MCPs, see Section X.X). First, the investigator can test his/her own hypotheses with orthogonal contrast codes. Most post hoc tests are atheoretical. Second, because the comparison of means using orthogonal contrast codes is planned or a priori, there is no need to adjust alpha or jump through any of the other statistical gyrations associated with MCPs. Hence, statistical power is almost always increased.

The mathematical niceties of orthogonal contrast codes, however, should always be sacrificed to clearly stated, substantive hypotheses. If hypotheses dictate that contrasts be non-orthogonal, then substantive considerations should always take precedence.

1.2.3.4 Comparing each treatment mean to a control mean

Non-orthogonal contrasts can also be used to compare each treatment mean to a control mean. The fundamental setup of these codes is illustrated in Table 1.5 in which the ANOVA

factor has four levels, a control level with mean \bar{Y}_C and three treatment levels with means \bar{Y}_{T1} through \bar{Y}_{T3} . Just assign the value of 1 to the control mean for every contrast. In the first contrast assign -1 to the first treatment mean and 0 to all other treatment means. The remaining contrasts then assign -1 to the treatment mean of interest and 0 to all other treatment means.

Table 1.5 Non-orthogonal contrast codes for comparing each treatment mean to a control mean.

Contrast Code:	Group Mean:			
	\bar{Y}_C	\bar{Y}_{T1}	\bar{Y}_{T2}	\bar{Y}_{T3}
w_1	1	-1	0	0
w_2	1	0	-1	0
w_3	1	0	0	-1

1.2.3.5 Contrast Codes: Orthogonal Polynomials

When the levels of the ANOVA factor are ordered groups, then orthogonal polynomial contrast codes are often informative. The first code fits a linear term to the group means. That is, it fits a straight line through the means. The second code fits a quadratic term—i.e., a parabola. The third fits a cubic, the fourth, a quartic, and so on. The key assumption is that the groups are evenly spaced.

The use of orthogonal polynomial contrast codes is very similar to the use of regression with ordered groups discussed in Section X.X. Regression with ordered groups, moreover, is much easier to apply to data, especially when the statistical package does not have contrast options with an ANOVA, ANCOVA, or GLM procedure. Hence, the reader could use the techniques outlined in Section X.X to fit orthogonal polynomials. The major difference between contrast codes in ANOVA and polynomial regression with ordered group lies in the error term for the F ratio.

With k levels to an ANOVA factor, the error variance from a oneway ANOVA may be viewed as the error from fitting a polynomial of order $(k - 1)$ to the data. Hence, if there are five levels, then the error variance from a oneway ANOVA is equal to fitting four orthogonal contrast codes—linear, quadratic, cubic, and quartic. In regression with ordered groups, however, the error term is derived from the best fitting polynomial, which could be a quadratic. Still, the difference between ANOVA with orthogonal polynomial contrast codes and regression with ordered groups should be slight. The reason is that the higher order polynomials ignored in the regression are insignificant and hence will not greatly reduce error.

Coding schemes for orthogonal polynomials for up to eight levels of an ANOVA factor are presented in Table 1.6. Note that it is not necessary to fit all terms to an ANOVA factor. For example, if the ANOVA factor has five levels, it is permissible to test only the linear and the quadratic term.

Table 1.6 Orthogonal polynomial codes for ANOVA factors with up to eight levels.

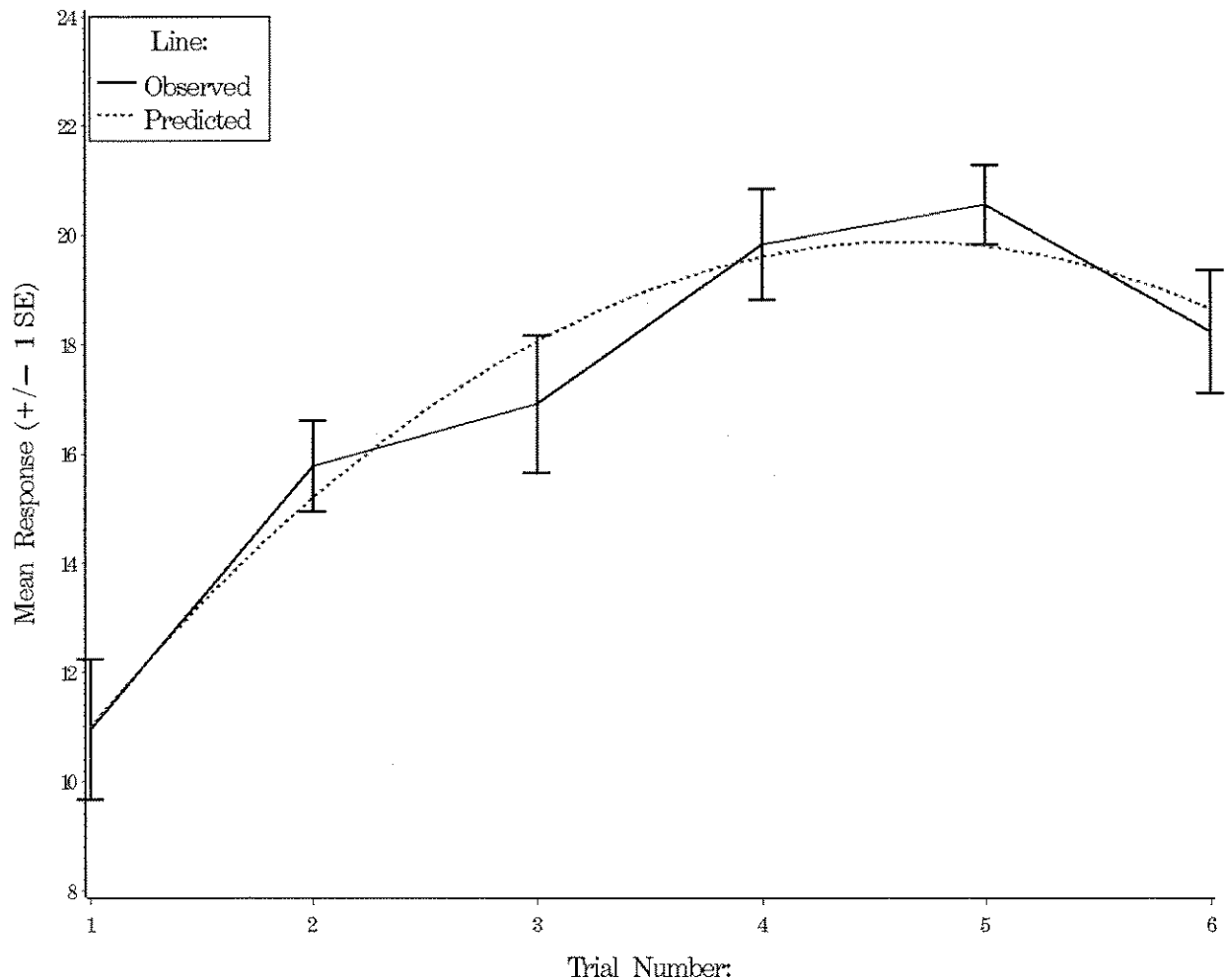
Order:	Level of ANOVA factor:							
$k=3$	1	2	3					
1	-1	0	1					
2	-1	2	-1					
$k=4$	1	2	3	4				
1	-3	-1	1	3				
2	1	-1	-1	1				
3	-1	3	-3	1				
$k=5$	1	2	3	4	5			
1	-2	-1	0	1	2			
2	2	-1	-2	-1	2			
3	-1	2	0	-2	1			
4	1	-4	6	-4	1			
$k=6$	1	2	3	4	5	6		
1	-5	-3	-1	1	3	5		
2	5	-1	-4	-4	-1	5		
3	-5	7	4	-4	-7	5		
4	1	-3	2	2	-3	1		
5	-1	5	-10	10	-5	1		
$k=7$	1	2	3	4	5	6	7	
1	-3	-2	-1	0	1	2	3	
2	5	0	-3	-4	-3	0	5	
3	-1	1	1	0	-1	-1	1	
4	3	-7	1	6	1	-7	3	
5	-1	4	-5	0	5	-4	1	
6	1	-6	15	-20	15	-6	1	
$k=8$	1	2	3	4	5	6	7	8
1	-7	-5	-3	-1	1	3	5	7
2	7	1	-3	-5	-5	-3	1	7
3	-7	5	7	3	-3	-7	-5	7
4	7	-13	-3	9	9	-3	-13	7
5	-7	23	-17	-15	15	17	-23	7
6	1	-5	9	-5	-5	9	-5	1
7	-1	7	-21	35	-35	21	-7	1

1.2.3.6 Contrast Codes: Helmert Codes

Many studies in neuroscience assess the time point (or dosage level) at which a response starts or stops. When the response curves are monotonic, then contrast codes called *Helmert* codes are useful. When issue is when a response stops, then the Helmert code compares the mean for a time point against the average of the means *after* that time point. When the issue is about the starting point for a response, then the Helmert code compares the mean for a time point against the average of the means *before* that time point³.

We illustrate Helmert codes with an example. Suppose that a researcher interested in learning examined the response of a biochemical parameter in the CNS as a function of the learning trial. Measurement of the response requires sacrifice of the animals. Hence, different groups of animals are required for each learning trial. Figure 1.6 presents the results of this study along with the predicted response from the best fitting polynomial (a quadratic).

Figure 1.6 Mean (+/- 1 SEM) responses for learning trials along with the predicted values from the best fitting polynomial.



³ This is usually referred to as a *reverse* Helmert code.

It is obvious from both the plot of observed means and the quadratic that the response increases until the fourth trial. Let us see whether the Helmert codes reveal that. The ANOVA factor in this example can be called Trial Number with levels of Trial1 through Trial6. Because there are 6 levels, we construct 5 contrast-coded variables. The first of these compares the mean of Trial 1 against the average of the means of Trials 2 through 6. This code is completely analogous to testing a “Control” (here, Trial1) against the average of “Treatments” (here, Trials 2 through 6). Hence, the equation for this variable is

$$5\bar{Y}_1 - \bar{Y}_2 - \bar{Y}_3 - \bar{Y}_4 - \bar{Y}_5 - \bar{Y}_6 = 0.$$

The second Helmert code is designed to test whether the mean for the next level of the ANOVA factor, Trial2, differs from the overall mean of the remaining trials, 3 through 6. Here, we assign a value of 0 to Trial 1 because we are not interested in that any more, treat Trial2 as a “Control” and the remaining trials as “Treatments.” The resulting code is

$$0\bar{Y}_1 + 4\bar{Y}_2 - \bar{Y}_3 - \bar{Y}_4 - \bar{Y}_5 - \bar{Y}_6 = 0.$$

These and the remaining contrast codes are given in Table 1.7. Note that all rows in Table 1.7 sum to 0, a necessity for contrast codes. Note also that Helmert codes are orthogonal. The product of the codes in each of the first four columns of Table 1.7 is 0. The product of the 5th column is 1, while the product of the last column is -1. Hence, the sum of the products equals 1 - 1 = 0. This is true of all Helmert codes, regardless of the number of levels.

Table 1.7 Example of reverse Helmert codes used to detect the ending point of a response.

Contrast-coded Variable:	Value assigned to level:					
	Trial1	Trial2	Trial3	Trial4	Trial5	Trial6
Trial1 vs Rest	5	-1	-1	-1	-1	-1
Trial2 vs Rest	0	4	-1	-1	-1	-1
Trial3 vs Rest	0	0	3	-1	-1	-1
Trial4 vs Rest	0	0	0	2	-1	-1
Trial5 vs Rest	0	0	0	0	1	-1

We now use the Helmert contrast-coded variables as the independent variables in the GLM. Fitting these to the data from Figure 1.6 gives a significant overall fit— $R^2 = .39$, $df = (5, 84)$, $p < .0001$. Hence, we can interpret the significance of the individual contrast-coded variables with some confidence. Figure 1.7 gives those results. We see that the results of Trial1 vs Rest through Trial3 vs Rest are significant. The remaining two variables are not significant. Hence, we conclude—as Figure 1.6 clearly illustrates—that the response stops changing at Trial4.

Figure 1.7 Results of testing Helmert contrast-coded variables.

Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F
Trial1 vs Rest	1	668.3168000	668.3168000	39.71	<.0001
Trial2 vs Rest	1	115.1960333	115.1960333	6.84	0.0105
Trial3 vs Rest	1	77.7493889	77.7493889	4.62	0.0345
Trial4 vs Rest	1	1.9067778	1.9067778	0.11	0.7373
Trial5 vs Rest	1	40.1363333	40.1363333	2.38	0.1263

The process of ascertaining the starting point for a response works in the opposite way. Here, the type of relationship starts out “flat” and then rapidly ascends (or descends). Figure 1.8 illustrates such a curve. The Helmert codes for detecting the starting Trial for the response (which is Trial 5) are given in Table 1.8.

Figure 1.8 Mean (± 1 SEM) responses for learning trials along with the predicted values from the best fitting polynomial; example of Helmert contrast coding to determine the starting point of a response.

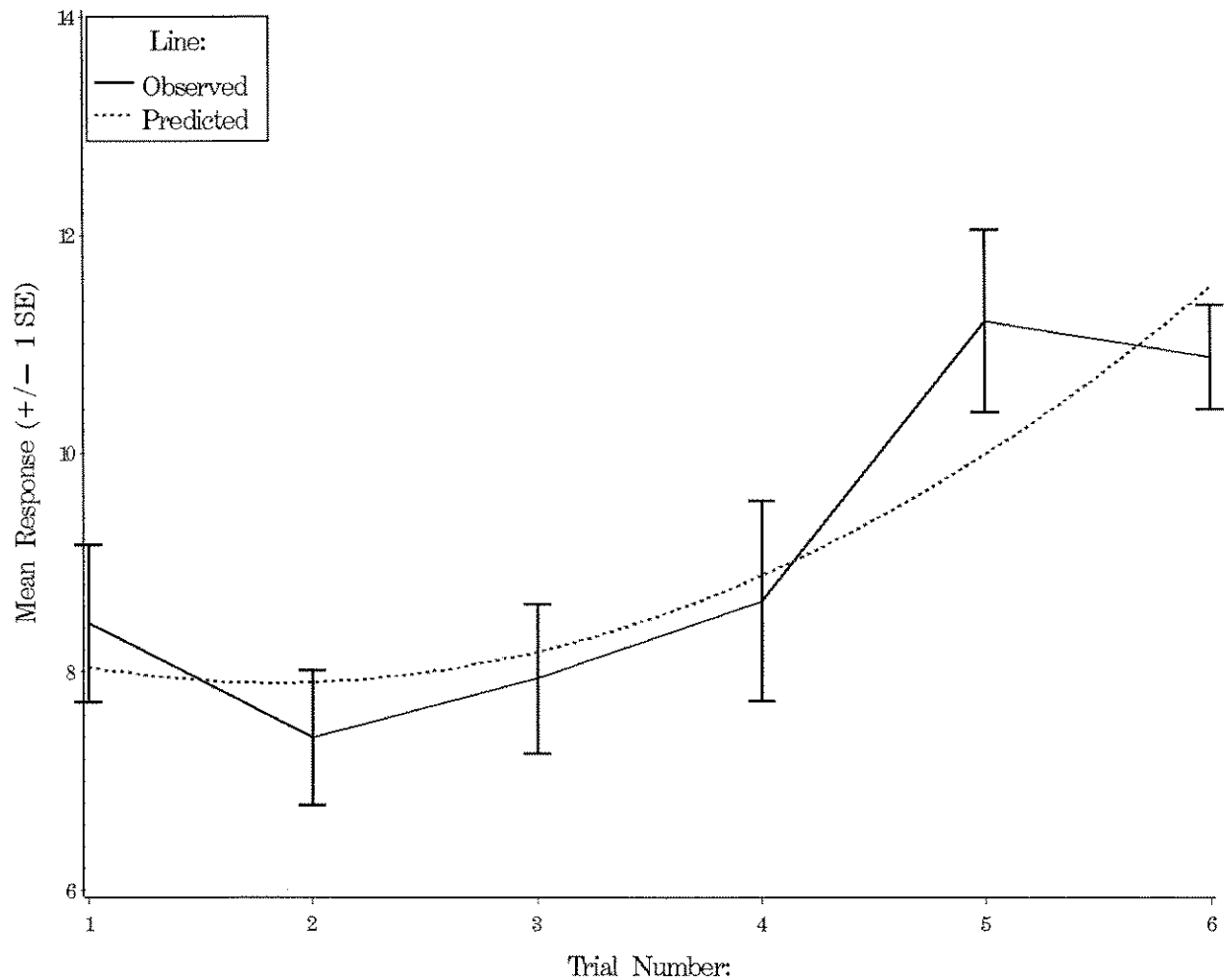


Table 1.8 Example of reverse Helmert codes to detect the starting point of a response.

Contrast-coded Variable:	Value assigned to level:					
	Trial1	Trial2	Trial3	Trial4	Trial5	Trial6
Rest vs Trial 2	-1	1	0	0	0	0
Rest vs Trial 3	-1	-1	2	0	0	0
Rest vs Trial 4	-1	-1	-1	3	0	0
Rest vs Trial 5	-1	-1	-1	-1	4	0
Rest vs Trial 6	-1	-1	-1	-1	-1	5

1.2.3.7 Implementing contrast codes: GLM Procedures with “Contrast” statements

Most modern statistical packages have the equivalent of a “Contrast” statement that allows one to provide contrast codes within an ANOVA, ANCOVA, or GLM procedure. In

these situations, the procedure will perform the classic ANOVA and then provide statistical tests for the hypotheses generated by the contrast code.

Figure 1.9 gives the output from PROC GLM in SAS used to analyze the PKC-gamma data. The code that generated this output contained two contrast statements, both designed to explore the effect of knocking out a PKC-gamma allele. The first contrast statement assigned the numeric values of 2, -1, and -1 to, respectively, genotypes ++, +-, and --. This contrast asks whether the average of the two genotypes having at least one knockout allele differs from the wild-type genotype. The second contrast assigned codes of 0, -1, and 1; this tests whether the heterozygote mean differs from the homozygote knockout mean.

Figure 1.9 Output from a oneway ANOVA with orthogonal contrasts.

Dependent Variable: Open_Arm Percent time in open arm						
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F	
Model	2	1154.920444	577.460222	10.91	0.0002	
Error	42	2223.837333	52.948508			
Corrected Total	44	3378.757778				
R-Square		Coeff Var	Root MSE	Open_Arm Mean		
0.341818		59.53559	7.276573	12.22222		
Source	DF	Type III SS	Mean Square	F Value	Pr > F	
Genotype	2	1154.920444	577.460222	10.91	0.0002	
Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F	
++ v Rest	1	291.960111	291.9601111	5.51	0.0236	
+ - v --	1	862.960333	862.9603333	16.30	0.0002	

The initial part of the output is identical to that of a oneway ANOVA with Genotype as the ANOVA factor. The only difference is the last section of output that gives the results of the two contrasts. The routine computes the *SS* for a contrast and the *MS* for the contrast. (Because a contrast always involves 1 degree of freedom, the *MS* for the contrast will always equal the *SS*). The *F* ratio for the contrast equals the *MS* for that contrast divided by the error *MS* from the model. Hence, the *F* ratio for the first contrast (“++ v Rest”) will equal

$$F_{++ \text{ v Rest}} = \frac{291.9601}{52.9485} = 5.51.$$

The numerator degrees of freedom for this *F* equal the *df* for the contrast (i.e., 1), and the denominator *df* equals the error *df* for the model (i.e., 42). Hence, the *p* value is the probability of observing an *F* greater than 5.51 from an *F* distribution with (1, 42) degrees of freedom. Because the observed *p* value of .02 is less than .05, we reject the null hypothesis that the knockout of at least one PKC-gamma allele has no effect on the percent of time spent in the open arm of an elevated plus-maze.

The *F* for the second contrast (“+ - v --”) divides the *MS* for this contrast by the error *MS*:

$$F_{+-v..} = \frac{862.9603}{52.9485} = 16.30.$$

The *df* for this contrast will also be (1, 42). Because the *p* value for this test is much less than .05, we conclude that the mean for the heterozygote is significantly different from that of the double knockout homozygote.

Note that these contrast codes are orthogonal and the ANOVA design is balanced (15 mice per genotype). Hence, the *SS* for both contrasts in Figure 1.9 add up to the *SS* for the ANOVA factor Genotype.

Figure 1.10 presents results from fitting two non-orthogonal contrasts to the PKC-gamma data. The first contrast assigned the codes 1, -1, and 0 to, respectively genotypes ++, +-, and --, thus testing the difference between the means of the wild-type homozygote and the heterozygote. The second contrast used the codes of 1, 0 and -1, so it tests for mean differences between the wild-type homozygote and the double knockout homozygote.

Figure 1.10 Output from a oneway ANOVA with non-orthogonal contrasts.

Dependent Variable: Open_Arm Percent time in open arm						
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F	
Model	2	1154.920444	577.460222	10.91	0.0002	
Error	42	2223.837333	52.948508			
Corrected Total	44	3378.757778				
R-Square		Coeff Var	Root MSE	Open_Arm Mean		
0.341818		59.53559	7.276573	12.22222		
Source	DF	Type III SS	Mean Square	F Value	Pr > F	
Genotype	2	1154.920444	577.460222	10.91	0.0002	
Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F	
++ v +-	1	0.0120000	0.0120000	0.00	.9881	
++ v --	1	869.4083333	869.4083333	16.42	.0002	

Just as in the orthogonal contrast, the *F* statistic for a non-orthogonal contrast equals the *MS* for that contrast divided by the error *MS* for the model, and the *df* for the contrast has 1 in the numerator and the error degrees of freedom in the denominator. The first contrast (“++ v +-”) is not significant. This agrees well with the observed data in **Error! Reference source not found.** which reveals only a small mean difference between the ++ and the +- genotypes. The second contrast (“++ v --”) is highly significant, consistent with the large mean difference between the ++ and the -- genotypes in **Error! Reference source not found.**

1.2.3.8 Implementing contrast codes: Software without “Contrast” statements

Some statistical software does not provide the option of “Contrast” statements with their ANOVA, ANCOVA, or GLM routines. One can still perform contrasts in these cases. If $(k - 1)$ contrasts are all coded and if all contrasts are orthogonal, then one can simply create new independent variables from the contrast codes and then regress the dependent variable on these contrast-coded independent variables. For example, in the coding scheme used above in Figure 1.9, we would create a new variable—let us call it CC1—that has a value of 2 if the genotype is ++ and a value of -1 otherwise. The second new variable, CC2, would have a value of 0 for genotype ++, 1 for genotype +-, and -1 for genotype --. We would then regress the dependent variable on CC1 and CC2. Figure 1.11 gives the output from this regression.

Figure 1.11 Solving for contrast-coded variables using regression: orthogonal contrast codes.

Dependent Variable: Open_Arm Percent time in open arm						
Analysis of Variance						
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F	
Model	2	1154.92044	577.46022	10.91	0.0002	
Error	42	2223.83733	52.94851			
Corrected Total	44	3378.75778				
Root MSE		7.27657	R-Square	0.3418		
Dependent Mean		12.22222	Adj R-Sq	0.3105		
Coeff Var		59.53559				
Variable	Label	DF	Parameter Estimate	Standard Error	t Value	Pr > t
Intercept	Intercept	1	12.22222	1.08473	11.27	<.0001
CC1	++ v Rest	1	-1.80111	0.76702	-2.35	0.0236
CC2	+- v --	1	-5.36333	1.32851	-4.04	0.0002

Note that the analysis of variance table in Figure 1.11 is identical to the one in Figure 1.9. Results of the two contrast-coded variables, CC1 and CC2, are also identical albeit expressed in a different form. The F statistics in Figure 1.9 are the square of the t statistics in Figure 1.11. The p values for the contrast-coded variables in Figure 1.11 are identical to those for the Contrast statements used to generate the results in Figure 1.9.

If (1) there are fewer than $(k - 1)$ contrasts or (2) the contrasts are non-orthogonal, then the solution is still tractable, albeit more cumbersome. Follow these steps:

- (1) Perform a classic ANOVA on the data.
- (2) Record the error df and the error MS from the results of the classic ANOVA.
- (3) Compute new independent variables using the contrast codes.
- (4) Using a regression procedure, regress the dependent variable on the first contrast-coded independent variable; do *not* regress it on *all* the contrast-coded independent variables.

- (5) Take the model sum of squares from this regression and divide it by the error *MS* from the classic ANOVA; this gives the *F* statistic for this contrast-coded independent variable.
- (6) The *F* statistic will have a numerator degrees of freedom equal to 1; the denominator *df* will equal the error *df* from the classic ANOVA.
- (7) Compute (or look up) the *p* value for the *F*; note that, because every contrast will have the same degrees of freedom in the numerator and in the denominator, the critical value for the *F* will be the same for all contrasts; hence, you may prefer to compute (or look up) the critical value for *F* and compare the observed *F* to that critical value.
- (8) Repeat steps (4) through (7) for the *next* contrast-coded variable; continue these steps until all contrast-coded variables have been analyzed.

We illustrate this procedure using the non-orthogonal contrast codes for the PKC-gamma data given above in Figure 1.10. Instead of reproducing the classic ANOVA, we can take the relevant numbers from that Figure—i.e., error *df* = 42 and error *MS* = 52.9485.

Figure 1.12 Regression analysis for non-orthogonal contrasts: first independent variable.

Dependent Variable: Open_Arm Percent time in open arm						
Analysis of Variance						
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F	
Model	1	0.01200	0.01200	0.00	0.9902	
Error	43	3378.74578	78.57548			
Corrected Total	44	378.75778				
Root MSE		8.86428	R-Square	0.0000		
Dependent Mean		12.22222	Adj R-Sq	-0.0233		
Coeff Var		72.52594				
Variable	Label	DF	Parameter Estimate	Standard Error	t Value	Pr > t
Intercept	Intercept	1	12.22222	1.32141	9.25	<.0001
CC1	++ v +-	1	-0.02000	1.61839	-0.01	0.9902

The first step is to construct a new independent variable from the first contrast code. This new variable, which we shall call CC1, has a value of 1 if the genotype is ++, a value of -1 if the genotype is +-, or a value of 0 if the genotype is --. Next, we regress the dependent variable, Open_Arm, on independent variable CC1. The results from this regression are given in Figure 1.12. The sum of squares for this regression is .012. (Note that this is also the value for the *SS* of the contrast using a contrast statement in Figure 1.10). Hence, the *F* ratio for this contrast is

$$F_{CC1} = \frac{SS_{CC1}}{MS_{error}} = \frac{.012}{52.9485} = 0.002.$$

The degrees of freedom for this *F* are (1, 42), and the *p* level is .988. Thus, there is no evidence that the means for the wild-type homozygote and the heterozygote differ.

We now move to the second independent variable. This will have values of 1 (genotype ++), 0 (genotype +-), or -1 (genotype --). Calling this variable CC2, we regress dependent variable Open_Arm on CC2. The results are given in Figure 1.13.

Figure 1.13 Regression analysis for non-orthogonal contrasts: second independent variable.

Dependent Variable: Open_Arm Percent time in open arm						
Analysis of Variance						
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F	
Model	1	869.40833	869.40833	14.90	0.0004	
Error	43	2509.34944	58.35696			
Corrected Total	44	3378.75778				
Root MSE		7.63917	R-Square	0.2573		
Dependent Mean		12.22222	Adj R-Sq	0.2400		
Coeff Var		62.50232				
Variable	Label	DF	Parameter Estimate	Standard Error	t Value	Pr > t
Intercept	Intercept	1	12.22222	1.13878	10.73	<.0001
CC2	++ v --	1	-5.38333	1.39472	-3.86	0.0004

The SS for the model from this regression is 869.4083 (once again, the same number given in the Figure 1.10 using a contrast statement). Hence, the *F* statistic for the second contrast-coded independent variable is

$$F_{CC2} = \frac{SS_{CC2}}{MS_{error}} = \frac{869.4083}{52.9485} = 16.42.$$

With *df* of (1, 42), the *p* level for this *F* is .0002. (You should verify that this *F*, its degrees of freedom, and the *p* value are the same as those in Figure 1.10). We conclude that there is strong evidence that the means for the two homozygotes differ.

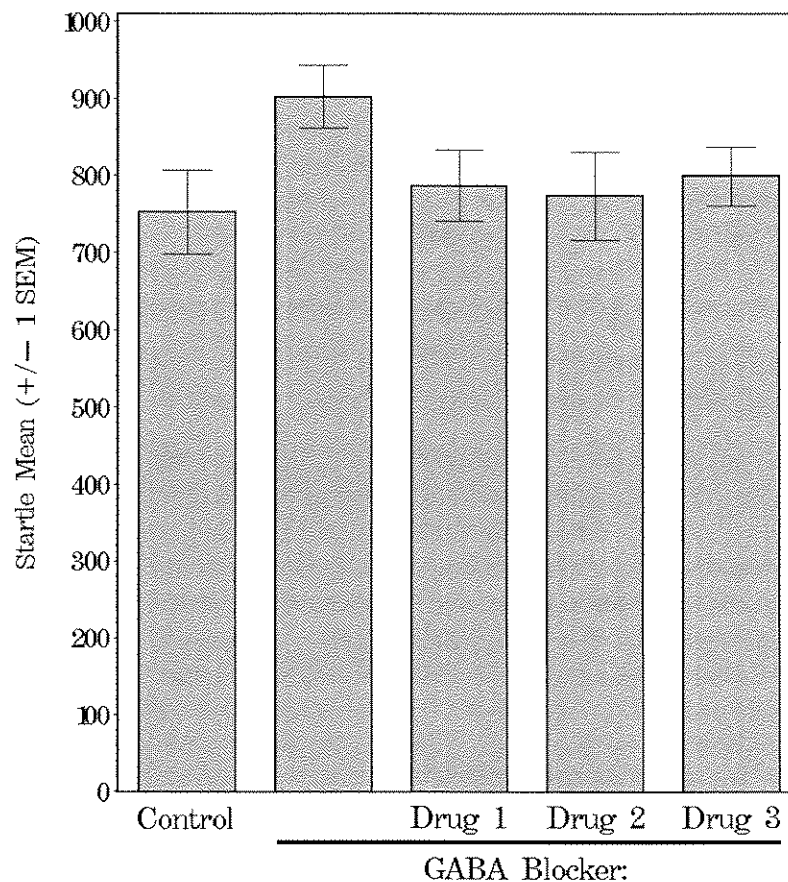
Note that we arrived at the same substantive results performing these hand calculations as we would have just examining the output from the two simple regressions in Figure 1.12 and Figure 1.13. This happened largely because of the example that we used. For the PKC-gamma data, the difference between the mean for genotype ++ and the mean for genotype +- is very small, so it is highly unlikely that a minor change in technique would ever make this difference significant. Similarly, the difference between the ++ mean and the - mean is very large; it would be very surprising if any reasonable test for this difference would not reach statistical significance. In general, however, the results from the simple regressions and those from the hand-calculated contrasts will not always be equal.

Examples:
Coding Several Hypotheses

Sometimes a study involves several groups, but only a few comparisons are of interest. Suppose that a lab interested in developmental effects on anxiety administered a GABA blocker to rat pups for two weeks shortly after birth and then tested them as adults. Naturally, there would be a control group who received vehicle injections. In the adult testing, those rats who had received the GABA blocker are randomly divided into four groups: a control, and three groups, each administered an anxiolytic compound shortly before testing. The dependent variable in this case is a measure of startle. The group has two major hypotheses: (1) administration of the GABA antagonist in early postnatal weeks will result in increased anxiety as adults; and (2) this effect will be blocked by each of the three anxiolytic agents.

Figure 1.14 presents the results of this hypothetical study.

Figure 1.14 Mean (+/- 1 SEM) startle as a function of early exposure to a GABA blocker and three anxiolytic drugs.



An overall ANOVA on these data would be inefficient because there are only two hypotheses to be tested. Hence, one can construct two sets of contrast codes, one for each hypothesis, and then examine the significance level of these two contrasts.

Let \bar{Y}_c denote the mean of the controls and \bar{Y}_0 through \bar{Y}_3 denote the means of the groups administered the GABA blocker, the subscript denoting the number of the anxiolytic drug. The

very first contrast code would have the set of numbers (1 -1 0 0 0) for, respectively, the groups as ordered in Figure 1.14. This code embodies the following null hypothesis

$$\bar{Y}_C - 1(\bar{Y}_0) + 0(\bar{Y}_1) + 0(\bar{Y}_2) + 0(\bar{Y}_3) = \bar{Y}_C - \bar{Y}_0 = 0.$$

Substantively, this code tests whether the GABA antagonist had an effect on startle.

The second code tests whether the three groups given the anxiolytic differ from the group previously administered the GABA blocker but receiving no anxiolytic before testing. The appropriate code here would be (0 3 -1 -1 -1), giving the null hypothesis

$$0(\bar{Y})_C + 3(\bar{Y}_0) - 1(\bar{Y}_1) - 1(\bar{Y}_2) - 1(\bar{Y}_3) = \bar{Y}_0 - \frac{\bar{Y}_1 + \bar{Y}_2 + \bar{Y}_3}{3} = 0.$$

Hence, this tests whether the GABA-inhibitor only group differs from the average mean of the GABA-inhibitors receiving an anxiolytic.

Figure 1.15 presents the results of fitting the ANOVA to these data. Note that the overall ANOVA is not significant. This is not a problem because the two hypotheses are embodied in the contrasts. The only utility of the overall ANOVA is to give an estimate of the error variance that is used in testing the significant of the contrasts.

Figure 1.15 Results of the two contrasts.

Dependent Variable: Startle					
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	4	163252.718	40813.179	1.47	0.2254
Error	55	1532196.322	27858.115		
Corrected Total	59	1695449.039			
R-Square		Coeff Var	Root MSE	Startle Mean	
0.096289		20.80112	166.9075	802.3967	
Source	DF	Type III SS	Mean Square	F Value	Pr > F
Group	4	163252.7177	40813.1794	1.47	0.2254
Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F
Ctrl v GABA Blkr	1	134430.6017	134430.6017	4.83	0.0323
No Drug v Drug	1	121626.5625	121626.5625	4.37	0.0413

Both contrasts are significant. The first, labeled “Ctrl v GABA Blkr” in the output, tells us that mean for the group receiving only GABA blocker does in fact differ from the Control mean. From Figure 1.14, we see that this is an anxiogenic effect—the early GABA blocker increases startle in the adult rat.

The second contrast tells us that there was an overall effect of the anxiolytic drugs. Comparison of the means of these three groups with the mean for the GABA blocker only group tells us that the drugs reduced startle.